

09-15-19
09-17-1909-15-19
09-16-19

1. Solve the inequality: $16 - 3x > 10$

Write the solution in interval notation.

2. Given $f(x) = 3x^2 + 4x - 2$ find the following:

a) $f(0) = \underline{\hspace{2cm}}$

b) $f(-x) = \underline{\hspace{2cm}}$

c) $f(x+1) = \underline{\hspace{2cm}}$

d) $f(x+h) = \underline{\hspace{2cm}}$

3. Find the domain of the function $f(x) = \sqrt{4x - 20}$. Use interval notation.

4. For the given functions find the following:

$$f(x) = 4x + 7 \quad g(x) = 8x - 1$$

a) $(f + g)(x) = \underline{\hspace{2cm}}$

b) $(g - f)(x) = \underline{\hspace{2cm}}$

c) $(f - g)(3) = \underline{\hspace{2cm}}$

d) $(f \cdot g)(2) = \underline{\hspace{2cm}}$

5. Find and simplify the difference quotient of f given: $\frac{f(x+h) - f(x)}{h}$, $h \neq 0$

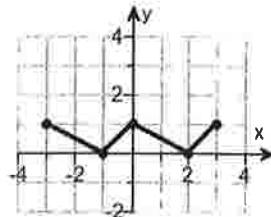
$$f(x) = x^2 - 8x + 3$$

6. Given $f(x) = x^2 - 2x + 2$, find the value(s) for x such that $f(x) = 17$.

7. Using the given graph of the function f , find its domain and range.

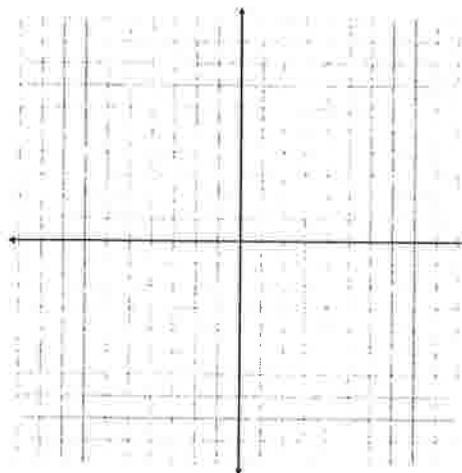
Domain: _____

Range: _____



8. The function f is defined as follows: $f(x) = \begin{cases} -3x + 4 & \text{if } x < 2 \\ 2x - 1 & \text{if } x \geq 2 \end{cases}$

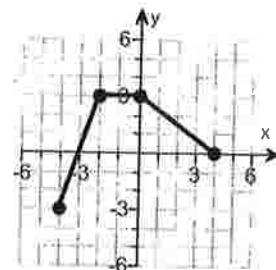
Graph the function.



9. The graph of a function f is illustrated to the right. Use the graph of f and graph each of the following functions.

a) $H(x) = f(x + 2) - 3$

b) $G(x) = f(x) + 2$



10. Factor the given polynomial completely.

$$x^2 + 18x + 77$$

11. Solve the equation: $(x - 8)(3x + 5) = 0$

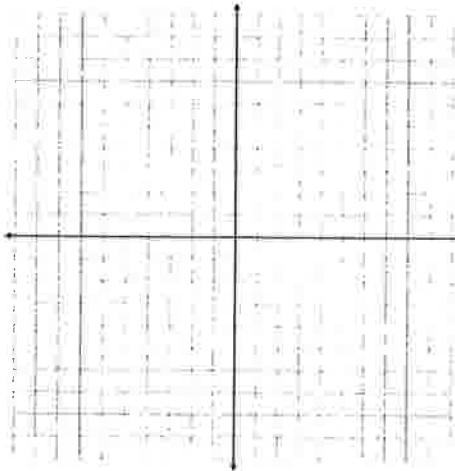
12. Find the zeros of the quadratic function by factoring: $g(x) = 3x^2 - 10x - 8$

13. Solve the quadratic equation by using the quadratic formula. Simplify your answer as much as possible.

$$x^2 + 6x = -4$$

14. Given the quadratic function $f(x) = x^2 - 4x + 3$ find the following and graph f.

a) the vertex



b) the y-intercept

c) the x-intercept(s)

15. Determine, without graphing, whether the given quadratic function has a maximum value or a minimum value and then find the value and where it occurs.

$$f(x) = -2x^2 + 4x - 7$$

16. Find a rational zero of the polynomial function and use it to find all of the zeros of the function.

$$f(x) = x^3 - 3x^2 - 25x - 21$$

17. Solve the equation: $3x^4 - 28x^3 + 81x^2 - 84x + 20 = 0$

18. Find the vertical and horizontal asymptotes, if any, for the following rational function.

$$R(x) = \frac{8x^2}{x^2 - 2x - 15}$$

19. Given the functions: $f(x) = 4x + 9$ and $g(x) = 2x - 5$, find the following

a) $(f \circ g)(x)$

b) $(g \circ f)(x)$

20. Given the functions: $f(x) = 3x + 3$ and $g(x) = x^2$, find the following

a) $(g \circ f)(x)$

b) $(f \circ g)(-3)$

21) The function $f(x) = 6x - 3$ is one-to-one. Find the following and graph f and f^{-1} .

