	udent: ite:	Instructor: Alfredo Alvarez Course: 2413 Cal I	Assignment: calmath2413alvarez139nextfinaal	
1.		ne function s(t) represents the position of an object at time t moving along a line. Suppose s(2) = 135 and s(4) = 183. Find e average velocity of the object over the interval of time [2,4].		
	The average velocity over the	ne interval [2,4] is v _{av} = (Sim	plify your answer.)	
	Answer: 24			
2.	The position of an object mo object over the following inte		= - 15t ² + 120t. Find the average velocity of the	
	(a) [1, 10]	(b) [1, 9]		
	(c) [1, 8]	(d) [1, 1 + h] where h > 0 is	s any real number.	
	(a) The average velocity of	the object over the interval [1, 10] is		
	(b) The average velocity of	the object over the interval [1, 9] is		
	(c) The average velocity of	the object over the interval [1, 8] is		
	(d) The average velocity of	the object over the interval [1, 1 + h] is		
	Answers - 45			
	- 30			
	- 15			
	– 15h + 90			

^{3.} For the position function $s(t) = -16t^2 + 111t$, complete the following table with the appropriate average velocities. Then make a conjecture about the value of the instantaneous velocity at t = 1.

Time Interval	[1, 2]	[1, 1.5]	[1, 1.1]	[1, 1.01]	[1, 1.001]
Average Velocity					

Complete the following table.

Time Interval	[1, 2]	[1, 1.5]	[1, 1.1]	[1, 1.01]	[1, 1.001]
Average Velocity					

(Type exact answers. Type integers or decimals.)

The value of the instantaneous velocity at t = 1 is	
(Round to the nearest integer as needed.)	

Answers 63

71 77.4 78.84 78.984 79 ^{4.} For the function $f(x) = 20x^3 - x$, make a table of slopes of secant lines and make a conjecture about the slope of the tangent line at x = 1.

Complete the table.

(Round the final answer to three decimal places as needed. Round all intermediate values to four decimal places as needed.)

Interval	Slope of secant line
[1, 2]	
[1, 1.5]	
[1, 1.1]	
[1, 1.01]	
[1, 1.001]	

An accurate conjecture for the slope of the tangent line at x = 1 is _____. (Round to the nearest integer as needed.)

Answers 139.000

94.000 65.200 59.600 59.100 59

5. Let $f(x) = \frac{x^2 - 16}{x + 4}$. (a) Calculate f(x) for each value of x in the following table. (b) Make a conjecture about the value of $\lim_{x \to -4} \frac{x^2 - 16}{x + 4}$.

(a) Calculate f(x) for each value of x in the following table.

х	- 3.9	- 3.99	- 3.999	- 3.9999
$f(x) = \frac{x^2 - 16}{x^2 - 16}$				
x + 4				
X	- 4.1	- 4.01	- 4.001	- 4.0001
$x^2 - 16$				
$f(x) = \frac{x+4}{x+4}$				

(Type an integer or decimal rounded to four decimal places as needed.)

(b) Make a conjecture about the value of
$$\lim_{x \to -4} \frac{x^2 - 16}{x+4}$$
.

$$\lim_{x \to -4} \frac{x^2 - 16}{x + 4} =$$
 (Type an integer or a decimal.)

Answers - 7.9

- 7.99 - 7.999 - 7.9999 - 8.1 - 8.01 - 8.001 - 8.0001
- 8

6. Let
$$g(t) = \frac{t-4}{\sqrt{t}-2}$$
.

a. Make two tables, one showing the values of g for t = 3.9, 3.99, and 3.999 and one showing values of g for t = 4.1, 4.01, and 4.001.

b. Make a conjecture about the value of $\lim_{t\to 4} \frac{t-4}{\sqrt{t}-2}$.

a. Make a table showing the values of g for t = 3.9, 3.99, and 3.999.

t	3.9	3.99	3.999
g(t)			

(Round to four decimal places.)

Make a table showing the values of g for t = 4.1, 4.01, and 4.001.

t	4.1	4.01	4.001	
g(t)				
(Deveral to form de size al planes)				

(Round to four decimal places.)

b. Make a conjecture about the value of $\lim_{t\to 4} \frac{t-4}{\sqrt{t}-2}$. Select the correct choice below and fill in any answer boxes in your

choice.

• A.
$$\lim_{t \to 4} \frac{t-4}{\sqrt{t}-2} =$$
 (Simplify your answer.)

O B. The limit does not exist.

Answers 3.9748

3.9975

3.9997

4.0248

4.0025

4.0003

A.
$$\lim_{t \to 4} \frac{t-4}{\sqrt{t}-2} =$$
 (Simplify your answer.)

7.	Use the graph to find the following limits	
	and function value.	
	a. lim f(x)	4-
	x→1 ⁻	2-
	b. lim f(x)	

- $x \to 1^+$ c. $\lim_{x \to 1} f(x)$
- **d.** f(1)

a. Find the limit. Select the correct choice below and fill in any answer boxes in your choice.

<mark>)</mark> A.	lim f(x) =	(Type an integer.)
	x→1 ⁻	

O B. The limit does not exist.

b. Find the limit. Select the correct choice below and fill in any answer boxes in your choice.

• A. $\lim_{x \to 1^+} f(x) =$ _____ (Type an integer.)

O B. The limit does not exist.

c. Find the limit. Select the correct choice below and fill in any answer boxes in your choice.

- A. $\lim_{x \to 1} f(x) =$ (Type an integer.)
- O B. The limit does not exist.

d. Find the function value. Select the correct choice below and fill in any answer boxes in your choice.

 \bigcirc **A.** f(1) = (Type an integer.)

- O B. The answer is undefined.
- Answers A. $\lim_{x \to 1^{-}} f(x) = 3$ (Type an integer.)
 - A. $\lim_{x \to 1^+} f(x) =$ **0** (Type an integer.)
 - B. The limit does not exist.
 - A. f(1) = **3** (Type an integer.)

8. Explain why
$$\lim_{x \to -5} \frac{x^2 + 8x + 15}{x + 5} = \lim_{x \to -5} (x + 3)$$
, and then evaluate $\lim_{x \to -5} \frac{x^2 + 8x + 15}{x + 5}$.

Choose the correct answer below.

A. Since each limit approaches -5, it follows that the limits are equal.
B. Since \$\frac{x^2 + 8x + 15}{x + 5}\$ = x + 3 whenever \$x \neq -5\$, it follows that the two expressions evaluate to the same number as x approaches -5.
C. The numerator of the expression \$\frac{x^2 + 8x + 15}{x + 5}\$ simplifies to \$x + 3\$ for all \$x\$, so the limits are equal.
D. The limits \$\lim_{x \rightarrow -5}\$ \$\frac{x^2 + 8x + 15}{x + 5}\$ and \$\lim_{x \rightarrow -5}\$ \$(x + 3)\$ equal the same number when evaluated using direct substitution.
Now evaluate the limit.
\$\lim_{x \rightarrow -5}\$ \$\frac{x^2 + 8x + 15}{x + 5}\$ and \$\lim_{x \rightarrow -5}\$\$ \$(Simplify your answer.)\$
Answers B. \$\lim_{x \rightarrow -5}\$ \$(Simplify yer x \neq -5)\$, it follows that the two expressions evaluate to the same number as \$x\$ approaches -5.

-2

9. Assume $\lim_{x\to 9} f(x) = 21$ and $\lim_{x\to 9} h(x) = 3$. Compute the following limit and state the limit laws used to justify the computation.

 $\lim_{x \to 9} \frac{f(x)}{h(x)}$ $\lim_{x \to 9} \frac{f(x)}{h(x)} =$ (Simplify your answer.)

Select each limit law used to justify the computation.

- A. Power
 B. Root
 C. Sum
 D. Difference
 E. Quotient
 F. Constant multiple
- **G.** Product

Answers 7

E. Quotient

10. Find the following limit or state that it does not exist.

$$\lim_{x \to 5} \frac{x^2 - 6x + 5}{x - 5}$$

Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

• A.
$$\lim_{x \to 5} \frac{x^2 - 6x + 5}{x - 5} =$$
 (Type an exact answer.)

O B. The limit does not exist.

Answer: A.
$$\lim_{x \to 5} \frac{x^2 - 6x + 5}{x - 5} =$$
4 (Type an exact answer.)

11. Find the following limit or state that it does not exist.

$$\lim_{x \to 100} \frac{\sqrt{x} - 10}{x - 100}$$

Simplify the given limit.

$$\lim_{x \to 100} \frac{\sqrt{x} - 10}{x - 100} = \lim_{x \to 100} ((Simplify your answer.))$$

Evaluate the limit, if possible. Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

○ A.
$$\lim_{x \to 100} \frac{\sqrt{x} - 10}{x - 100} =$$
 (Type an exact answer.)

O B. The limit does not exist.

Answers
$$\frac{1}{\sqrt{x} + 10}$$

A. $\lim_{x \to 100} \frac{\sqrt{x} - 10}{x - 100} = \frac{1}{20}$ (Type an exact answer.)

12. Determine the following limit at infinity.

$$\lim_{x \to \infty} \frac{f(x)}{g(x)} \text{ if } f(x) \rightarrow 200,000 \text{ and } g(x) \rightarrow \infty \text{ as } x \rightarrow \infty$$

Find the limit. Choose the correct answer below.

• A.
$$\lim_{x \to \infty} \frac{f(x)}{g(x)} = \infty$$

• B.
$$\lim_{x \to \infty} \frac{f(x)}{g(x)} = 0$$

• C.
$$\lim_{x \to \infty} \frac{f(x)}{g(x)} = 200,000$$

• D.
$$\lim_{x \to \infty} \frac{f(x)}{g(x)} = \frac{1}{200,000}$$

Answer: B.
$$\lim_{x \to \infty} \frac{f(x)}{g(x)} = 0$$

13. Determine the following limit at infinity.

$$\lim_{x \to \infty} \frac{5 + 3x + 4x^2}{x^2}$$

Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

• A. $\lim_{x \to \infty} \frac{5 + 3x + 4x^2}{x^2} =$ _____

 \bigcirc **B.** The limit does not exist and is neither $-\infty$ nor ∞ .

Answer: A.
$$\lim_{x \to \infty} \frac{5 + 3x + 4x^2}{x^2} =$$

14. Determine the following limit.

$$\lim_{w \to \infty} \frac{8w^2 + 3w + 9}{\sqrt{4w^4 + w^3}}$$

Select the correct choice below, and, if necessary, fill in the answer box to complete your choice.

• A.
$$\lim_{w \to \infty} \frac{8w^2 + 3w + 9}{\sqrt{4w^4 + w^3}} =$$
(Simplify your answer.)

○ **B.** The limit does not exist and is neither ∞ nor $-\infty$.

Answer: A.
$$\lim_{w \to \infty} \frac{8w^2 + 3w + 9}{\sqrt{4w^4 + w^3}} =$$
 4 (Simplify your answer.)

15. Determine the following limit.

$$\lim_{x \to -\infty} \frac{\sqrt{121x^2 + x}}{x}$$

Select the correct choice below, and, if necessary, fill in the answer box to complete your choice.

• A.
$$\lim_{x \to -\infty} \frac{\sqrt{121x^2 + x}}{x} =$$
(Simplify your answer.)

 \bigcirc **B.** The limit does not exist and is neither ∞ nor $-\infty$.

Answer: A.
$$\lim_{x \to -\infty} \frac{\sqrt{121x^2 + x}}{x} =$$
 (Simplify your answer.)

