

1

Factor
 $81x^2 - 49 =$
 $(9x)^2 - (7)^2 =$

$(9x+7)(9x-7) =$

for mula
 $a^2 - b^2 = (a+b)(a-b)$

1

m0410046 stepd

MATH 0320 Final Exam Review

2.

Solve
 $(2x+1)(5x-3) = 0$

Let $2x+1=0$ OR $5x-3=0$

$2x+1-1=0-1$ OR $5x-3+3=0+3$

$2x=-1$ OR $5x=3$

$\frac{2x}{2} = \frac{-1}{2}$ OR $\frac{5x}{5} = \frac{3}{5}$

$x = -\frac{1}{2}$ OR $x = \frac{3}{5}$

3.

Solve

$x^2 + 2x - 80 = 0$

$(x-8)(x+10) = 0$

Let $x-8=0$ OR $x+10=0$

$x-8+8=0+8$ OR $x+10-10=0-10$

$x=8$ OR $x=-10$

30.1
 40.2
 20.4
 10.8
 Possible

4.

Solve

$x^2 - 7x - 18 = 0$

$(x+2)(x-9) = 0$

Let $x+2=0$ OR $x-9=0$

$x+2-2=0-2$ OR $x-9+9=0+9$

$x=-2$ OR $x=9$

18.1
 9.2
 6.3
 Possible

5.

Solve

$$x^2 - x = 72$$

$$x^2 - x - 72 = 72 - 72$$

$$x^2 - x - 72 = 0$$

$$(x + 8)(x - 9) = 0$$

Ans $x + 8 = 0$ OR $x - 9 = 0$

$$x + 8 - 8 = 0 - 8 \quad \text{OR} \quad x - 9 + 9 = 0 + 9$$

$$x = -8 \quad \text{OR} \quad x = 9$$

72.1
36.2
18.4
9.8

Possible

2

6.

Solve

$$x^2 + 3x = 28$$

$$x^2 + 3x - 28 = 28 - 28$$

$$x^2 + 3x - 28 = 0$$

$$(x - 4)(x + 7) = 0$$

Ans $x - 4 = 0$ OR $x + 7 = 0$

$$x - 4 + 4 = 0 + 4 \quad \text{OR} \quad x + 7 - 7 = 0 - 7$$

$$x = 4 \quad \text{OR} \quad x = -7$$

28.1
14.2
4.7

7.

Solve

$$2x^2 - 7x - 9 = 0$$

$$(2x - 9)(x + 1) = 0$$

Ans $2x - 9 = 0$ OR $x + 1 = 0$

$$2x - 9 + 9 = 0 + 9 \quad \text{OR} \quad x + 1 - 1 = 0 - 1$$

$$2x = 9 \quad \text{OR}$$

$$x = -1$$

$$\frac{2x}{2} = \frac{9}{2}$$

$$x = \frac{9}{2}$$

2.1

9.1
3.3

8.

Solve

$$15x^2 - 8x = 0$$

$$x(15x - 8) = 0$$

or $x = 0$ OR $15x - 8 = 0$

$$15x - 8 + 8 = 0 + 8$$

$$15x = 8$$

OR $\frac{15x}{15} = \frac{8}{15}$

$$x = \frac{8}{15}$$

3

9.

Solve

$$9x^2 - 16 = 0$$

$$(3x)^2 - (4)^2 = 0$$

$$(3x + 4)(3x - 4) = 0$$

or $3x + 4 = 0$ OR $3x - 4 = 0$

$$3x + 4 - 4 = 0 - 4 \quad \text{OR} \quad 3x - 4 + 4 = 0 + 4$$

$$3x = -4 \quad \text{OR} \quad 3x = 4$$

$$\frac{3x}{3} = \frac{-4}{3} \quad \text{OR} \quad \frac{3x}{3} = \frac{4}{3}$$

$$x = \frac{-4}{3} \quad \text{OR} \quad x = \frac{4}{3}$$

for middle
 $a^2 - b^2 = (a + b)(a - b)$

10.