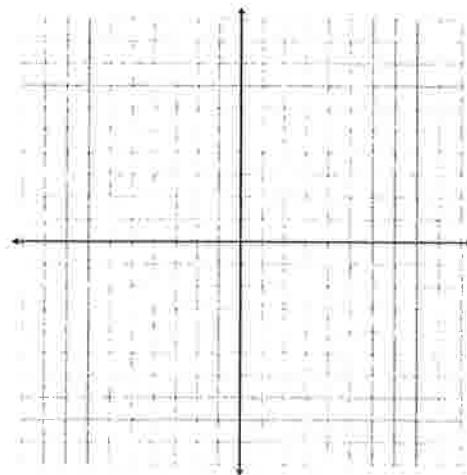
a) $f^{-1}(x) =$

b) Domain of f :

Range of f :

c) Domain of f^{-1} :

Range of f^{-1} :



22) Solve the equation: $64^{-x+52} = 128^x$

23) Solve the equation: $\log_2(2x + 1) = 3$

24) Solve the equation: $\log_4(5x) = 2$

25) Find the accumulated value of a \$400 investment after 4 years if interest is compounded quarterly at an annual rate of 5.2%.

26) How many years will it take for an investment of \$10,000 to grow to \$35,000?

Assume an interest rate of 9% compounded continuously.

27. Solve the system of equations by addition. If the system has no solution, say that it is inconsistent.

$$4x - 3y = -1$$

$$5x + y = 13$$

28. Solve the given system of equations using matrices. If the system has no solution, say that it is inconsistent.

$$x - 3y + 4z = 24$$

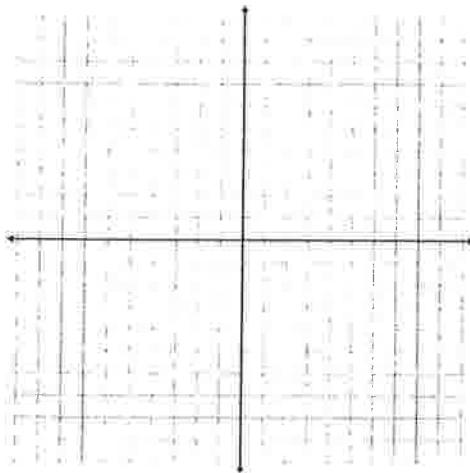
$$2x + y + z = 6$$

$$-2x + 3y - 3z = -22$$

29. Solve the radical equation: $\sqrt{5x - 1} = x - 3$

Be sure to check all solutions.

30. The quadratic function $f(x) = x^2 - 2x - 8$ has a vertex at $(1, -9)$, a y-intercept at $(0, -8)$, and x-intercepts at $(4, 0)$ and $(-2, 0)$. Also, $f(2) = -8$. Sketch the graph of this quadratic function by plotting the 5 given points.



Solve

① $16 - 3x > 10$

$$16 - 3x \cancel{+ 6} > 10 - 16$$

$$-3x > -6$$

$$\frac{-3x}{-3} < \frac{-6}{-3}$$

divide by a
negative at
turn all signs
around

$$x < 2$$

$$x < 2$$

$$2$$

$$(-\infty, 2)$$

$$\textcircled{2a} \quad f(x) = 3x^2 + 4x - 2$$

$$f(0) = 3(0)^2 + 4(0) - 2$$

$$f(0) = 3(0)x_0 + 4(0) - 2$$

$$f(0) = 3(0) + 4(0) - 2$$

$$f(0) = 0 + 0 - 2$$

$$f(0) = 0 - 2$$

$$f(0) = -2$$

$$\textcircled{2b} \quad f(x) = 3x^2 + 4x - 2$$

$$f(-x) = 3(-x)^2 + 4(-x) - 2$$

$$f(-x) = 3(-x)(-x) + 4(-x) - 2$$

$$f(-x) = 3(x^2) + 4(-x) - 2$$

$$(f(-x)) = 3x^2 - 4x - 2$$

(2c) $f(x) = 3x^2 + 4x - 2$

$$f(x+1) = 3(x+1)^2 + 4(x+1) - 2$$

$$f(x+1) = 3(x+1)(x+1) + 4(x+1) - 2$$

$$f(x+1) = 3(x^2 + 1x + 1x + 1) + 4(x+1) - 2$$

$$f(x+1) = 3(x^2 + 2x + 1) + 4(x+1) - 2$$

$$\underline{f(x+1) = 3x^2 + 6x + 3 + 4x + 4 - 2}$$

$$\underline{\underline{f(x+1) = 3x^2 + 10x + 5}}$$

(2d) $f(x) = 3x^2 + 4x - 2$

$$f(x+h) = 3(x+h)^2 + 4(x+h) - 2$$

$$f(x+h) = 3(x+h)(x+h) + 4(x+h) - 2$$

$$f(x+h) = 3(x^2 + xh + xh + h^2) + 4(x+h) - 2$$
~~$$f(x+h) = 3(x^2 + 1xh + 1xh + h^2) + 4(x+h) - 2$$~~
~~$$f(x+h) = 3(x^2 + 2xh + h^2) + 4(x+h) - 2$$~~