16. Determine $\lim_{x\to\infty} f(x)$ and $\lim_{x\to-\infty} f(x)$ for the following function. Then give the horizontal asymptotes of f, if any.

$$f(x) = \frac{3x}{21x + 3}$$

Evaluate $\lim_{x\to\infty} f(x)$. Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

• A. $\lim_{x \to \infty} \frac{3x}{21x + 3} =$ (Simplify your answer.)

 \bigcirc **B.** The limit does not exist and is neither ∞ nor $-\infty$.

Evaluate $\lim_{x \to -\infty} f(x)$. Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

• A. $\lim_{x \to -\infty} \frac{3x}{21x + 3} =$ (Simplify your answer.)

 \bigcirc **B.** The limit does not exist and is neither ∞ nor $-\infty$.

Give the horizontal asymptotes of f, if any. Select the correct choice below and, if necessary, fill in the answer box(es) to complete your choice.

- A. The function has one horizontal asymptote, _____.
 (Type an equation.)
- B. The function has two horizontal asymptotes. The top asymptote is ______ and the bottom asymptote is ______.
 (Type equations.)
- **C.** The function has no horizontal asymptotes.

Answers A.
$$\lim_{x \to \infty} \frac{3x}{21x + 3} = \frac{1}{7}$$
 (Simplify your answer.)
A.
$$\lim_{x \to -\infty} \frac{3x}{21x + 3} = \frac{1}{7}$$
 (Simplify your answer.)
A. The function has one horizontal asymptote, $y = \frac{1}{7}$. (Type an equation.)

17. Evaluate $\lim_{x\to\infty} f(x)$ and $\lim_{x\to-\infty} f(x)$ for the following rational function. Use ∞ or $-\infty$ where appropriate. Then give the horizontal asymptote of f (if any).

$$f(x) = \frac{16x^2 - 9x + 7}{4x^2 + 1}$$

Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

- A. $\lim_{x \to \infty} f(x) =$ (Simplify your answer.)
- O B. The limit does not exist and is neither ∞ nor -∞.

Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

- A. $\lim_{x \to -\infty} f(x) =$ (Simplify your answer.)
- \bigcirc **B.** The limit does not exist and is neither ∞ nor $-\infty$.

Identify the horizontal asymptote. Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

- A. The horizontal asymptote is y =
- O B. There are no horizontal asymptotes.
- Answers A. $\lim_{x \to \infty} f(x) = 4$ (Simplify your answer.)
 - A. $\lim_{x \to -\infty} f(x) =$ **4** (Simplify your answer.)
 - A. The horizontal asymptote is y = 4

18. Evaluate $\lim_{x\to\infty} f(x)$ and $\lim_{x\to-\infty} f(x)$ for the rational function. Then give the horizontal asymptote of f (if any).

$$f(x) = \frac{24x^8 - 2}{3x^8 - 4x^7}$$

Select the correct choice below, and, if necessary, fill in the answer box to complete your choice.

• A.
$$\lim_{x \to -\infty} \frac{24x^8 - 2}{3x^8 - 4x^7} =$$
(Simplify your answer.)

 \bigcirc **B.** The limit does not exist and is neither ∞ or $-\infty$.

Select the correct choice below, and, if necessary, fill in the answer box to complete your choice.

• A.

$$\lim_{x \to \infty} \frac{24x^8 - 2}{3x^8 - 4x^7} =$$
(Simplify your answer.)

 \bigcirc **B.** The limit does not exist and is neither ∞ or $-\infty$.

Select the correct choice below, and, if necessary, fill in the answer box to complete your choice.

- A. The function has a horizontal asymptote at y = _____.
 (Simplify your answer.)
- **B.** The function has no horizontal asymptote.

Answers A.
$$\lim_{x \to -\infty} \frac{24x^8 - 2}{3x^8 - 4x^7} = \mathbf{8}$$
 (Simplify your answer.)
A.
$$\lim_{x \to \infty} \frac{24x^8 - 2}{3x^8 - 4x^7} = \mathbf{8}$$
 (Simplify your answer.)
A. The function has a horizontal asymptote at $y = \mathbf{8}$. (Simplify your answer.)

19. Determine $\lim_{x\to\infty} f(x)$ and $\lim_{x\to-\infty} f(x)$ for the following function. Then give the horizontal asymptotes of f, if any.

$$f(x) = \frac{5x^4 - 8}{x^5 + 2x^3}$$

Evaluate $\lim_{x\to\infty} f(x)$. Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

• A.
$$\lim_{x \to \infty} \frac{5x^4 - 8}{x^5 + 2x^3} =$$
(Simplify your answer.)

 \bigcirc **B.** The limit does not exist and is neither ∞ nor $-\infty$.

- Evaluate $\lim_{x \to -\infty} f(x)$. Select the correct choice below and, if necessary, fill in the answer box to complete your choice.
- A. $\lim_{x \to -\infty} \frac{5x^4 8}{x^5 + 2x^3} =$ (Simplify your answer.)

 \bigcirc **B.** The limit does not exist and is neither ∞ nor $-\infty$.

Identify the horizontal asymptotes. Select the correct choice below and, if necessary, fill in the answer box(es) to complete your choice.

- A. The function has one horizontal asymptote, _____. (Type an equation.)
- B. The function has two horizontal asymptotes. The top asymptote is ______ and the bottom asymptote is ______.
 (Type equations.)
- **C.** The function has no horizontal asymptotes.

Answers A.
$$\lim_{x \to \infty} \frac{5x^4 - 8}{x^5 + 2x^3} = 0$$
 (Simplify your answer.)
A.
$$\lim_{x \to -\infty} \frac{5x^4 - 8}{x^5 + 2x^3} = 0$$
 (Simplify your answer.)
A. The function has one horizontal asymptote, $y = 0$. (Type an equation.)

20. Find all the asymptotes of the function.

$$f(x) = \frac{2x^2 + 4}{2x^2 - x - 36}$$

Find the horizontal asymptotes. Select the correct choice below and, if necessary, fill in the answer box(es) to complete your choice.

- B. The function has two horizontal asymptotes. The top asymptote is ______ and the bottom asymptote is ______.

(Type equations using y as the variable.)

○ C. The function has no horizontal asymptotes.

Find the vertical asymptotes. Select the correct choice below and, if necessary, fill in the answer box(es) to complete your choice.

A. The function has one vertical asymptote, ______. (Type an equation using x as the variable.)
B. The function has two vertical asymptotes. The leftmost asymptote is ______ and the rightmost asymptote is ______.

(Type equations using x as the variable.)

○ C. The function has no vertical asymptotes.

Find the slant asymptote(s). Select the correct choice below and, if necessary, fill in the answer box(es) to complete your choice.

<mark>)</mark> A.	The function has one slant asymptote,
	(Type an equation using x and y as the variables.)
⊖ В.	The function has two slant asymptotes. The asymptote with the larger slope is and the asymptote with the smaller slope is
	(Type equations using x and y as the variables.)
<mark>()</mark> C.	The function has no slant asymptotes.
Answ	pers A. The function has one horizontal asymptote, $y = 1$. (Type an equation using y as the variable.) B.
	The function has two vertical asymptotes. The leftmost asymptote is $x = -4$ and the rightmost
	asymptote is $x = \frac{9}{2}$.
	(Type equations using x as the variable.)
	C. The function has no slant asymptotes.

21. Determine whether the following function is continuous at a. Use the continuity checklist to justify your answer.

$$f(x) = \frac{2x^2 + 7x + 3}{x^2 - 7x}, a = 7$$

Select all that apply.

A. The function is continuous at a = 7.
B. The function is not continuous at a = 7 because f(7) is undefined.
C. The function is not continuous at a = 7 because lim f(x) does not exist. x→7
D. The function is not continuous at a = 7 because lim f(x) ≠ f(7). x→7
Answer: B. The function is not continuous at a = 7 because f(7) is undefined., C. The function is not continuous at a = 7 because lim f(x) does not exist., D. x→7
The function is not continuous at a = 7 because lim f(x) does not exist., D. x→7

22. Determine whether the following function is continuous at a. Use the continuity checklist to justify your answer.

$$f(x) = \begin{cases} \frac{x^2 - 169}{x - 13} & \text{if } x \neq 13\\ 10 & \text{if } x = 13 \end{cases}$$
; a = 13

Select all that apply.

A. The function is continuous at a = 13.

B. The function is not continuous at a = 13 because f(13) is undefined.

C. The function is not continuous at a = 13 because $\lim_{x\to 13} f(x)$ does not exist.

D. The function is not continuous at a = 13 because lim $f(x) \neq f(13)$.

Answer: D. The function is not continuous at a = 13 because $\lim_{x \to 13} f(x) \neq f(13)$.

23. Determine the intervals on which the following function is continuous.

$$f(x) = \frac{x^2 - 4x + 3}{x^2 - 9}$$

On what interval(s) is f continuous?

(Simplify your answer. Type your answer in interval notation. Use a comma to separate answers as needed.)

 $x \rightarrow 13$

Answer: $(-\infty, -3), (-3,3), (3,\infty)$

24. Evaluate the following limit.

$$\lim_{x \to 5} \sqrt{x^2 + 24}$$

Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

○ A. $\lim_{x\to 5} \sqrt{x^2 + 24} =$ _____, because $x^2 + 24$ is continuous for all x and the square root function is continuous for all x ≥ 0. (Type an integer or a fraction.)

 \bigcirc **B.** The limit does not exist and is neither ∞ nor $-\infty$.

Answer: A.

 $\lim_{x\to 5} \sqrt{x^2 + 24} = \boxed{7}$, because $x^2 + 24$ is continuous for all x and the square root function is continuous for all $x \ge 0$. (Type an integer or a fraction.)

25. Suppose x lies in the interval (4,6) with x ≠ 5. Find the smallest positive value of δ such that the inequality 0 < |x − 5| < δ is true for all possible values of x.

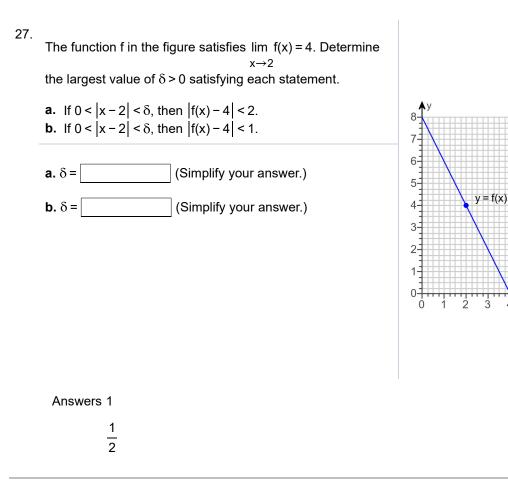
The smallest positive value of δ is	. (Type an integer or a fraction.)

Answer: 1

26. Suppose |f(x) - 5| < 0.3 whenever 0 < x < 5. Find all values of $\delta > 0$ such that |f(x) - 5| < 0.3 whenever $0 < |x - 1| < \delta$.

The values of δ are $0 < \delta \le$. (Type an integer or a fraction.)

Answer: 1



28. Use the precise definition of a limit to prove the following limit. Specify a relationship between ε and δ that guarantees the limit exists.

 $\lim_{x \to 0} (8x - 5) = -5$

Let $\varepsilon > 0$ be given. Choose the correct proof below.

○ A. Choose
$$\delta = 8\varepsilon$$
. Then, $|(8x - 5) - -5| < \varepsilon$ whenever $0 < |x - 0| < \delta$.