Solve

$$3x^2 + 21x + 36 = 0$$

$$3(x^2 + 7x + 12) = 0$$

$$3(x + 3)(x + 4) = 0$$

~~3 = 0~~ OR $x + 3 = 0$
 $x + 3 - 3 = 0 - 3$

$$x = -3$$

OR $x + 4 = 0$

OR $x + 4 - 4 = 0 - 4$

OR $x = -4$

12-1
6-2
3-4

possible

11.

Solve

$$15x^2 + 31x + 1 = -9$$

$$15x^2 + 31x + 1 + 9 = -9 + 9$$

$$15x^2 + 31x + 10 = 0$$

$$(3x+5)(5x+2) = 0$$

Ans $3x+5=0$ OR $5x+2=0$

$$3x+5-5=0-5 \text{ OR } 5x+2-x-x=0-2$$

$$3x = -5 \text{ OR } 5x = -2$$

$$\frac{3x}{3} = \frac{-5}{3} \text{ OR } \frac{5x}{5} = \frac{-2}{5}$$

$$x = -\frac{5}{3} \text{ OR } x = -\frac{2}{5}$$

15.1

3.5

10.1

2.5

4

Possible

12

Solve

$$10x^3 + 70x^2 + 120x = 0$$

$$10x(x^2 + 7x + 12) = 0$$

$$10x(x+3)(x+4) = 0$$

Ans $10x=0$ OR $x+3=0$ OR $x+4=0$

$$\frac{10x}{10} = \frac{0}{10} \text{ OR } x+3-3=0-3 \text{ OR } x+4-4=0-4$$

$$x=0 \text{ OR } x=-3 \text{ OR } x=-4$$

12.1

6.2

3.4

13

Solve

$$y^3 + 6y^2 + 9y = 0$$

$$y(y^2 + 6y + 9) = 0$$

$$y(y+3)(y+3) = 0$$

$$y=0 \text{ OR } y+3=0 \text{ OR } y+3=0$$

$$y+3-3=0-3 \text{ OR } y+3-3=0-3$$

$$y=-3 \text{ OR } y=-3$$

9.1, 3.3 possible

Solve

14.

$$(3x+2)(9x^2+12x+4)=0$$

$$(3x+2)(3x+2)(3x+2)=0$$

$$\begin{matrix} 9 \cdot 1 \\ 3 \cdot 3 \end{matrix}$$

$$\begin{matrix} 4 \cdot 1 \\ 2 \cdot 2 \end{matrix}$$

9

but $3x+2=0$ or $3x+2=0$ or $3x+2=0$

$$3x + \cancel{x} - \cancel{x} = 0 - 2 \quad \text{or} \quad 3x + 2 - 2 = 0 - 2 \quad \text{or} \quad 3x + 2 - 2 = 0 - 2$$

$$3x = -2 \quad \text{or} \quad 3x = -2 \quad \text{or} \quad 3x = -2$$

$$\frac{3x}{3} = \frac{-2}{3} \quad \text{or} \quad \frac{\cancel{3}x}{\cancel{3}} = \frac{-2}{3} \quad \text{or} \quad \frac{\cancel{3}x}{\cancel{3}} = \frac{-2}{3}$$

$$x = -\frac{2}{3} \quad \text{or} \quad x = -\frac{2}{3} \quad \text{or} \quad x = -\frac{2}{3}$$

15.

Solve

$$9x^3 - 16x = 0$$

$$x(9x^2 - 16) = 0$$

$$x((3x)^2 - (4)^2) = 0$$

$$x(3x+4)(3x-4) = 0$$

but $x=0$ or $3x+4=0$ or $3x-4=0$

$$3x + \cancel{4} - 4 = 0 - 4 \quad \text{or} \quad 3x - \cancel{4} + 4 = 0 + 4$$

$$3x = -4 \quad \text{or} \quad 3x = 4$$

$$\frac{3x}{3} = \frac{-4}{3} \quad \text{or} \quad \frac{\cancel{3}x}{\cancel{3}} = \frac{4}{3}$$

$$x = -\frac{4}{3} \quad \text{or} \quad x = \frac{4}{3}$$

Formula
 $a^2 - b^2 = (a+b)(a-b)$

16.