$$\underline{\underline{f(x+h) = 3x^2 + 6xh + 3h^2 + 4x + 4h - 2}}$$

③ find the domain

$$f(x) = \sqrt{4x - 20}$$

but $4x - 20 \geq 0$

$$4x - 4 + 20 \geq 0 + 20$$

$$4x \geq 20$$

$$\frac{4x}{4} \geq \frac{20}{4}$$

$$x \geq 5$$



5

$$[5, \infty)$$

formula
domain

$$f(x) = \sqrt{Ax+B}$$

$$\text{but } Ax+B \geq 0$$

(4a) $f(x) = 4x + 7$ und $g(x) = 8x - 1$

$$(f+g)(x) =$$

$$f(x) + g(x) =$$

$$(4x + 7) + (8x - 1) =$$

$$4x + 7 + 8x - 1 =$$

$$12x + 6 =$$

(4b) $f(x) = 4x + 7$ und $g(x) = 8x - 1$

$$(g - f)(x) =$$

$$g(x) - f(x) =$$

$$(8x - 1) - (4x + 7) =$$

$$8x - 1 - 4x - 7 =$$

$$4x - 8 =$$

(4) Given $f(x) = 4x+7$ and $g(x) = 8x-1$

Find $(f-g)(x) =$

$$f(x) - g(x) =$$

$$(4x+7) - (8x-1) =$$

$$4x+7 - 8x+1 =$$

$$-4x+8$$

1st
do this

$$(f-g)(x) = -4x+8$$

$$(f-g)(3) = -4(3)+8$$

2nd
do this

$$(f-g)(3) = -12+8$$

$$(f-g)(3) = -4$$

(E) (4) $f(x) = 4x + 7$ and $g(x) = 8x - 1$

$$(f \circ g)(x) =$$

$$f(g(x)) =$$

$$(4x+7)(8x-1) =$$

1st
do this

$$32x^2 - 4x + 56x - 7 =$$

$$32x^2 + 52x - 7 =$$

$$(f \circ g)(x) = 32x^2 + 52x - 7$$

2nd
do this

$$(f \circ g)(2) = 32(2)^2 + 52(2) - 7$$

$$(f \circ g)(2) = 32(2)(2) + 52(2) - 7$$

$$(f \circ g)(2) = 32(4) + 52(2) - 7$$

$$(f \circ g)(2) = 128 + 104 - 7$$

$$(f \circ g)(2) = 232 - 7$$

$$(f \circ g)(2) = 225$$

$$⑤ f(x) = x^2 - 8x + 3$$

$$\frac{f(x+h) - f(x)}{h} =$$

$$\frac{(x+h)^2 - 8(x+h) + 3 - (x^2 - 8x + 3)}{h} =$$

$$\frac{(x+h)(x+h) - 8x - 8h + 3 - x^2 + 8x - 3}{h} =$$

$$\frac{x^2 + xh + xh + h^2 - 8x - 8h + 3 - x^2 + 8x - 3}{h} =$$

$$\frac{x^2 + (xh + xh + h^2) - 8x - 8h + 3 - x^2 + 8x - 3}{h} =$$

$$\frac{2xh + h^2 - 8h}{h} =$$

$$\frac{2xh}{h} + \frac{h^2}{h} - \frac{8h}{h} =$$

$$2x + h - 8 =$$

⑥ Given $f(x) = x^2 - 2x + 2$ find the values
for x such that $f(x) = 17$

$$\text{ie } x^2 - 2x + 2 = 17$$

$$x^2 - 2x + 2 - 17 = 17 - 17$$

$$x^2 - 2x - 15 = 0$$

$$(x+3)(x-5) = 0$$

$$\text{ie } x+3=0 \quad \text{OR} \quad x-5=0$$

$$x+3-3=0-3 \quad \text{OR} \quad x-5+5=0+5$$

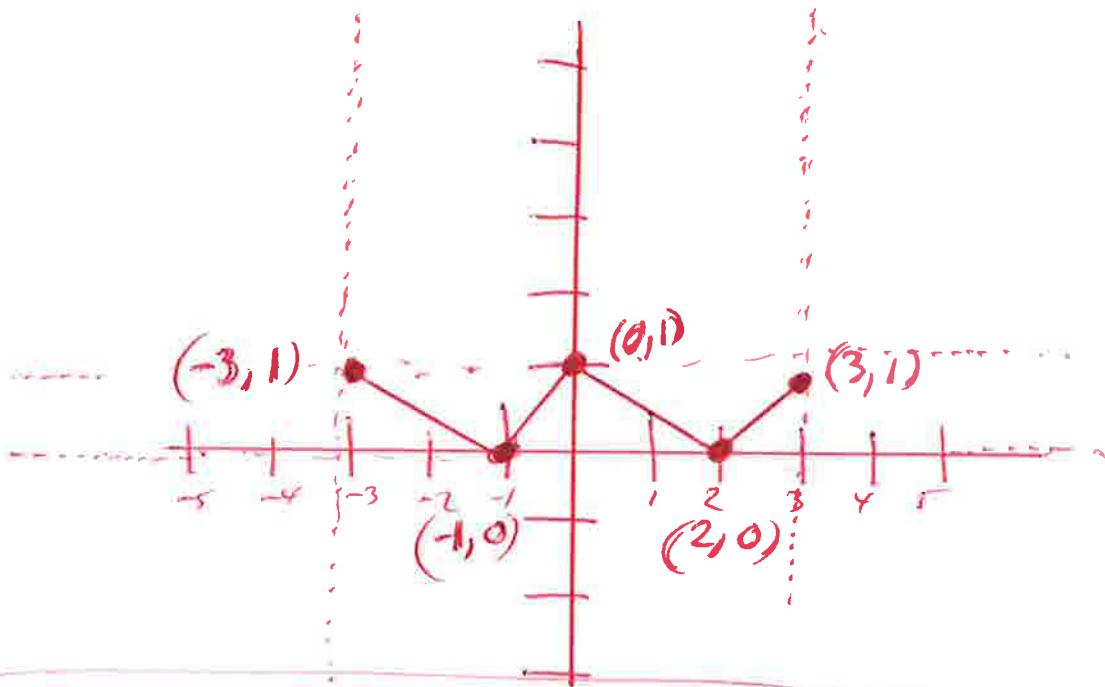
$$x=-3$$

$$\text{or } x=5$$

Possible
15.1
3.5



Q. Use the given graph of the function f , find its domain and range.

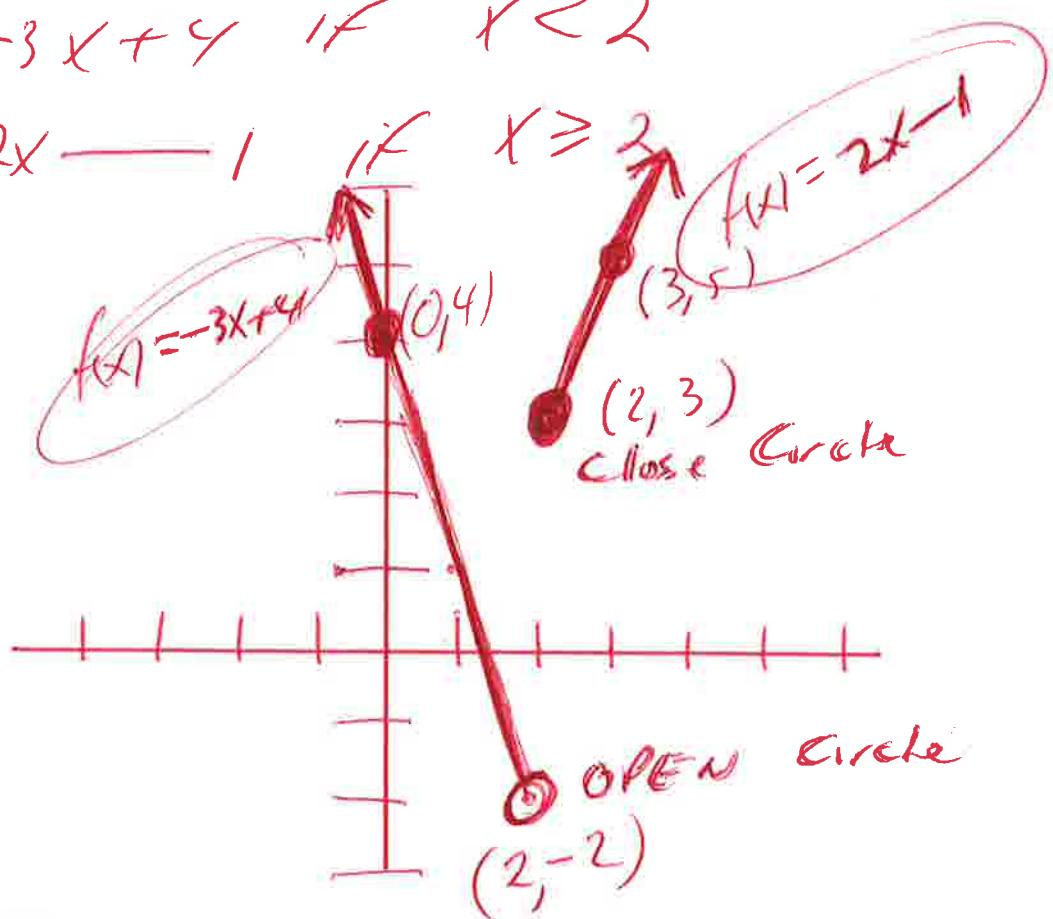


$$\text{domain} = [-3, 3] \leftarrow [\text{left}, \text{right}]$$

$$\text{range} = [0, 1] \leftarrow [\text{bottom}, \text{top}]$$

⑧ Graph

$$f(x) = \begin{cases} -3x + 4 & \text{if } x < 2 \\ 2x - 1 & \text{if } x \geq 2 \end{cases}$$