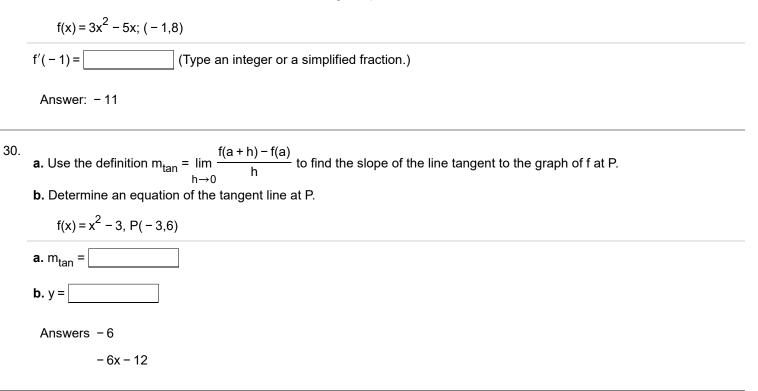
$$\bigcirc$$
 B. Choose $\delta = \frac{1}{5}$. Then, $|(8x-5) - -5| < \varepsilon$ whenever $0 < |x-0| < \delta$

○ **C.** Choose $\delta = \varepsilon$. Then, $|(8x-5) - -5| < \varepsilon$ whenever $0 < |x-0| < \delta$.

○ **D.** Choose
$$\delta = \frac{\varepsilon}{8}$$
. Then, $|(8x - 5) - -5| < \varepsilon$ whenever $0 < |x - 0| < \delta$

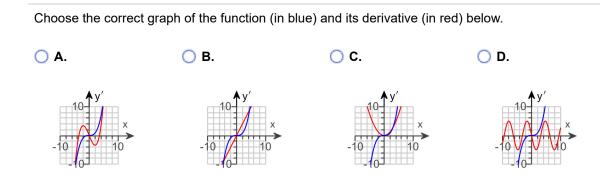
C E. None of the above proofs is correct.

Answer: D. Choose $\delta = \frac{\varepsilon}{8}$. Then, $|(8x-5) - 5| < \varepsilon$ whenever $0 < |x - 0| < \delta$. 29. Find the value of the derivative of the function at the given point.



31. Match the graph of the function on the right with the graph of its derivative.





Answer:



C.

32. A line perpendicular to another line or to a tangent line is called a normal line. Find an equation of the line perpendicular to the line that is tangent to the following curve at the given point P.

y = 11x + 23; P(-2,1)

The equation of the normal line at P(-2,1) is

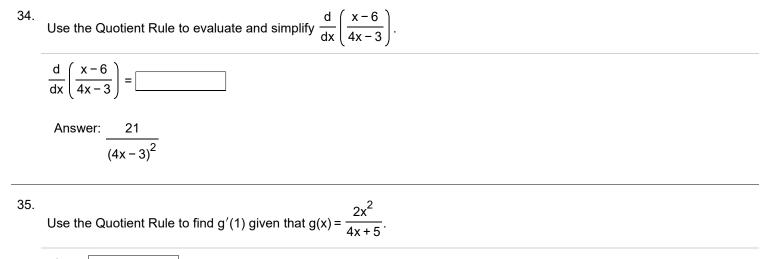
Answer: $y = -\frac{1}{11}x + \frac{9}{11}$

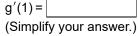
33. Evaluate the derivative of the function given below using a limit definition of the derivative.

$$f(x) = x^2 - 8x + 5$$

 $f'(x) =$

Answer: 2x - 8





Answer: 28

81

36. a. Use the Product Rule to find the derivative of the given function.b. Find the derivative by expanding the product first.

f(x) = (x - 3)(2x + 4)

a. Use the product rule to find the derivative of the function. Select the correct answer below and fill in the answer box(es) to complete your choice.

○ A. The derivative is $(x - 3)(2x + 4) + ($).
B. The derivative is $($) $x(2x + 4)$.
C. The derivative is $(x - 3)($ + $(2x + 4)($).
D. The derivative is $($) $(x-3)$.
E. The derivative is $(x - 3)(2x + 4)$.
b. Expand the product.
(x-3)(2x+4) = (Simplify your answer.)
Using either approach, $\frac{d}{dx}(x-3)(2x+4) =$
Answers C. The derivative is $(x - 3)(2) + (2x + 4)(1)$
$2x^2 - 2x - 12$
4x - 2

37. Use the quotient rule to find the derivative of the given function. Then find the derivative by first simplifying the function. Are the results the same?

$$h(w) = \frac{5w^6 - w}{w}$$

What is the immediate result of applying the quotient rule? Select the correct answer below.

• A.
$$\frac{w(30w^{5}-1) - (5w^{6}-w)(1)}{w^{2}}$$
• B.
$$(30w^{5}-1)(w) + (5w^{6}-w)(1)$$
• C.
$$5w^{5}-1$$
• D.
$$25w^{4}$$

What is the fully simplified result of applying the quotient rule?

What is the result of first simplifying the function, then taking the derivative? Select the correct answer below.

• A.
$$\frac{w(30w^5 - 1) - (5w^6 - w)(1)}{w^2}$$
• B. $5w^5 - 1$
• C. $(30w^5 - 1)(w) + (5w^6 - w)(1)$
• D. $25w^4$

Are the two results the same?

🔘 No

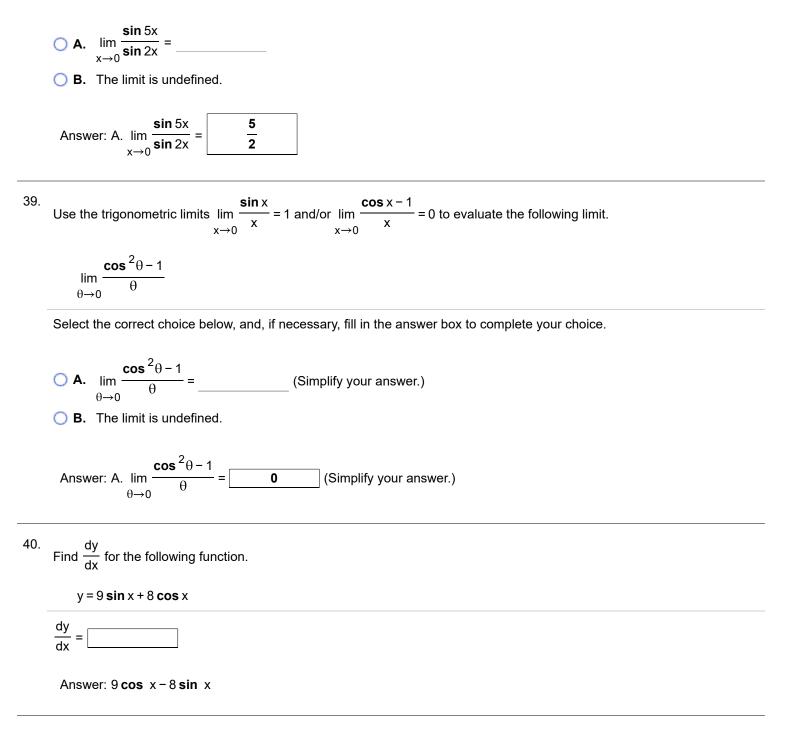
Answers
A.
$$\frac{w(30w^5 - 1) - (5w^6 - w)(1)}{w^2}$$

25w⁴
D. 25w⁴
Yes

38. Evaluate the limit.

$$\lim_{x\to 0} \frac{\sin 5x}{\sin 2x}$$

Select the correct choice below and, if necessary, fill in the answer box to complete your choice.



41. Find the derivative of the following function.

$$y = e^{-x} \sin x$$

 $\frac{dy}{dx} =$

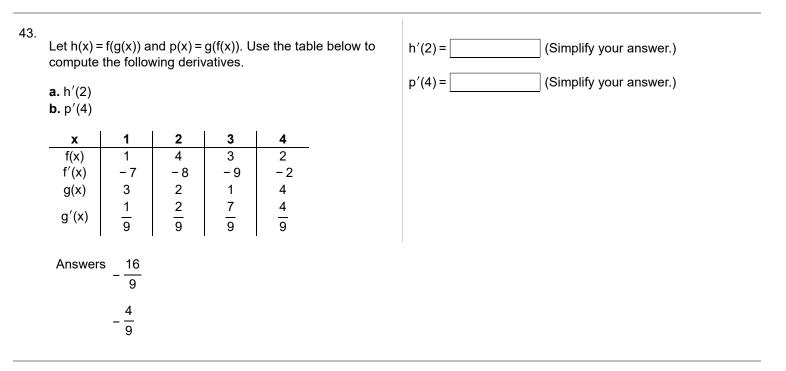
Answer: $e^{-x}(\cos x - \sin x)$

42. Find an equation of the line tangent to the following curve at the given point.

 $y = -18x^2 + 5 \sin x$; P(0,0)

The equation for the tangent line is

Answer: y = 5x



44. Calculate the derivative of the following function.

$$y = (5x + 6)^7$$

$$\frac{dy}{dx} =$$

Answer: $35(5x+6)^{6}$

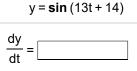
45. Calculate the derivative of the following function.

$$y = 5(2x^{4} + 9)^{-8}$$

$$\frac{dy}{dx} =$$
Answer: $-220x^{3}$

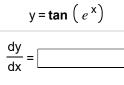
$$\frac{320x}{\left(2x^4+9\right)^9}$$

46. Calculate the derivative of the following function.



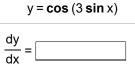
Answer: 13 **cos** (13t + 14)

47. Calculate the derivative of the following function.

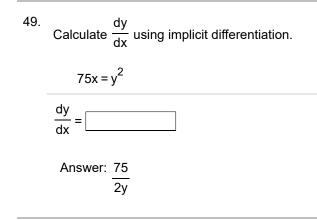


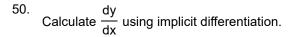
Answer: $e^{x} \sec^{2} e^{x}$

48. Calculate the derivative of the following function.



Answer: $-3 \sin (3 \sin x) \cdot \cos x$





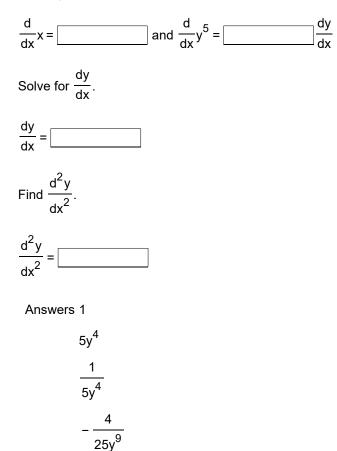
 $\frac{dy}{dx} =$

Answer: - csc y

51.

Consider the curve $x = y^5$. Use implicit differentiation to verify that $\frac{dy}{dx} = \frac{1}{5y^4}$ and then find $\frac{d^2y}{dx^2}$.

Use implicit differentiation to find the derivative of each side of the equation.



- 52. Carry out the following steps for the given curve.
 - **a.** Use implicit differentiation to find $\frac{dy}{dx}$.
 - **b.** Find the slope of the curve at the given point.

$$x^{5} + y^{5} = -275; (-3, -2)$$

a. Use implicit differentiation to find $\frac{dy}{dx}$.



b. Find the slope of the curve at the given point.

The slope of $x^5 + y^5 = -275$ at (-3, -2) is _____. (Simplify your answer.)

Answers $\frac{-x^4}{y^4}$ $-\frac{81}{16}$

53.

Use implicit differentiation to find $\frac{dy}{dx}$.