Solve

$$25x^3 - 30x^2 + 8x = 0$$

$$x(25x^2 - 30x + 8) = 0$$

$$x(5x-2)(5x-4) = 0$$

Ans $x=0$ OR $5x-2=0$ OR $5x-4=0$

$$5x - \cancel{x} + \cancel{x} = 0 + 2 \quad \text{OR} \quad 5x - \cancel{4} + \cancel{4} = 0 + 4$$

$$5x = 2 \quad \text{OR} \quad 5x = 4$$

$$\frac{5x}{5} = \frac{2}{5} \quad \text{OR} \quad \frac{5x}{5} = \frac{4}{5}$$

$$x = \frac{2}{5} \quad \text{OR} \quad x = \frac{4}{5}$$

25.1
5.5
8.1
2.4
Possible
6

17.

Simplify

$$\frac{2y}{4y+2} \cdot \frac{10y+5}{7} =$$

$$\frac{2y}{2(2y+1)} \cdot \frac{5(2y+1)}{7} =$$

$$\frac{5y}{7} =$$

18.

Simplify

$$\frac{x^2 - y^2}{x+y} \div \frac{x}{x^2 - xy} =$$

$$\frac{x^2 - y^2}{x+y} \cdot \frac{x^2 - xy}{x} =$$

$$\frac{(x+y)(x-y)}{(x+y)} \cdot \frac{x(x-y)}{x} =$$

$(x-y)(x-y) =$ OR
 $(x-y)^2 =$

19. $\frac{x^2 - 8x}{x-6} + \frac{12}{x-6} =$ Simplify

$$\frac{(x^2 - 8x) + (12)}{x-6} =$$

$$\frac{x^2 - 8x + 12}{x-6} =$$

$$\frac{(x-2)(x-6)}{(x-6)} =$$

$$x-2 =$$

Solve

20.

$$13 \leq 4t + 5 \leq 29$$

$$13 - 5 \leq 4t + 5 - 5 \leq 29 - 5$$

$$8 \leq 4t \leq 24$$

$$\frac{8}{4} \leq \frac{4t}{4} \leq \frac{24}{4}$$

$$2 \leq t \leq 6$$



$$[2, 6]$$

12-1
6-2
3-4 possible

10

21.

Solve

$$|x+3|=6$$

$|x|=a$ formula
 $x=-a$ OR $x=a$

8

or $x+3=-6$ OR $x+3=6$

$$x+x-3=-6-3 \text{ OR } x+x-3=6-3$$

$x=-9$ OR $x=3$

22.

Solve

$$|x+18| < 9$$

formula
 $|x| < a$
 $-a < x < a$

$$-9 < x+18 < 9$$

$$-9-18 < x+18-x < 9-18$$

$-27 < x < -9$



$(-27, -9)$

23.

Solve

$$|x+3| > 4$$

$|x| > a$
 $x < -a$ OR $x > a$

or $x+3 < -4$ OR $x+3 > 4$

$$x+x-3 < -4-3 \text{ OR } x+x-3 > 4-3$$

$x < -7$ OR $x > 1$



$(-\infty, -7) \cup (1, +\infty)$

24.

Simplify

$$\sqrt{16 \times 10} =$$

$$\sqrt{4^2 \times 10} =$$

$$4^1 \times 10^{\frac{1}{2}} =$$

$$4 \times 10^{\frac{1}{2}} =$$

9.

25.

$f(x) = \sqrt{2x+7}$ find $f(37)$

$$f(37) = \sqrt{2(37)+7}$$

$$f(37) = \sqrt{74+7}$$

$$f(37) = \sqrt{81}$$

$$f(37) = 9$$

26.