window

$$X_{\text{Min}} = -12$$

$$X_{\text{Max}} = 12$$

$$Y_{\text{Min}} = -10$$

$$Y_{\text{Max}} = 10$$

using
graphing
calculator

2nd
math

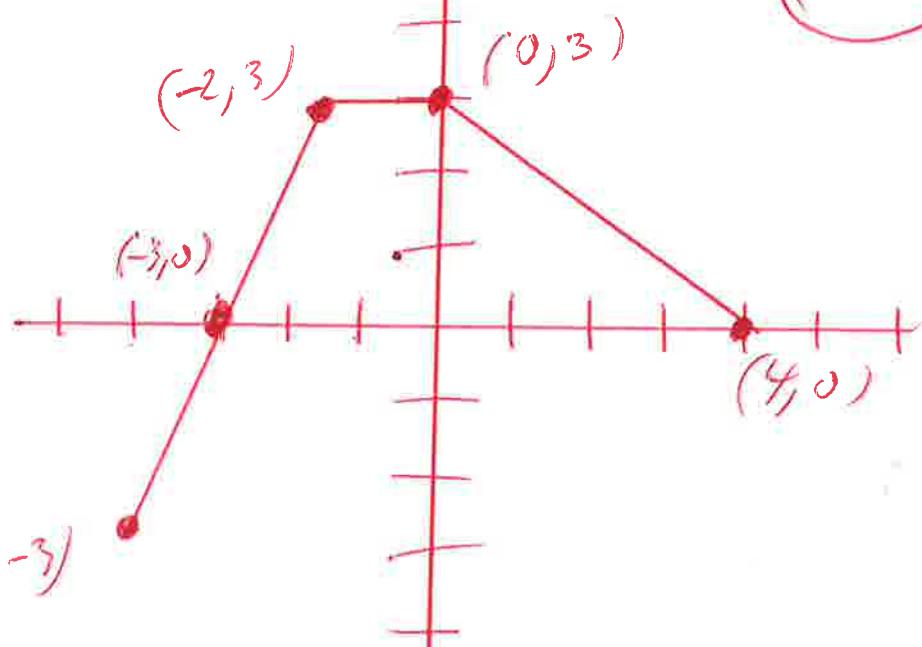
$$y_1 = -3x + 4 \quad \div (x < 2) \quad \text{open circle}$$