 $\cos(y) + \sin(x) = 3y$



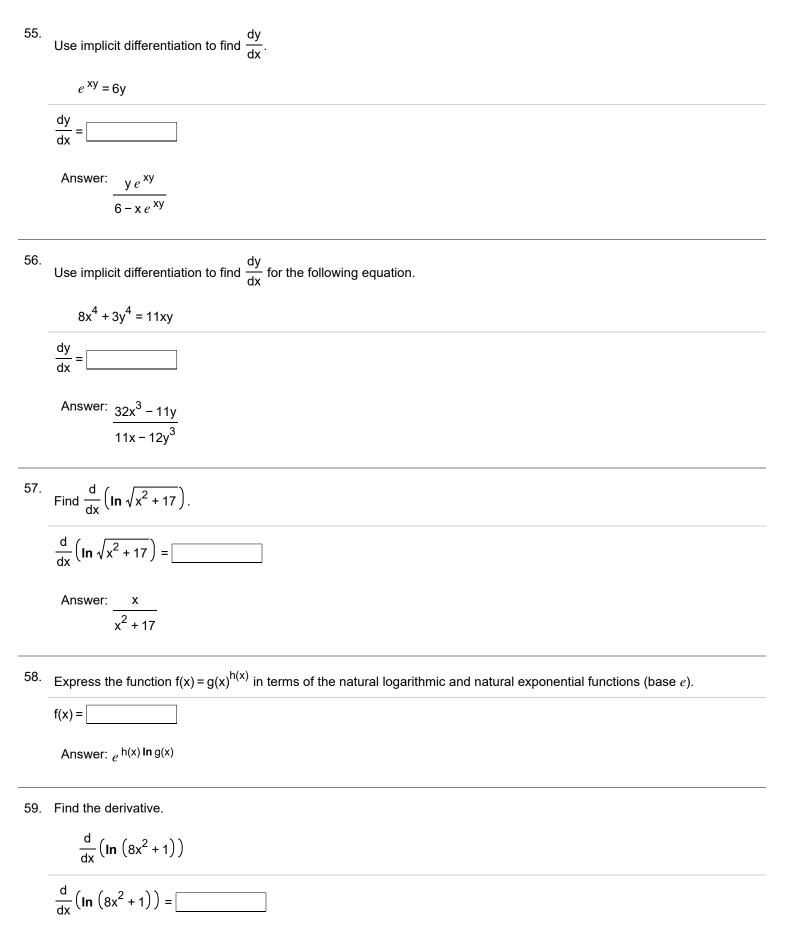
Answer: $\frac{\cos x}{3 + \sin y}$

54. Use implicit differentiation to find $\frac{dy}{dx}$.

2 **cos** (xy) = 5x + 9y

$$\frac{dy}{dx} =$$

Answer: 5 + 2y sin (xy) - 2x sin (xy) - 9



Answer: $\frac{16x}{8x^2 + 1}$

60. Evaluate the derivative.

$$y = 2x^{2\pi}$$

 $y' =$ (Type an exact answer.)
Answer: $4\pi x^{(2\pi - 1)}$

61.

Find $\frac{dy}{dx}$ for the function $y = 23^x$.

 $\frac{dy}{dx} =$

Answer: 23^x In 23

62. Calculate the derivative of the following function.

y = 4
$$\log_4 (x^2 - 3)$$

 $\frac{d}{dx} 4 \log_4 (x^2 - 3) =$

Answer: $\frac{8x}{(x^2-3) \text{ In } 4}$

63. Use logarithmic differentiation to evaluate f'(x).

$$f(x) = \frac{(x+2)^9}{(2x-2)^{11}}$$

$$f'(x) =$$
Answer:
$$\frac{(x+2)^9}{(2x-2)^{11}} \left[\frac{9}{x+2} - \frac{11}{x-1}\right]$$

^{64.} State the derivative formulas for sin ^{-1}x , tan ^{-1}x , and sec ^{-1}x .

What is the derivative of $\sin^{-1}x$?

• A.
$$\frac{1}{|x|\sqrt{x^2 - 1}}$$
 for $|x| > 1$
• B. $-\frac{1}{|x|\sqrt{x^2 - 1}}$ for $|x| > 1$
• C. $-\frac{1}{\sqrt{1 - x^2}}$ for $-1 < x < 1$
• D. $\frac{1}{\sqrt{1 - x^2}}$ for $-1 < x < 1$

What is the derivative of **tan** ^{-1}x ?

• A.
$$-\frac{1}{|x|\sqrt{x^2-1}}$$
 for $|x| > 1$
• B. $\frac{1}{1+x^2}$ for $-\infty < x < \infty$
• C. $-\frac{1}{1+x^2}$ for $-\infty < x < \infty$

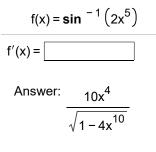
D.
$$-\frac{1}{\sqrt{1-x^2}}$$
 for $-1 < x < 1$

What is the derivative of **sec** ^{-1}x ?

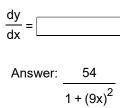
• A.
$$-\frac{1}{|x|\sqrt{x^2-1}}$$
 for $|x| > 1$
• B. $\frac{1}{\sqrt{1-x^2}}$ for $-1 < x < 1$
• C. $-\frac{1}{\sqrt{1-x^2}}$ for $-1 < x < 1$
• D. $\frac{1}{|x|\sqrt{x^2-1}}$ for $|x| > 1$

Answers D.
$$\frac{1}{\sqrt{1-x^2}}$$
 for $-1 < x < 1$
B. $\frac{1}{1+x^2}$ for $-\infty < x < \infty$
D. $\frac{1}{|x|\sqrt{x^2-1}}$ for $|x| > 1$

65. Evaluate the derivative of the function.



^{66.} Find the derivative of the function $y = 6 \tan^{-1}(9x)$.



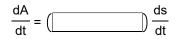
67. Evaluate the derivative of the following function.

$$f(s) = \cot^{-1} (e^{s})$$

$$\frac{d}{ds} \cot^{-1} (e^{s}) =$$
Answer:
$$-\frac{e^{s}}{1 + e^{2s}}$$

- 68. The sides of a square increase in length at a rate of 4 m/sec.
 - $\boldsymbol{a}.$ At what rate is the area of the square changing when the sides are 16 m long?
 - **b.** At what rate is the area of the square changing when the sides are 27 m long?
 - **a.** Write an equation relating the area of a square, A, and the side length of the square, s.

Differentiate both sides of the equation with respect to t.



The area of the so	uare is changing at a	ate of	(1)	when the sides are 16 m long.
b. The area of the	square is changing at	a rate of	(2)	when the sides are 27 m long.
(1) 🔿 m	(2) 🔘 m/s			
🔘 m/s	O m ² / s			
🔘 m ³ /s	🔘 m			
○ m ² /s	O m ³ /s			

Answers $A = s^2$

2s 128 (1) m² / s 216 (2) m² / s

(2)

- ^{69.} The area of a circle increases at a rate of $1 \text{ cm}^2 / \text{s}$.
 - **a.** How fast is the radius changing when the radius is 5 cm?
 - b. How fast is the radius changing when the circumference is 5 cm?
 - **a.** Write an equation relating the area of a circle, A, and the radius of the circle, r.

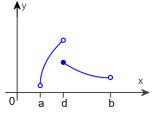
(Type an exact answer, using π as needed.)

Differentiate both sides of the equation with respect to t.

```
\frac{dA}{dt} = (
                            dr
                            dt
(Type an exact answer, using \pi as needed.)
When the radius is 5 cm, the radius is changing at a rate of
                                                                                      (1)
(Type an exact answer, using \pi as needed.)
b. When the circumference is 5 cm, the radius is changing at a rate of
(Type an exact answer, using \pi as needed.)
                        (2) \bigcirc cm<sup>3</sup>/s.
(1) O cm/s.
     🔘 cm.
                             🔘 cm.
     \bigcirc cm<sup>2</sup>/s.
                           ◯ cm<sup>2</sup>/s.
     \bigcirc cm<sup>3</sup>/s.
                              ○ cm / s.
 Answers A = \pi r^2
            2πr
              1
            10π
            (1) cm / s.
            1
            5
```

(2) cm / s.

70. Determine from the graph whether the function has any absolute extreme values on [a, b].



Where do the absolute extreme values of the function occur on [a, b]?

- \bigcirc A. The absolute maximum occurs at x = d and the absolute minimum occurs at x = a on [a, b].
- B. There is no absolute maximum and the absolute minimum occurs at x = a on [a, b].
- C. There is no absolute maximum and there is no absolute minimum on [a, b].
- \bigcirc **D.** The absolute maximum occurs at x = d and there is no absolute minimum on [a, b].

Answer: C. There is no absolute maximum and there is no absolute minimum on [a, b].

71. Find the critical points of the following function.

$$f(x) = 4x^2 - 5x + 1$$

What is the derivative of $f(x) = 4x^2 - 5x + 1$?

f'(x) =

Find the critical points, if any, of f on the domain. Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

5

A. The critical point(s) occur(s) at x = _____.
 (Use a comma to separate answers as needed.)

B. There are no critical points for $f(x) = 4x^2 - 5x + 1$ on the domain.

Answers 8x - 5

A. The critical point(s) occur(s) at x =

(Use a comma to separate answers as needed.)

72. Find the critical points of the following function.

$$f(x) = -\frac{x^3}{3} + 100x$$

Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

 A. The critical point(s) occur(s) at x = (Use a comma to separate answers as needed.)

O B. There are no critical points.

Answer: A. The critical point(s) occur(s) at x = 10, -10. (Use a comma to separate answers as needed.)

73. Determine the location and value of the absolute extreme values of f on the given interval, if they exist.

 $f(x) = x^2 - 5$ on [-2,4]

What is/are the absolute maximum/maxima of f on the given interval? Select the correct choice below and, if necessary, fill in the answer boxes to complete your choice.

- A. The absolute maximum/maxima is/are ________ at x = ______. (Use a comma to separate answers as needed.)
- **B.** There is no absolute maximum of f on the given interval.

What is/are the absolute minimum/minima of f on the given interval? Select the correct choice below and, if necessary, fill in the answer boxes to complete your choice.

- **B.** There is no absolute minimum of f on the given interval.

Answers A. The absolute maximum/maxima is/are **11** at x = **4** (Use a comma to separate answers as needed.) A. The absolute minimum/minima is/are **-5** at x = **0**.

- (Use a comma to separate answers as needed.)
- 74. A stone is launched vertically upward from a cliff 112 ft above the ground at a speed of 96 ft / s. Its height above the ground t seconds after the launch is given by $s = -16t^2 + 96t + 112$ for $0 \le t \le 7$. When does the stone reach its maximum height?