graph $f(x) = \sqrt{x} - 4$

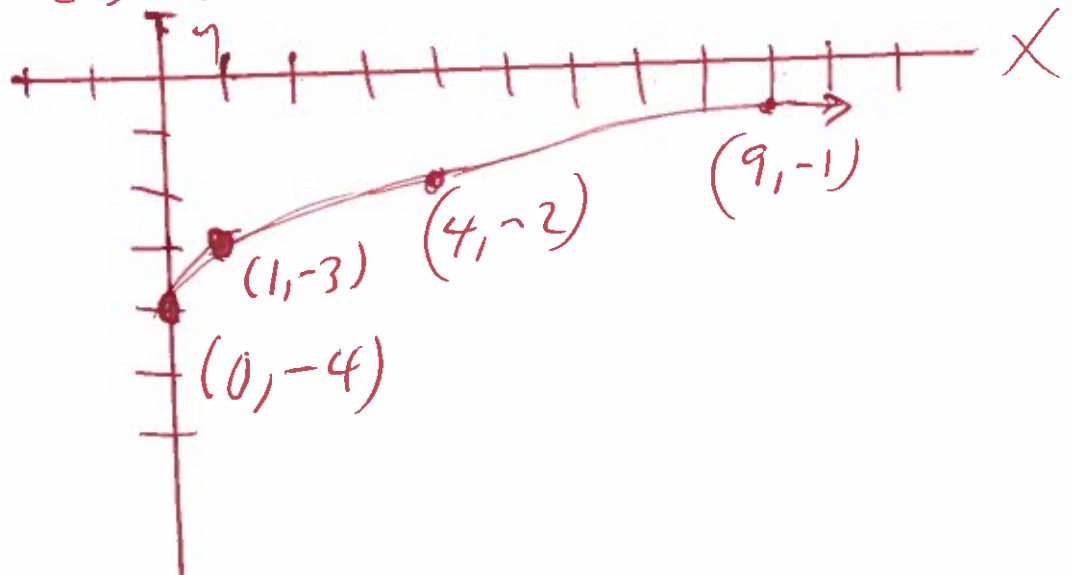
$$f(0) = \sqrt{0} - 4 = 0 - 4 = -4$$

$$f(1) = \sqrt{1} - 4 = 1 - 4 = -3$$

$$f(4) = \sqrt{4} - 4 = 2 - 4 = -2$$

$$f(9) = \sqrt{9} - 4 = 3 - 4 = -1$$

x	f(x)
0	-4
1	-3
4	-2
9	-1



(12)

27

$$256^{1/4} =$$

$$(4^4)^{1/4} =$$

$$(4^{4/4})^{1/4} =$$

$$4^{1/4} =$$

$$4^1 =$$

$$4 =$$

28

Simplify Primes 2, 3, 5, 7, ...

$$\sqrt{20} =$$

$$\sqrt{4 \cdot 5} =$$

$$\sqrt{4} \sqrt{5} =$$

$$2\sqrt{5} =$$

$$\begin{array}{r} 2 \overline{) 20} \\ \underline{4} \\ 2 \\ \underline{4} \\ 5 \\ \underline{5} \\ 1 \end{array}$$

29

Simplify Primes 2, 3, 5, 7, ...

$$\sqrt{320 k^7 q^8} =$$

$$\sqrt{2^6 \cdot 5 \cdot k^6 \cdot k^1 \cdot q^8} =$$

$$2^3 k^3 q^4 \sqrt{5k} =$$

$$2 \cdot 2 \cdot 2 k^3 q^4 \sqrt{5k} =$$

$$8 k^3 q^4 \sqrt{5k} =$$

$$\begin{array}{r} 2 \overline{) 320} \\ \underline{640} \\ 2 \overline{) 160} \\ \underline{320} \\ 2 \overline{) 80} \\ \underline{160} \\ 2 \overline{) 40} \\ \underline{80} \\ 2 \overline{) 20} \\ \underline{40} \\ 2 \overline{) 10} \\ \underline{20} \\ 5 \overline{) 5} \\ \underline{5} \\ 1 \end{array}$$

30 $\sqrt[3]{512x^4y^5}$ Primes 2, 3, 5, 7, ...