$$y_2 = 2x - 1 \quad \div (x \geq 2) \quad \text{closed circle}$$

$\textcircled{1}$ $f(x)$

$\textcircled{2} f(x+2)$

$\textcircled{3} f(x+2) - 3$

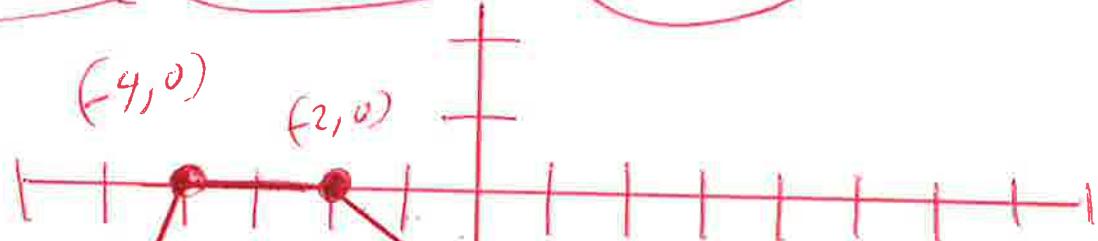


$$H(x) = f(x+2) - 3$$

Shift down
-3

NEW

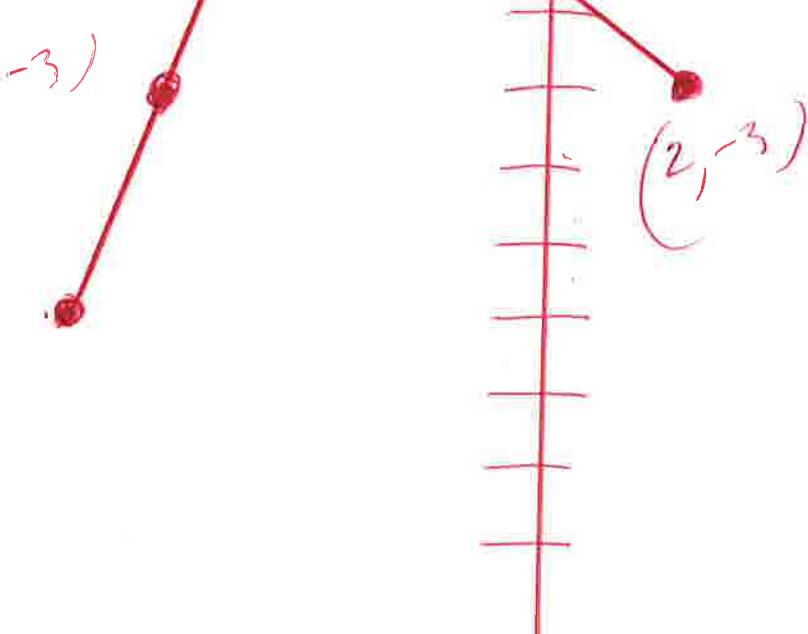
Shift left
-2

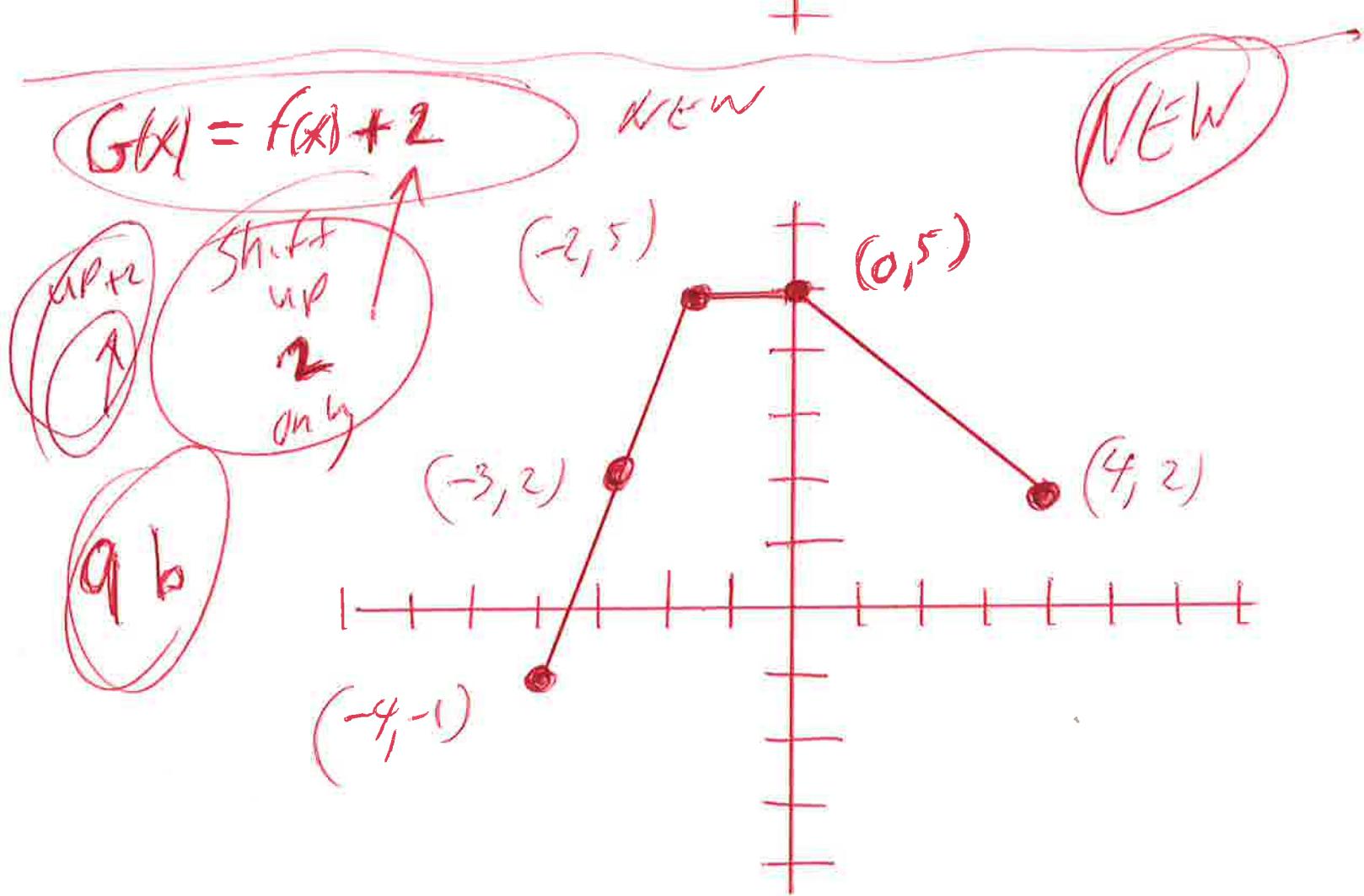
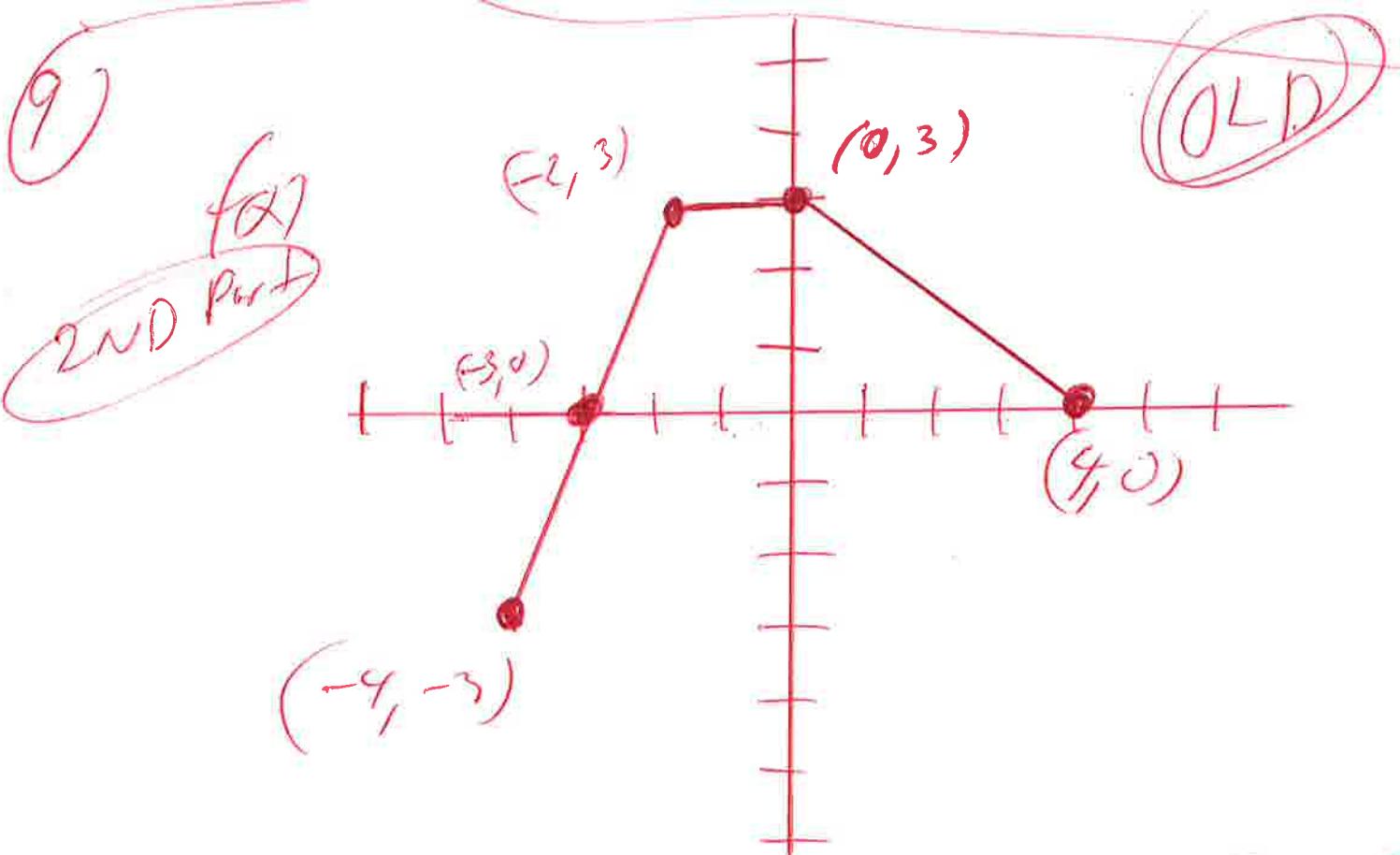