Find the derivative of s.	
s' =	
The stone reaches its maximum height at (Simplify your answer.)	S.
Answers - 32t + 96	
3	

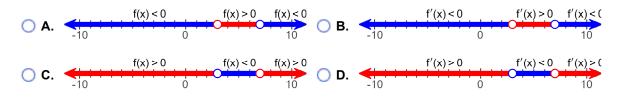
- 75. Suppose a tour guide has a bus that holds a maximum of 88 people. Assume his profit (in dollars) for taking n people on a city tour is P(n) = n(44 0.5n) 88. (Although P is defined only for positive integers, treat it as a continuous function.)
 - a. How many people should the guide take on a tour to maximize the profit?
 - b. Suppose the bus holds a maximum of 38 people. How many people should be taken on a tour to maximize the profit?

	a. Find the derivative of the given function P(n).					
	P'(n) =					
	If the bus holds a maximum of 88 people, the guide should take people on a tour to maximize the profit.					
	b. If the bus holds a maximum of 38 people, the guide should take people on a tour to maximize the profit.					
	Answers - n + 44					
	44					
	38					
76.	At what points c does the conclusion of the Mean Value Theorem hold for $f(x) = x^3$ on the interval [-20,20]?					
	The conclusion of the Mean Value Theorem holds for c = (Use a comma to separate answers as needed. Type an exact answer, using radicals as needed.)					
	Answer: $20\sqrt{3}$ $20\sqrt{3}$					
	Answer: $\frac{20\sqrt{3}}{3}$, $-\frac{20\sqrt{3}}{3}$					
77.	a. Determine whether the Mean Value Theorem applies to the function $f(x) = 3 - x^2$ on the interval [-2,1]. b. If so, find the point(s) that are guaranteed to exist by the Mean Value Theorem.					
	a. Choose the correct answer below.					
	○ A. No, because the function is continuous on the interval [-2,1], but is not differentiable on the interval (-2,1).					
	O B. Yes, because the function is continuous on the interval [−2,1] and differentiable on the interval (−2,1).					
	○ C. No, because the function is not continuous on the interval [-2,1], and is not differentiable on the interval (-2,1).					
	D. No, because the function is differentiable on the interval (-2,1), but is not continuous on the interval [-2,1].					
	b. Select the correct choice below and, if necessary, fill in the answer box to complete your choice.					
	\bigcirc A. The point(s) is/are x = .					
	(Simplify your answer. Use a comma to separate answers as needed.)					
	◯ B. The Mean Value Theorem does not apply in this case.					
	Answers B. Yes, because the function is continuous on the interval [$-2,1$] and differentiable on the interval ($-2,1$).					
	A. The point(s) is/are x = $-\frac{1}{2}$.					
	(Simplify your answer. Use a comma to separate answers as needed.)					

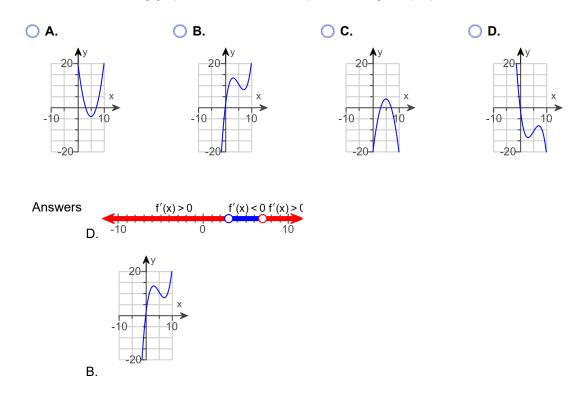
Sketch a function that is continuous on (−∞,∞) and has the following properties. Use a number line to summarize information about the function.

f'(x) > 0 on $(-\infty,3)$; f'(x) < 0 on (3,7); f'(x) > 0 on $(7,\infty)$.

Which number line summarizes the information about the function?



Which of the following graphs matches the description of the given properties?



79. Find the intervals on which f is increasing and the intervals on which it is decreasing.

 $f(x) = -2 + x^2$

Select the correct choice below and, if necessary, fill in the answer box(es) to complete your choice.

- A. The function is increasing on ______ and decreasing on ______.
 (Simplify your answers. Type your answers in interval notation. Use a comma to separate answers as needed.)
- B. The function is increasing on ______. The function is never decreasing. (Simplify your answer. Type your answer in interval notation. Use a comma to separate answers as needed.)
- C. The function is decreasing on ______. The function is never increasing. (Simplify your answer. Type your answer in interval notation. Use a comma to separate answers as needed.)
- D. The function is never increasing nor decreasing.

Answer: A. The function is increasing on $(0,\infty)$ and decreasing on $(-\infty,0)$. (Simplify your answers. Type your answers in interval notation. Use a comma to separate answers as needed.)

80. Find the intervals on which f is increasing and the intervals on which it is decreasing.

$$f(x) = -10 - x + 2x^2$$

Select the correct choice below and, if necessary, fill in the answer box(es) to complete your choice.

- A. The function is increasing on ______ and decreasing on ______.
 (Simplify your answers. Type your answers in interval notation. Use a comma to separate answers as needed.)
- B. The function is increasing on ______. The function is never decreasing. (Simplify your answer. Type your answer in interval notation. Use a comma to separate answers as needed.)
- C. The function is decreasing on ______. The function is never increasing. (Simplify your answer. Type your answer in interval notation. Use a comma to separate answers as needed.)
- **D.** The function is never increasing nor decreasing.

Answer: A. The function is increasing on



and decreasing on



(Simplify your answers. Type your answers in interval notation. Use a comma to separate answers as needed.)

81. Locate the critical points of the following function. Then use the Second Derivative Test to determine whether they correspond to local maxima, local minima, or neither.

 $f(x) = 5 + x^2$

What is(are) the critical point(s) of f? Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

- A. The critical point(s) is(are) x = _____.
 (Use a comma to separate answers as needed. Type an integer or a simplified fraction.)
- **B.** There are no critical points for f.

What is/are the local minimum/minima of f? Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

- A. The local minimum/minima of f is/are at x = _____.
 (Use a comma to separate answers as needed. Type an integer or a simplified fraction.)
- O B. There is no local minimum of f.

What is/are the local maximum/maxima of f? Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

- A. The local maximum/maxima of f is/are at x =______. (Use a comma to separate answers as needed. Type an integer or a simplified fraction.)
- **B.** There is no local maximum of f.

Answers A. The critical point(s) is(are) x = 0.
(Use a comma to separate answers as needed. Type an integer or a simplified fraction.)
A. The local minimum/minima of f is/are at x = 0.
(Use a comma to separate answers as needed. Type an integer or a simplified fraction.)
B. There is no local maximum of f.

82. Locate the critical points of the following function. Then use the Second Derivative Test to determine whether they correspond to local maxima, local minima, or neither.

 $f(x) = x^3 + 12x^2 + 5$

What is(are) the critical point(s) of f? Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

- A. The critical point(s) is(are) x = _____.
 (Use a comma to separate answers as needed. Type an integer or a simplified fraction.)
- **B.** There are no critical points for f.

What is/are the local minimum/minima of f? Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

- A. The local minimum/minima of f is/are at x = _____.
 (Use a comma to separate answers as needed. Type an integer or a simplified fraction.)
- O B. There is no local minimum of f.

What is/are the local maximum/maxima of f? Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

- A. The local maximum/maxima of f is/are at x = _____.
 (Use a comma to separate answers as needed. Type an integer or a simplified fraction.)
- **B.** There is no local maximum of f.

Answers A. The critical point(s) is(are) x = 0, −8 . (Use a comma to separate answers as needed. Type an integer or a simplified fraction.)
A. The local minimum/minima of f is/are at x = 0 . (Use a comma to separate answers as needed. Type an integer or a simplified fraction.)
A. The local maximum/maxima of f is/are at $x = -8$. (Use a comma to separate answers as needed. Type an integer or a simplified fraction.)

83. **a.** Squares with sides of length x are cut out of each corner of a rectangular piece of cardboard measuring 7 ft by 5 ft. The resulting piece of cardboard is then folded into a box without a lid. Find the volume of the largest box that can be formed in this way.

b. Suppose that in part (a) the original piece of cardboard is a square with sides of length s. Find the volume of the largest box that can be formed in this way.

a. To find the objective function, express the volume V of the box in terms of x.

V = ______ (Type an expression.)

The interval of interest of the objective function is _____.

(Simplify your answer. Type your answer in interval notation. Use integers or decimals for any numbers in the expression.)

The maximum volume of the box is approximately ft^3 . (Round to the nearest hundredth as needed.)

b. To find the objective function, express the volume V of the box in terms of s and x.

V = _____ (Type an expression.)

The maximum volume of the box is

(Type an expression using s as the variable.)

Answers x(7 – 2x)(5 – 2x) [0,2.5] 15.02

 $\frac{x(s-2x)(s-2x)}{\frac{2s^3}{27}}$

84. Use a linear approximation to estimate the following quantity. Choose a value of a to produce a small error.

In (1.05)

What is the value found using the linear approximation?

In $(1.05) \approx$ (Round to two decimal places as needed.)

Answer: 0.05

85. Consider the following function and express the relationship between a small change in x and the corresponding change in y in the form dy = f'(x)dx.

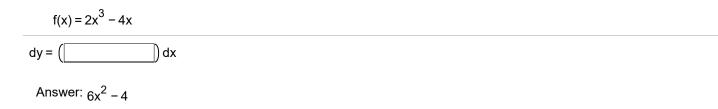
 $f(x) = e^{20x}$

dy = (

) dx (Type an exact answer in terms of *e*.)

Answer: 20 e 20x

86. Consider the following function and express the relationship between a small change in x and the corresponding change in y in the form dy = f'(x)dx.



87. Consider the following function and express the relationship between a small change in x and the corresponding change in y in the form dy = f'(x) dx.

 $f(x) = \cot 4x$ $dy = \boxed{\qquad} dx$

Answer: $-4 \csc^2(4x)$

88. Evaluate the following limit. Use l'Hôpital's Rule when it is convenient and applicable.

$$\lim_{x \to 0} \frac{7 \sin 9x}{5x}$$

5

Use l'Hôpital's Rule to rewrite the given limit so that it is not an indeterminate form.

$$\lim_{x \to 0} \frac{7 \sin 9x}{5x} = \lim_{x \to 0} ($$

Evaluate the limit.
$$\lim_{x \to 0} \frac{7 \sin 9x}{5x} =$$
(Type an exact answer.)
Answers $\frac{63 \cos (9x)}{5}$

89. Evaluate the following limit. Use l'Hôpital's Rule when it is convenient and applicable.

$$\lim_{u \to \frac{\pi}{4}} \frac{\tan u - \cot u}{u - \frac{\pi}{4}}$$

Use I'Hôpital's Rule to rewrite the given limit so that it is not an indeterminate form.

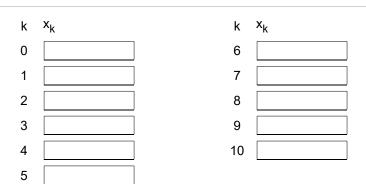
$$\lim_{u \to \frac{\pi}{4}} \frac{\tan u - \cot u}{u - \frac{\pi}{4}} = \lim_{u \to \frac{\pi}{4}} ($$

Evaluate the limit.

$$\lim_{u \to \frac{\pi}{4}} \frac{\tan u - \cot u}{u - \frac{\pi}{4}} =$$
 (Type an exact answer.)

Answers $\sec^2 u + \csc^2 u$ 4 90. Use a calculator or program to compute the first 10 iterations of Newton's method when they are applied to the following function with the given initial approximation.

 $f(x) = x^2 - 24; x_0 = 5$



(Round to six decimal places as needed.)

Answers 5.000000

4.898979

- 4.900000
- 4.898979
- 4.898980
- 4.898979
- 4.898979
- 4.898979
- 4.898979
- 4.898979
- 4.898979

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91. Use a calculator or program to compute the first 10 iterations of Newton's method for the given function and initial approximation.

 $f(x) = 5 \sin x - 3x + 1, x_0 = 1.4$

Complete the table.

(Do not round until the final answer. Then round to six decimal places as needed.)

k	x _k	k	x _k
1		6	
2		7	
3		8	
4		9	
5		10	

Answers 2.203310

1.906800 1.938494

1.906800

1.907290

1.906800

1.906800

1.906800

1.906800

1.906800

92. Determine the following indefinite integral. Check your work by differentiation.

$$\int (5x^9 - 3x^5) dx$$

$$\int (5x^9 - 3x^5) dx =$$
(Use C as the arbitrary constant.)