$$\sqrt[3]{2^9 x^3 y^3 y^2} =$$

$$2^3 x^1 y^1 \sqrt[3]{x^1 y^2} =$$

$$2 \cdot 2 \cdot 2 \cdot xy \sqrt[3]{xy^2} =$$

$$8xy \sqrt[3]{xy^2} =$$

$$\begin{array}{r} 2 \overline{) 512} \\ \underline{2} \\ 256 \\ 2 \overline{) 256} \\ \underline{2} \\ 228 \\ 2 \overline{) 228} \\ \underline{2} \\ 208 \\ 2 \overline{) 208} \\ \underline{2} \\ 184 \\ 2 \overline{) 184} \\ \underline{2} \\ 160 \\ 2 \overline{) 160} \\ \underline{2} \\ 128 \\ 2 \overline{) 128} \\ \underline{2} \\ 96 \\ 2 \overline{) 96} \\ \underline{2} \\ 64 \\ 2 \overline{) 64} \\ \underline{2} \\ 32 \\ 2 \overline{) 32} \\ \underline{2} \\ 16 \\ 2 \overline{) 16} \\ \underline{2} \\ 8 \\ 2 \overline{) 8} \\ \underline{2} \\ 4 \\ 2 \overline{) 4} \\ \underline{2} \\ 2 \end{array}$$

31 Find distance $(-4, 2)$ and $(-12, -4)$
 $x_1 \quad y_1 \quad x_2 \quad y_2$

$$d = \sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2}$$

$$d = \sqrt{(-4) - (-12))^2 + (2) - (-4))^2}$$

$$d = \sqrt{(-4 + 12)^2 + (2 + 4)^2}$$

$$d = \sqrt{(8)^2 + (6)^2}$$

$$d = \sqrt{64 + 36}$$

$$d = \sqrt{100}$$

$$d = 10$$

32 Find mid point $(4, -8)$ and $(0, 4)$
 $x_1 \quad y_1 \quad x_2 \quad y_2$

$$\text{mid point} = \left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$$

$$\text{mid point} = \left(\frac{(4) + (0)}{2}, \frac{(-8) + (4)}{2} \right)$$

$$\text{mid point} = \left(\frac{4+0}{2}, \frac{-8+4}{2} \right)$$

$$= \left(\frac{4}{2}, \frac{-4}{2} \right)$$

$$= (2, -2)$$

33

Solve

$$\sqrt{x+4} = 8$$

$$(\sqrt{x+4})^2 = (8)^2$$

$$x+4 = 64$$

$$x+4-4 = 64-4$$

$$x = 60$$

12

34

$$\sqrt{20x+20} = x+6$$

$$(\sqrt{20x+20})^2 = (x+6)^2$$

$$20x+20 = (x+6)(x+6)$$

$$20x+20 = x^2+6x+6x+36$$

$$20x+20 = x^2+12x+36$$

$$0 = x^2+12x+36-20x-20$$

$$0 = x^2-8x+16$$

$$0 = (x-4)(x-4)$$

Let $x-4=0$ or $x-4=0$

$x-4+4=0+4$ or $x-4+4=0+4$

$x=4$

or $x=4$

possible

- 16.1
- 8.2
- 4.4

ck

$$\sqrt{20x+20} = x+6$$

Good

$$\sqrt{20(4)+20} = (4)+6$$

$$\sqrt{80+20} = 4+6$$

$$\sqrt{100} = 10$$

$$10 = 10 \quad \checkmark$$

{ 4 }

35. $(6+6i) - (-9+i) =$
 $6+6i+9-i =$
 $6+6i+9-1i =$
 $15+5i =$

13.

36. $(5+3i)(5-3i) =$
 $25 - 15i + 15i - 9i^2 =$
 $25 - 9i^2 =$
 $25 - 9(-1) =$
 $25 + 9 =$
 $34 =$ OR $34 + 0i$

Formula
 $i^2 = -1$

37. $\frac{8+7i}{9-2i} =$
 $\left(\frac{8+7i}{9-2i}\right) \left(\frac{9+2i}{9+2i}\right) =$
 $\frac{72 + 16i + 63i + 14i^2}{81 + 18i - 18i - 4i^2} =$
 $\frac{72 + 79i + 14i^2}{81 - 4i^2} =$
 $\frac{72 + 79i + 14(-1)}{81 - 4(-1)} =$
 $\frac{72 + 79i - 14}{81 + 4} =$
 $\frac{58 + 79i}{85} =$