$\textcircled{4} g(x)$

Shift left
 $\leftarrow -2$
 $\downarrow -3$

Shift left
 $\leftarrow -6$





(16) Factor

$$x^2 + 18x + 77 =$$

Possible
77, 1

7, 11

$$(x+7)(x+11) =$$

Check

$$(x+7)(x+11) =$$

$$x^2 + 11x + 7x + 77 =$$

$$x^2 + 18x + 77 =$$

Good

(11)

Solve

$$(x-8)(3x+5) = 0$$

set $x-8=0$ OR

$$3x+5=0$$

$$x-8+8=0+8 \quad \text{OR}$$

$$\cancel{3x+5} = 0-5$$

$x=8$ OR

$$3x = -5$$

$$\frac{3x}{3} = \frac{-5}{3}$$

$$x = -\frac{5}{3}$$

(12) Find the zeros of the quadratic function by factoring

$$g(x) = 3x^2 - 10x - 8$$

$$3x^2 - 10x - 8 = 0$$

$$(3x + 2)(x - 4) = 0$$

Let $3x + 2 = 0$ OR $x - 4 = 0$

$$3x + 2 = 0 - 2 \quad \text{OR} \quad x - 4 + 4 = 0 + 4$$

$$3x = -2$$

$$\frac{3x}{3} = \frac{-2}{3}$$

$$x = -\frac{2}{3}$$

OR $x = 4$

Poss. b/g

(3,-1)

(8,1)
2,-4

(B) Solve the quadratic equation by using
the quadratic formula

$$x^2 + 6x = -4$$

$$x^2 + 6x + 4 = -4 + 4$$

$$x^2 + 6x + 4 = 0$$

$$x^2 + 6x + 4 = 0$$

$$a=1, b=6, c=4$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{-(6) \pm \sqrt{(6)^2 - 4(1)(4)}}{2(1)}$$

$$x = \frac{-6 \pm \sqrt{36 - 16}}{2}$$

$$x = \frac{-6 \pm \sqrt{20}}{2}$$

$$x = \frac{-6 \pm \sqrt{4 \cdot 5}}{2} \text{ rewrite}$$

$$x = \frac{-6 \pm \sqrt{4 \cdot 5}}{2}$$

Primes
2, 3, 5, 7, 11, ...