Answer: $\frac{x^{10}}{2} - \frac{x^6}{2} + C$

93. Evaluate the following indefinite integral.

$$\int \left(\frac{12}{\sqrt{x}} + 12\sqrt{x}\right) dx$$

$$\int \left(\frac{12}{\sqrt{x}} + 12\sqrt{x}\right) dx =$$

(Use C as the arbitrary constant.)

Answer:
$$\frac{3}{24\sqrt{x}+8x^2}$$
 + C

94. Determine the following indefinite integral.

$$\int \left(\frac{2}{s^2} - 9s^4\right) ds$$
$$\int \left(\frac{2}{s^2} - 9s^4\right) ds =$$

(Use C as the arbitrary constant.)

Answer:
$$-2s^{-1} - \frac{9}{5}s^5 + C$$

95.

^

Find $\int (6x+5)^2 dx$.

$$\int (6x+5)^2 dx =$$

(Use C as the arbitrary constant.)

Answer: $12x^3 + 30x^2 + 25x + C$

96. Determine the following indefinite integral. Check your work by differentiation.

$$\int 4m \left(8m^2 - 5m\right) dm$$

$$\int 4m \left(8m^2 - 5m\right) dm =$$
(Use C as the arbitrary constant.)
Answer:
$$8m^4 - \frac{20m^3}{3} + C$$

97. Determine the following indefinite integral. Check your work by differentiation.

$$\int \left(2x^{\frac{2}{3}} + 4x^{-\frac{1}{3}} + 7 \right) dx$$

$$\int \left(2x^{\frac{2}{3}} + 4x^{-\frac{1}{3}} + 7 \right) dx =$$
(Use C as the arbitrary constant.)
Answer: $\frac{6}{5}x^{\frac{5}{3}} + 6x^{\frac{2}{3}} + 7x + C$

98. Determine the following indefinite integral. Check your work by differentiation.

$$\int 4\sqrt[9]{x} dx$$

$$\int 4\sqrt[9]{x} dx =$$
(Use C as the arbitrary constant.)
Answer: $\frac{18}{5}x^{\frac{10}{9}} + C$

99. Determine the following indefinite integral. Check your work by differentiation.

$$\int (9x+1)(7-x) dx$$

$$\int (9x+1)(7-x) dx =$$
(Use C as the arbitrary constant.)

Answer:
$$-3x^3 + 31x^2 + 7x + C$$

100. Determine the following indefinite integral. Check your work by differentiation.

$$\int \left(\frac{8}{x^4} + 2 - \frac{8}{x^2}\right) dx$$

$$\int \left(\frac{8}{x^4} + 2 - \frac{8}{x^2}\right) dx =$$

(Use C as the arbitrary constant.)

Answer:
$$-\frac{8}{3x^3} + 2x + \frac{8}{x} + C$$

101. Determine the following indefinite integral.

$$\int \frac{4x^4 + 15x^3}{x} \, dx$$

$$\int \frac{4x^4 + 15x^3}{x} dx =$$
(Use C as the arbitrary constant.)

Answer:
$$x^4 + 5x^3 + C$$

102. For the following function f, find the antiderivative F that satisfies the given condition.

$$f(x) = 6x^3 + 9 \sin x$$
, $F(0) = 4$

The antiderivative that satisfies the given condition is F(x) =

Answer: $\frac{3}{2}x^4 - 9\cos x + 13$

103. For the following function f, find the antiderivative F that satisfies the given condition.

 $f(u) = 6 e^{u} + 10; F(0) = -6$

The antiderivative that satisfies the given condition is F(u) =

Answer: 6 e^u + 10u - 12

104. Find the solution of the following initial value problems.

f'(x) = 4x - 7; f(0) = 8

The solution to the initial value problem is f(x) =

Answer: $2x^2 - 7x + 8$

105. Given the following velocity function of an object moving along a line, find the position function with the given initial position.

v(t) = 4t + 5; s(0) = 0

The position function is s(t) =

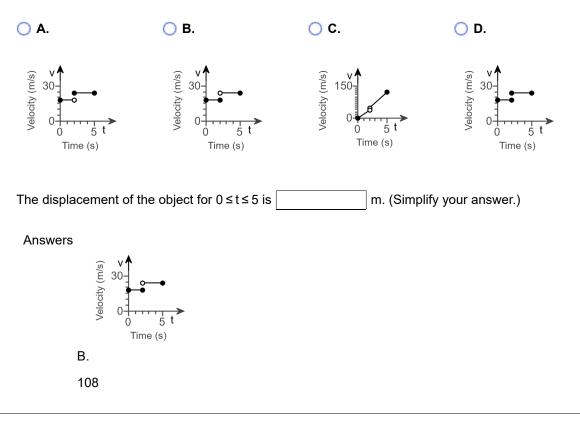
Answer: 2t² + 5t

106. Given the following velocity function of an object moving along a line, find the position function with the given initial position.

 $v(t) = 9t^{2} + 2t - 7$; s(0) = 0The position function is s(t) =______. Answer: $3t^{3} + t^{2} - 7t$

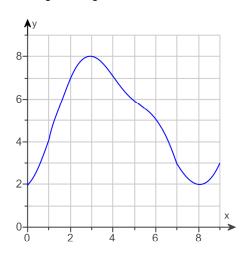
107. Suppose an object moves along a line at 18 m/s for $0 \le t \le 2$ s and at 24 m/s for $2 < t \le 5$ s. Sketch the graph of the velocity function and find the displacement of the object for $0 \le t \le 5$.

Sketch the graph of the velocity function. Choose the correct graph below.

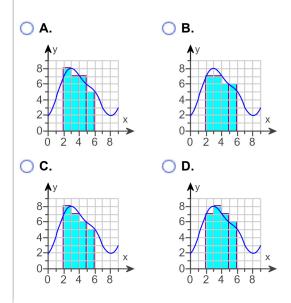


108.

Approximate the area of the region bounded by the graph of f(x) (shown below) and the x-axis by dividing the interval [0,4] into n = 4 subintervals. Use a right and left Riemann sum to obtain two different approximations. Draw the approximating rectangles.



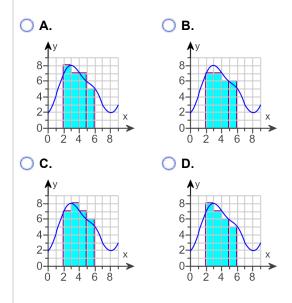
In which graph below are the selected points the right endpoints of the 4 approximating rectangles?



Using the specified rectangles, approximate the area.

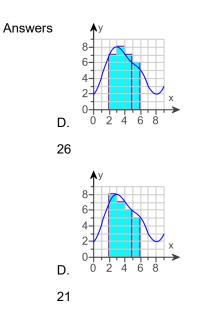


In which graph below are the selected points the left endpoints of the 4 approximating rectangles?

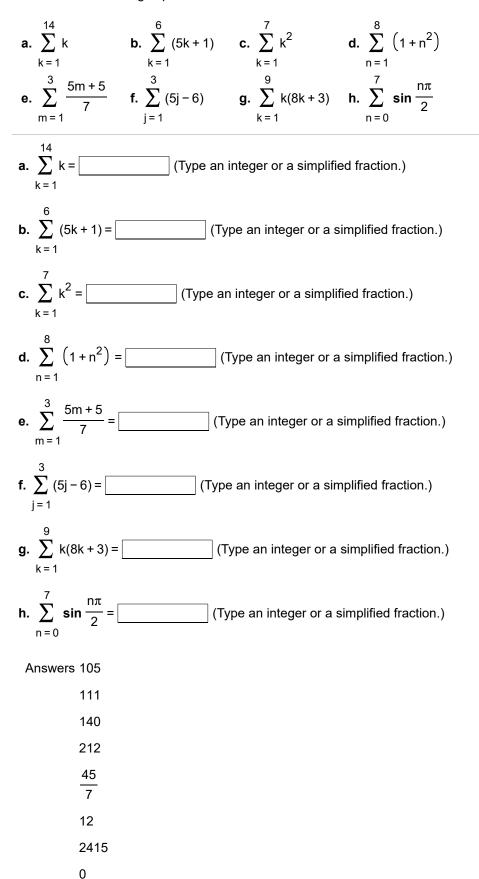


Using the specified rectangles, approximate the area.



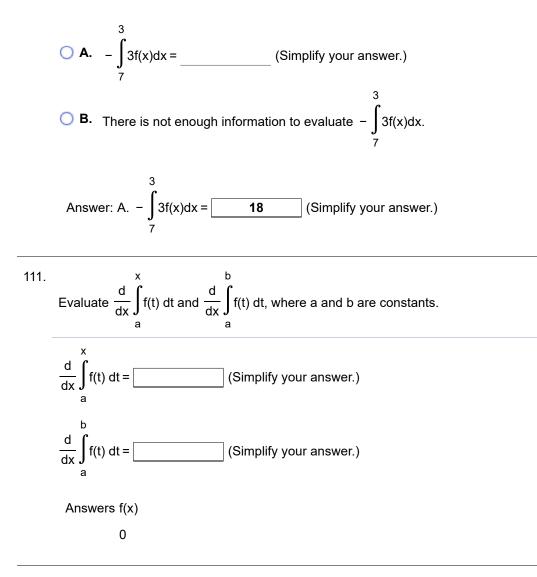


109. Evaluate the following expressions.



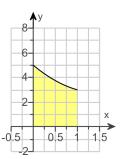
110.
The functions f and g are integrable and
$$\int_{3}^{7} f(x)dx = 6$$
, $\int_{3}^{7} g(x)dx = 4$, and $\int_{5}^{7} f(x)dx = 3$. Evaluate the integral below or state that there is not enough information.
 $-\int_{7}^{3} 3f(x)dx$

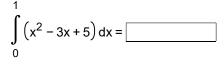
Select the correct choice below and, if necessary, fill in the answer box to complete your choice.



112. Evaluate the following integral using the Fundamental Theorem of Calculus. Discuss whether your result is consistent with the figure.

$$\int_{0}^{1} \left(x^2 - 3x + 5\right) dx$$





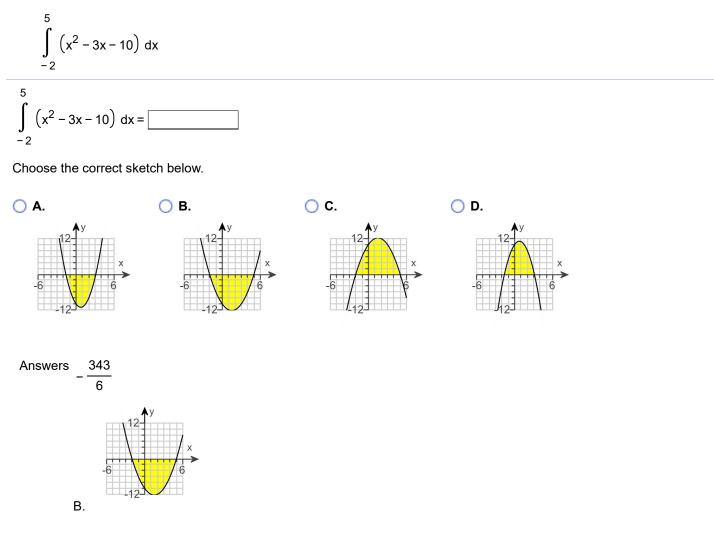
Is your result consistent with the figure?