Formula
 $i^2 = -1$

$\frac{58}{85} + \frac{79i}{85} =$

$$38 \quad (x-5)^2 = 36$$

$$\sqrt{(x-5)^2} = \pm\sqrt{36}$$

$$x-5 = \pm 6$$

$$\text{2A } x-5 = -6 \quad \text{OR} \quad x-5 = 6$$

$$x-5+5 = -6+5 \quad \text{OR} \quad x-5+5 = 6+5$$

$$x = -1 \quad \text{OR} \quad x = 11$$

4

$$39 \quad x^2 + 24x + 144 = 0 \quad \text{use quadratic formula}$$

$$a=1, \quad b=24, \quad c=144$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{-(24) \pm \sqrt{(24)^2 - 4(1)(144)}}{2(1)}$$

$$x = \frac{-24 \pm \sqrt{576 - 576}}{2}$$

$$x = \frac{-24 \pm \sqrt{0}}{2}$$

$$x = \frac{-24 \pm 0}{2}$$

$$x = -12 \pm 0$$

$$x = -12 - 0 \quad \text{OR}$$

$$x = -12 + 0$$

$$x = -12 \quad \text{OR}$$

$$x = -12$$

$$40 \quad 1x^2 + 18x + 70 = 0$$

$$a=1, b=18, c=70$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{-(18) \pm \sqrt{(18)^2 - 4(1)(70)}}{2(1)}$$

$$x = \frac{-18 \pm \sqrt{324 - 280}}{2}$$

$$x = \frac{-18 \pm \sqrt{44}}{2}$$

$$x = \frac{-18 \pm \sqrt{4 \cdot 11}}{2}$$

$$x = \frac{-18 \pm \sqrt{4} \sqrt{11}}{2}$$

$$x = \frac{-18 \pm 2\sqrt{11}}{2}$$

$$x = -9 \pm \sqrt{11}$$

$$x = -9 + \sqrt{11}$$

$$x = -9 - \sqrt{11} \quad \text{or}$$

$$x = -9 + \sqrt{11}$$

Prime 2, 3, 5, 7.

$$\begin{array}{r} 2 \overline{) 44} \\ \underline{22} \\ 22 \\ \underline{22} \\ 0 \end{array}$$

15.

41) $x^2 - 8x + 20 = 0$
 $a=1, b=-8, c=20$

Use Quadratic formula

16.

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{-(-8) \pm \sqrt{(-8)^2 - 4(1)(20)}}{2(1)}$$

$$x = \frac{8 \pm \sqrt{64 - 80}}{2}$$

$$x = \frac{8 \pm \sqrt{-16}}{2}$$

$$x = \frac{8 \pm 4i}{2}$$

$$x = 4 \pm 2i$$

$$x = 4 - 2i \text{ or}$$

$$x = 4 + 2i$$

use Quadratic Formula

42) $2x^2 - 7x - 9 = 0$
 $a=2, b=-7, c=-9$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{-(-7) \pm \sqrt{(-7)^2 - 4(2)(-9)}}{2(2)}$$

$$x = \frac{7 \pm \sqrt{49 + 72}}{4}$$

$$x = \frac{7 \pm \sqrt{121}}{4}$$

$$x = \frac{7 \pm 11}{4}$$

$$x = \frac{7-11}{4} \text{ or}$$

$$x = \frac{7+11}{4}$$

$$x = \frac{-4}{4} \text{ or}$$

$$x = \frac{18}{4}$$

$$x = -1 \text{ or}$$

$$x = \frac{2(9)}{2(2)}$$

$$x = \frac{9}{2}$$

$$43 \quad 7x^2 = -12x - 3$$

$$7x^2 + 12x + 3 = 0$$

$$a=7, b=12, c=3$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{-(12) \pm \sqrt{(12)^2 - 4(7)(3)}}{2(7)}$$

$$x = \frac{-12 \pm \sqrt{144 - 84}}{14}$$

$$x = \frac{-12 \pm \sqrt{60}}{14}$$

$$x = \frac{-12 \pm \sqrt{4 \cdot 15}}{14}$$

$$x = \frac{-12 \pm \sqrt{4} \sqrt{15}}{14}$$

$$x = \frac{-12 \pm 2\sqrt{15}}{14}$$

$$x = \frac{2(-6 \pm \sqrt{15})}{2(7)}$$

$$x = \frac{-6 \pm \sqrt{15}}{7}$$

$$x = \frac{-6 - \sqrt{15}}{7} \text{ OR}$$

$$x = \frac{-6 + \sqrt{15}}{7}$$

Use Quadratic Formula

17

Prime 2, 3, 5, 7

$$\begin{array}{r} 2 \overline{) 60} \\ \underline{2 0} \\ 0 \\ 3 \overline{) 45} \\ \underline{3 0} \\ 0 \\ 5 \overline{) 15} \\ \underline{5 0} \\ 0 \\ 1 \end{array}$$

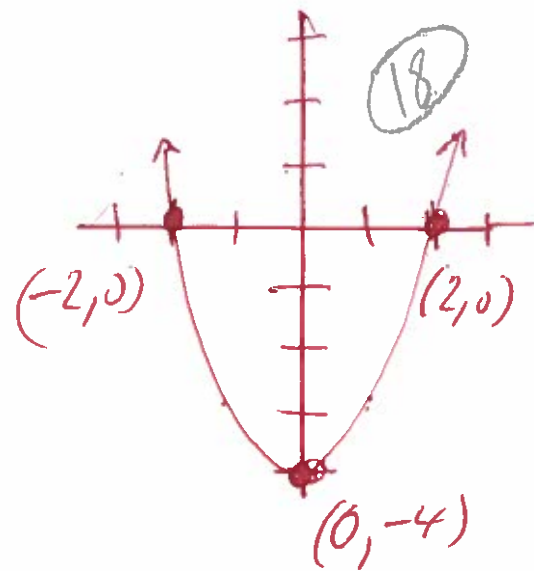
44 graph $f(x) = x^2 - 4$

$$f(-2) = (-2)^2 - 4 = (-2)(-2) - 4 = 4 - 4 = 0$$

$$f(0) = (0)^2 - 4 = (0)(0) - 4 = 0 - 4 = -4$$

$$f(2) = (2)^2 - 4 = (2)(2) - 4 = 4 - 4 = 0$$

x	f(x)
-2	0
0	-4
2	0



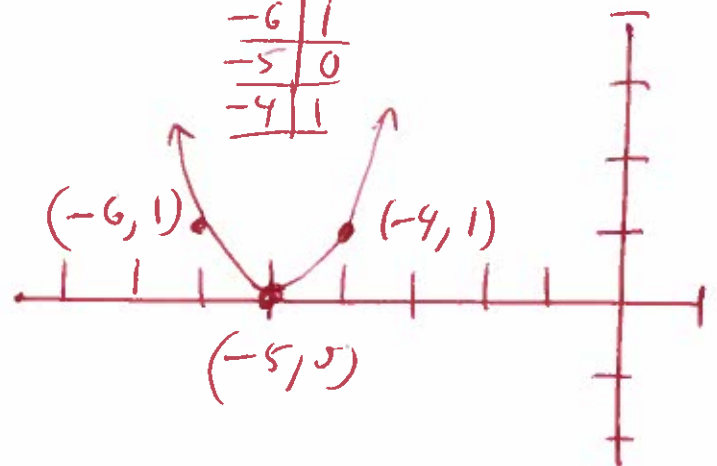
45 graph $f(x) = (x+5)^2$

$$f(-6) = (-6+5)^2 = (-1)^2 = (-1)(-1) = 1$$

$$f(-5) = (-5+5)^2 = (0)^2 = (0)(0) = 0$$

$$f(-4) = (-4+5)^2 = (1)^2 = (1)(1) = 1$$

x	f(x)
-6	1
-5	0
-4	1



46 graph $f(x) = -x^2 - 5$

$$f(-1) = -(-1)^2 - 5 = -(-1)(-1) - 5 = -1 - 5 = -6$$

$$f(0) = -(0)^2 - 5 = -(0)(0) - 5 = 0 - 5 = -5$$

$$f(1) = -(1)^2 - 5 = -(1)(1) - 5 = -1 - 5 = -6$$

x	f(x)
-1	-6
0	-5
1	-6