- A. Yes, because the definite integral is positive and the graph of f lies above the x-axis.
- O B. Yes, because the definite integral is negative and the graph of f lies below the x-axis.
- C. No, because the definite integral is positive and the graph of f lies below the x-axis.
- D. No, because the definite integral is negative and the graph of f lies above the x-axis.

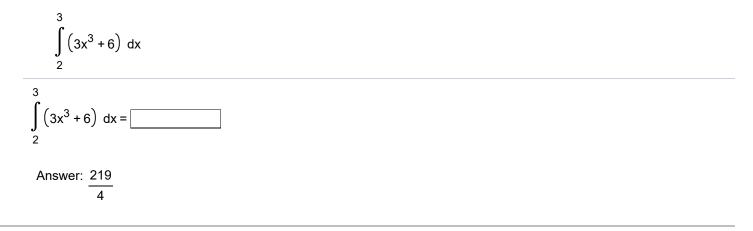
Answers $\frac{23}{6}$

A. Yes, because the definite integral is positive and the graph of f lies above the x-axis.

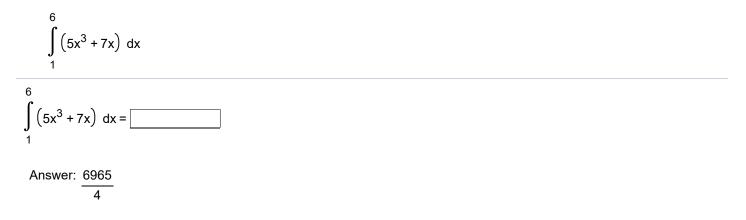
113. Evaluate the following integral using the fundamental theorem of calculus. Sketch the graph of the integrand and shade the region whose net area you have found.



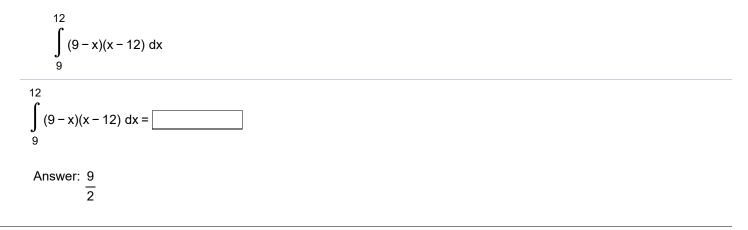
114. Use the fundamental theorem of calculus to evaluate the following definite integral.



115. Evaluate the following integral using the Fundamental Theorem of Calculus.

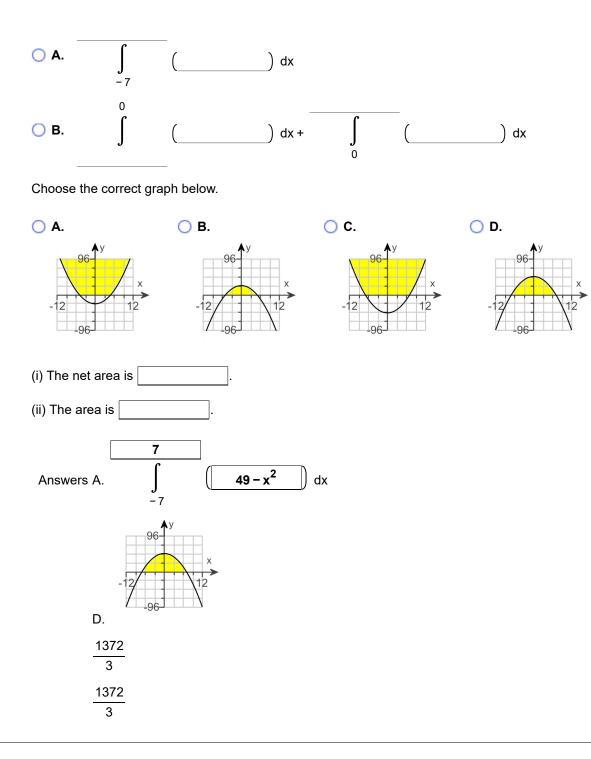


116. Evaluate the following integral using the Fundamental Theorem of Calculus.



^{117.} Find (i) the net area and (ii) the area of the region above the x-axis bounded by $y = 49 - x^2$. Graph the function and indicate the region in question.

Set up the integral (or integrals) needed to compute this area. Select the correct choice below and fill in the answer boxes to complete your answer.



118. Find the area of the region bounded by the graph of f and the x-axis on the given interval.

$$f(x) = x^2 - 25; [1,4]$$

The area is _____. (Type an integer or a simplified fraction.)

Answer: 54

119. Simplify the following expression.

$$\frac{d}{dx}\int_{2}^{x} (2t^{2}+t+8) dt$$
$$\frac{d}{dx}\int_{2}^{x} (2t^{2}+t+8) dt =$$

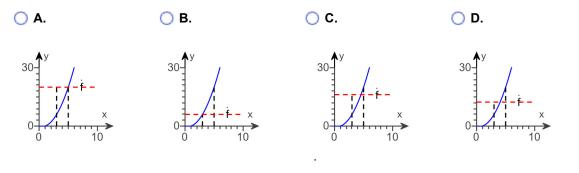
Answer: $2x^2 + x + 8$

120. Find the average value of the following function over the given interval. Draw a graph of the function and indicate the average value.

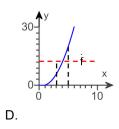
f(x) = x(x - 1); [3,5]

The average value of the function is f =

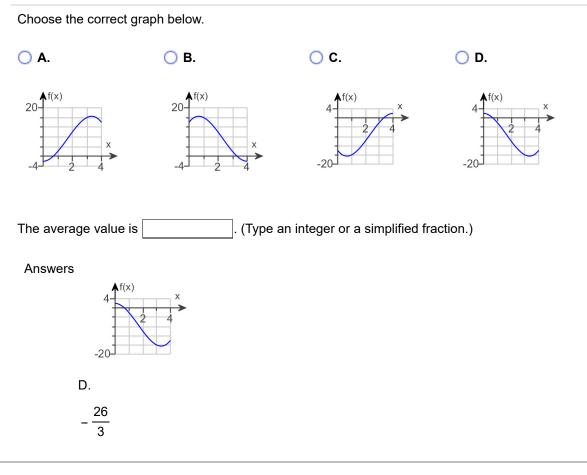
Choose the correct graph of f(x) and \overline{f} below.



Answers 37



121. The elevation of a path is given by $f(x) = x^3 - 5x^2 + 2$, where x measures horizontal distances. Draw a graph of the elevation function and find its average value for $0 \le x \le 4$.



122. Find the point(s) at which the function f(x) = 7 - 6x equals its average value on the interval [0,8].

The function equals its average value at $x =$	
(Use a comma to separate answers as need	led.)

Answer: 4

^{123.} Use the substitution $u = x^2 + 11$ to find the following indefinite integral. Check your answer by differentiation.

 $\int 2x(x^2+11)^4 dx$ $\int 2x(x^2+11)^4 dx = [$

(Use C as the arbitrary constant.)

Answer:
$$\frac{1}{5}(x^2 + 11)^5 + C$$

^{124.} Use the substitution $u = 7x^2 - 3$ to find the following indefinite integral. Check your answer by differentiation.

$$\int -14x \sin (7x^2 - 3) dx$$
$$\int -14x \sin (7x^2 - 3) dx =$$
(Use C as the arbitrary constant.)

Answer: $\cos(7x^2 - 3) + C$

^{125.} Use the substitution $u = 2x^2 + 4x$ to evaluate the indefinite integral below.

$$\int (4x+4)\sqrt{2x^2+4x} \, dx$$

Write the integrand in terms of u.

$$\int (4x+4)\sqrt{2x^2+4x} \, dx = \int ($$

Evaluate the integral.

$$\int (4x+4)\sqrt{2x^2+4x} \, dx =$$
(Use C as the arbitrary constant.)

Answers \sqrt{u}

$$\frac{2}{3}(2x^2+4x)^{\frac{3}{2}}+C$$

126. Find an antiderivative of the following function by trial and error. Check your answer by differentiation.

$$e^{9x-4}$$

$$\int e^{9x-4} dx =$$
(Use C as the arbitrary constant.)
Answer: $\frac{1}{9}e^{9x-4} + C$

$$\int x^{10} e^{x^{11}} dx$$

¹ Click the icon to view the table of general integration formulas.

 $\int x^{10} e^{x^{11}} dx =$ (Use C as the arbitrary constant.)

1: General Integration Formulas

$$\int \cos ax \, dx = \frac{1}{a} \sin ax + C$$

$$\int \sin ax \, dx = -\frac{1}{a} \cos ax + C$$

$$\int \sec^2 ax \, dx = \frac{1}{a} \tan ax + C$$

$$\int \csc^2 ax \, dx = -\frac{1}{a} \cot ax + C$$

$$\int \sec ax \tan ax \, dx = \frac{1}{a} \sec ax + C$$

$$\int \csc ax \cot ax \, dx = -\frac{1}{a} \csc ax + C$$

$$\int csc ax \cot ax \, dx = -\frac{1}{a} \csc ax + C$$

$$\int b^x dx = \frac{1}{a} b^x + C, b > 0, b \neq 1$$

$$\int \frac{dx}{a^2 + x^2} = \frac{1}{a} \tan^{-1} \frac{x}{a} + C$$

$$\int \frac{dx}{\sqrt{a^2 - x^2}} = \sin^{-1} \frac{x}{a} + C, a > 0$$

$$\int \frac{dx}{\sqrt{x^2 - a^2}} = \frac{1}{a} \sec^{-1} \left| \frac{x}{a} \right| + C, a > 0$$

Answer: $\frac{1}{11} e^{x^{11}} + C$

$$\int (x^5 + x^2)^{15} (5x^4 + 2x) dx$$

 2 Click the icon to view the table of general integration formulas.

$$\int (x^5 + x^2)^{15} (5x^4 + 2x) dx =$$
 (Use C as the arbitrary constant.)

2: General Integration Formulas

$$\int \cos ax \, dx = \frac{1}{a} \sin ax + C$$

$$\int \sin ax \, dx = -\frac{1}{a} \cos ax + C$$

$$\int \sec^2 ax \, dx = \frac{1}{a} \tan ax + C$$

$$\int \csc^2 ax \, dx = -\frac{1}{a} \cot ax + C$$

$$\int \sec ax \tan ax \, dx = \frac{1}{a} \sec ax + C$$

$$\int \csc ax \cot ax \, dx = -\frac{1}{a} \csc ax + C$$

$$\int e^{ax} dx = \frac{1}{a} e^{ax} + C$$

$$\int b^x dx = \frac{1}{\ln b} b^x + C, \quad b > 0, \quad b \neq 1$$

$$\int \frac{dx}{a^2 + x^2} = \frac{1}{a} \tan^{-1} \frac{x}{a} + C$$

$$\int \frac{dx}{\sqrt{a^2 - x^2}} = \sin^{-1} \frac{x}{a} + C, \quad a > 0$$

$$\int \frac{dx}{x\sqrt{x^2 - a^2}} = \frac{1}{a} \sec^{-1} \left| \frac{x}{a} \right| + C, \quad a > 0$$
Answer:
$$\frac{(x^5 + x^2)^{16}}{16} + C$$

$$\int \frac{e^{2x}}{e^{2x}+2} \, \mathrm{d}x$$

³ Click the icon to view the table of general integration formulas.

Determine a change of variables from x to u. Choose the correct answer below.

• A.
$$u = \frac{1}{e^{2x} + 2}$$

• B. $u = e^{2x}$
• C. $u = 2x$

$$\bigcirc$$
 D. $u = e^{2x} + 2$

Write the integral in terms of u.

$$\int \frac{e^{2x}}{e^{2x}+2} \, \mathrm{d}x = \int (\boxed{ \qquad } \mathrm{d}u$$

Evaluate the integral.

$$\int \frac{e^{2x}}{e^{2x}+2} \, \mathrm{d}x =$$

(Use C as the arbitrary constant.)

3: General Integration Formulas

$$\int \cos ax \, dx = \frac{1}{a} \sin ax + C \qquad \int \sin ax \, dx = -\frac{1}{a} \cos ax + C$$

$$\int \sec^2 ax \, dx = \frac{1}{a} \tan ax + C \qquad \int \csc^2 ax \, dx = -\frac{1}{a} \cot ax + C$$

$$\int \sec ax \tan ax \, dx = \frac{1}{a} \sec ax + C \qquad \int \csc ax \cot ax \, dx = -\frac{1}{a} \csc ax + C$$

$$\int e^{ax} dx = \frac{1}{a} e^{ax} + C \qquad \int b^x dx = \frac{1}{\ln b} b^x + C, \ b > 0, \ b \neq 1$$

$$\int \frac{dx}{a^2 + x^2} = \frac{1}{a} \tan^{-1} \frac{x}{a} + C \qquad \int \frac{dx}{\sqrt{a^2 - x^2}} = \sin^{-1} \frac{x}{a} + C, \ a > 0$$

$$\int \frac{dx}{x\sqrt{x^2 - a^2}} = \frac{1}{a} \sec^{-1} \left| \frac{x}{a} \right| + C, \ a > 0$$

Answers D. u = e^{2x} + 2

$$\frac{1}{2u}$$
$$\frac{1}{2}\ln \left|e^{2x}+2\right|+C$$

 $\int_{0}^{\pi/30} \cos 5x \, dx$

⁴ Click to view the table of general integration formulas.

 $\int_{0} \cos 5x \, dx =$ (Type an exact answer.)

4: General Integration Formulas

$$\int \cos ax \, dx = \frac{1}{a} \sin ax + C$$

$$\int \sin ax \, dx = -\frac{1}{a} \cos ax + C$$

$$\int \sec^2 ax \, dx = \frac{1}{a} \tan ax + C$$

$$\int \csc^2 ax \, dx = -\frac{1}{a} \cot ax + C$$

$$\int \sec ax \tan ax \, dx = \frac{1}{a} \sec ax + C$$

$$\int \csc ax \ \cot ax \, dx = -\frac{1}{a} \csc ax + C$$

$$\int csc \ ax \ \cot ax \ dx = -\frac{1}{a} \csc ax + C$$

$$\int b^x dx = \frac{1}{a} b^x + C, \ b > 0, \ b \neq 1$$

$$\int \frac{dx}{a^2 + x^2} = \frac{1}{a} \tan^{-1} \frac{x}{a} + C$$

$$\int \frac{dx}{\sqrt{a^2 - x^2}} = \sin^{-1} \frac{x}{a} + C, \ a > 0$$

Answer: 1 10

$$\int_{0}^{3} 4e^{2x} dx$$

⁵ Click to view the table of general integration formulas.

$$\int_{0}^{3} 4e^{2x} dx =$$
 (Type an exact answer.)

5: General Integration Formulas

$$\int \cos ax \, dx = \frac{1}{a} \sin ax + C$$

$$\int \sin ax \, dx = -\frac{1}{a} \cos ax + C$$

$$\int \sec^2 ax \, dx = \frac{1}{a} \tan ax + C$$

$$\int \csc^2 ax \, dx = -\frac{1}{a} \cot ax + C$$

$$\int \sec ax \tan ax \, dx = \frac{1}{a} \sec ax + C$$

$$\int \csc ax \ \cot ax \, dx = -\frac{1}{a} \csc ax + C$$

$$\int \csc ax \ \cot ax \, dx = -\frac{1}{a} \csc ax + C$$

$$\int e^{ax} dx = \frac{1}{a} e^{ax} + C$$

$$\int b^x dx = \frac{1}{\ln b} b^x + C, \ b > 0, \ b \neq 1$$

$$\int \frac{dx}{a^2 + x^2} = \frac{1}{a} \tan^{-1} \frac{x}{a} + C$$

$$\int \frac{dx}{\sqrt{a^2 - x^2}} = \sin^{-1} \frac{x}{a} + C, \ a > 0$$

Answer: $2e^{6} - 2$

$$\int_{0}^{1} 7x^{6} \left(8 - x^{7}\right) dx$$

 $^{\rm 6}$ Click to view the table of general integration formulas.

$$\int_{0}^{1} 7x^{6} (8 - x^{7}) dx =$$
 (Type an exact answer.)

6: General Integration Formulas

Answer: 15

2

$$\int \cos ax \, dx = \frac{1}{a} \sin ax + C$$

$$\int \sin ax \, dx = -\frac{1}{a} \cos ax + C$$

$$\int \sec^2 ax \, dx = \frac{1}{a} \tan ax + C$$

$$\int \sec^2 ax \, dx = \frac{1}{a} \tan ax + C$$

$$\int \csc^2 ax \, dx = -\frac{1}{a} \cot ax + C$$

$$\int \sec ax \tan ax \, dx = \frac{1}{a} \sec ax + C$$

$$\int \csc ax \cot ax \, dx = -\frac{1}{a} \csc ax + C$$

$$\int e^{ax} dx = \frac{1}{a} e^{ax} + C$$

$$\int b^x dx = \frac{1}{ab} b^x + C, \quad b > 0, \quad b \neq 1$$

$$\int \frac{dx}{a^2 + x^2} = \frac{1}{a} \tan^{-1} \frac{x}{a} + C$$

$$\int \frac{dx}{\sqrt{a^2 - x^2}} = \sin^{-1} \frac{x}{a} + C, \quad a > 0$$

$$\int_{0}^{1} \frac{2x}{\left(x^{2}+1\right)^{3}} \, \mathrm{d}x$$

⁷ Click to view the table of general integration formulas.

$$\int_{0}^{1} \frac{2x}{(x^{2} + 1)^{3}} dx =$$
 (Type an exact answer.)

7: General Integration Formulas

$$\int \cos ax \, dx = \frac{1}{a} \sin ax + C$$

$$\int \sin ax \, dx = -\frac{1}{a} \cos ax + C$$

$$\int \sec^2 ax \, dx = \frac{1}{a} \tan ax + C$$

$$\int \csc^2 ax \, dx = -\frac{1}{a} \cot ax + C$$

$$\int \sec ax \tan ax \, dx = \frac{1}{a} \sec ax + C$$

$$\int \csc ax \cot ax \, dx = -\frac{1}{a} \csc ax + C$$

$$\int \csc ax \cot ax \, dx = -\frac{1}{a} \csc ax + C$$

$$\int b^x \, dx = \frac{1}{a} b^x + C, \quad b > 0, \quad b \neq 1$$

$$\int \frac{dx}{a^2 + x^2} = \frac{1}{a} \tan^{-1} \frac{x}{a} + C$$

$$\int \frac{dx}{\sqrt{a^2 - x^2}} = \sin^{-1} \frac{x}{a} + C, \quad a > 0$$

Answer: $\frac{3}{8}$

$$\int_{0}^{\frac{\pi}{4}} 2 \tan x \sec^2 x \, dx$$

⁸ Click to view the table of general integration formulas.

$$\int_{0}^{\frac{\pi}{4}} 2 \tan x \sec^{2} x \, dx =$$
 (Type an exact answer.)

8: General Integration Formulas

$$\int \cos ax \, dx = \frac{1}{a} \sin ax + C$$

$$\int \sin ax \, dx = -\frac{1}{a} \cos ax + C$$

$$\int \sec^2 ax \, dx = \frac{1}{a} \tan ax + C$$

$$\int \csc^2 ax \, dx = -\frac{1}{a} \cot ax + C$$

$$\int \sec ax \tan ax \, dx = \frac{1}{a} \sec ax + C$$

$$\int \csc ax \ \cot ax \, dx = -\frac{1}{a} \csc ax + C$$

$$\int e^{ax} dx = \frac{1}{a} e^{ax} + C$$

$$\int b^x dx = \frac{1}{\ln b} b^x + C, \ b > 0, \ b \neq 1$$

$$\int \frac{dx}{a^2 + x^2} = \frac{1}{a} \tan^{-1} \frac{x}{a} + C$$

$$\int \frac{dx}{\sqrt{a^2 - x^2}} = \sin^{-1} \frac{x}{a} + C, \ a > 0$$

Answer: 1

$$\int_{0}^{3} \frac{x^2}{x^3 + 7} dx$$

⁹ Click to view the table of general integration formulas.

$$\int_{0}^{3} \frac{x^{2}}{x^{3}+7} dx =$$
 (Type an exact answer.)

9: General Integration Formulas

$$\int \cos ax \, dx = \frac{1}{a} \sin ax + C$$

$$\int \sin ax \, dx = -\frac{1}{a} \cos ax + C$$

$$\int \sec^2 ax \, dx = \frac{1}{a} \tan ax + C$$

$$\int \csc^2 ax \, dx = -\frac{1}{a} \cot ax + C$$

$$\int \sec ax \tan ax \, dx = \frac{1}{a} \sec ax + C$$

$$\int \csc ax \cot ax \, dx = -\frac{1}{a} \csc ax + C$$

$$\int e^{ax} dx = \frac{1}{a} e^{ax} + C$$

$$\int b^x dx = \frac{1}{\ln b} b^x + C, \ b > 0, \ b \neq 1$$

$$\int \frac{dx}{a^2 + x^2} = \frac{1}{a} \tan^{-1} \frac{x}{a} + C$$

$$\int \frac{dx}{\sqrt{a^2 - x^2}} = \sin^{-1} \frac{x}{a} + C, \ a > 0$$

Answer: $\frac{1}{3} \ln \frac{34}{7}$

136. Evaluate the following integral.

$$\int \frac{\mathrm{d}x}{x^2 - 2x + 17}$$

 $\int \frac{\mathrm{d}x}{x^2 - 2x + 17} =$

(Use C as the arbitrary constant as needed.)

Answer:
$$\frac{1}{4} \tan^{-1} \frac{x-1}{4} + C$$

137. Evaluate the following integral using integration by parts.

$$\int$$
 13t e^{t} dt

Use the integration by parts formula so that the new integral is simpler than the original one. Choose the correct answer below.

• A.
$$13t e^{t} + \int (13t e^{t}) dt$$

• B. $13 e^{t} - \int (13t e^{t}) dt$
• C. $13 e^{t} + \int (13 e^{t}) dt$
• D. $13t e^{t} - \int (13 e^{t}) dt$

Evaluate the integral.

$$\int 13t e^{t} dt =$$
(Use C as the arbitrary constant as needed.)

Answers
D. 13t
$$e^{t} - \int (13 e^{t}) dt$$

13t $e^{t} - 13 e^{t} + C$

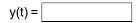
138. Evaluate the following integral using integration by parts.

$$\int 16x \ln 8x \, dx$$

$$\int 16x \ln 8x \, dx =$$
(Use C as the arbitrary constant as needed.)

Answer: $8x^2 \ln 8x - 4x^2 + C$

139. If the general solution of a differential equation is $y(t) = C e^{-5t} + 4$, what is the solution that satisfies the initial condition y(0) = 7?



Answer: $3e^{-5t} + 4$