~~2(2)~~
~~2(1)~~
5(5)
1

$$20 = 2 \cdot 2 \cdot 5$$

OR
20 = 4 \cdot 5

$$x = -6 \pm \frac{\pm 2\sqrt{5}}{2}$$

$$x = -\frac{6}{2} \pm \frac{\pm 2\sqrt{5}}{2}$$

$$x = -3 \pm \sqrt{5}$$

$$x = -3 \pm \sqrt{5}$$

$$x = -3 + \sqrt{5}$$

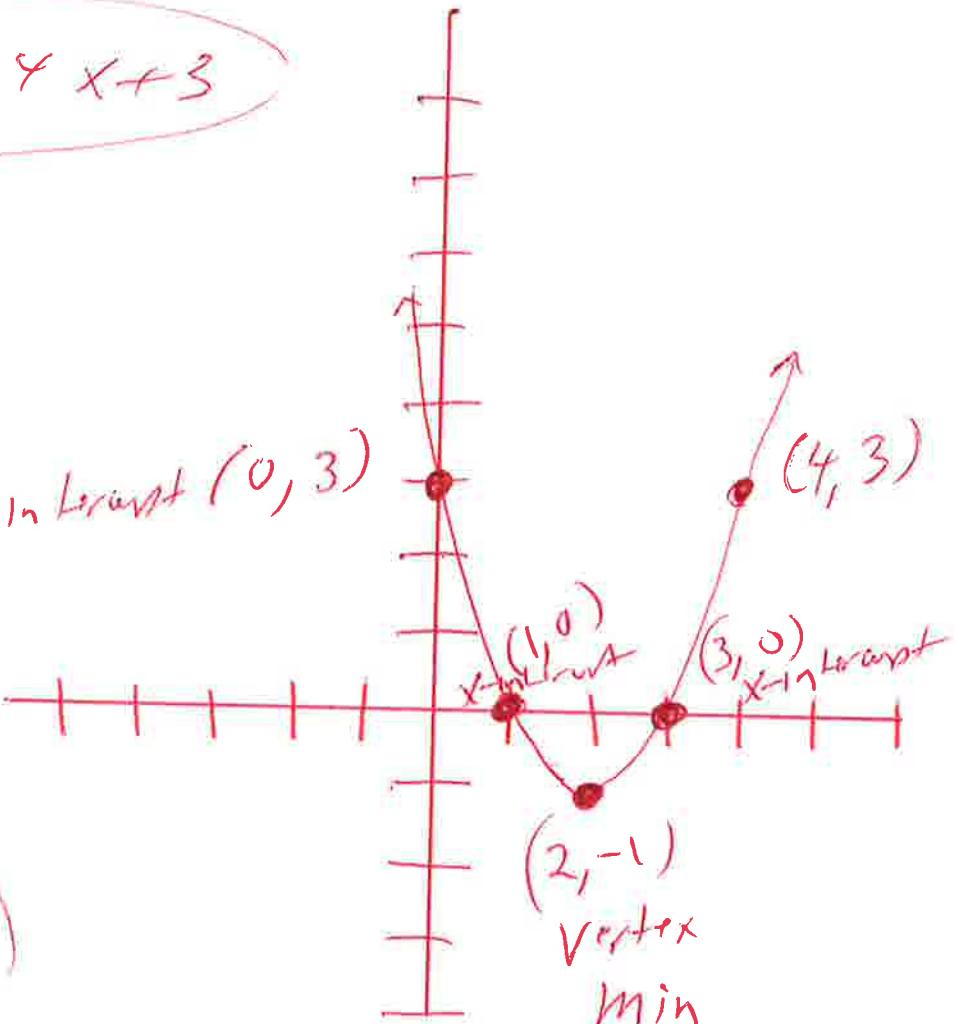
OR

$$x = -3 - \sqrt{5}$$

(14.) graph

$$f(x) = x^2 - 4x + 3$$

y-intercept $(0, 3)$



windows

$$x_{\text{min}} = -12$$

$$x_{\text{max}} = 12$$

$$y_{\text{min}} = -10$$

$$y_{\text{max}} = 10$$

use graphing
calculator

$$y_1 = x^2 - 4x + 3$$

BIG

$$\text{Vertex} = (2, -1) \quad \text{min}$$

$$y\text{-intercept} = (0, 3)$$

$$x\text{-intercepts} = (1, 0) \text{ and } (3, 0)$$

⑯. determine without graphing whether the given quadratic function has a maximum value or a minimum value and then find the value where it occurs

~~Since it is negative graph opens down and has a Max~~

$$\text{MAX } f(x) = -2x^2 + 4x - 7$$

$$a = -2, b = 4, c = -7$$

$$\text{Vertex} = \left(-\frac{b}{2a}, f\left(-\frac{b}{2a}\right) \right) \quad \text{formula}$$

$$\text{Vertex } x = \left(-\frac{(4)}{2(-2)}, f\left(\frac{4}{2(-2)}\right) \right)$$

$$\text{Vertex} = \left(-\frac{4}{-4}, f\left(\frac{4}{-4}\right) \right)$$

$$\text{Vertex} = (1, f(1))$$

$$\text{Vertex} = (1, -2(1)^2 + 4(1) - 7)$$

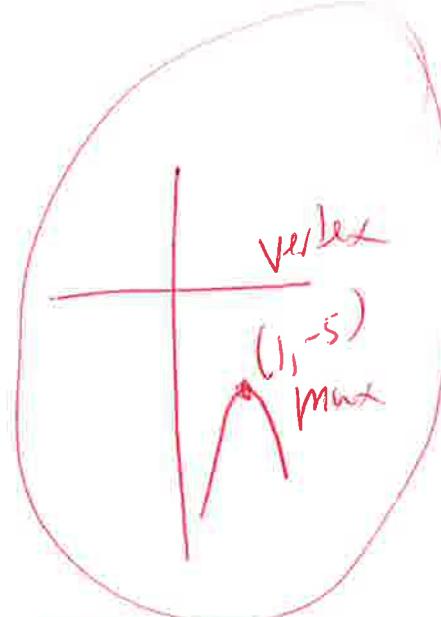
$$\text{Vertex} = (1, -2(1)(1) + 4(1) - 7)$$

$$\text{Vertex} = (1, -2(1) + 4(1) - 7)$$

$$\text{Vertex} = (1, -2 + 4 - 7)$$

$$\text{Vertex} = (1, 2 - 7)$$

$$\text{Vertex} = (1, -5) \quad \text{Max}$$



$$⑯ f(x) = x^3 - 3x^2 - 25x - 21$$

Possible

use synthetic division

Last
First

try $x = -1$

$$\frac{\pm 21}{\pm 1}$$

$$\begin{array}{cccccc} -1 & | & 1 & -3 & -25 & -21 \\ & | & -1 & 4 & 21 & \\ \hline & | & 1 & -4 & -21 & 0 \end{array}$$

from $\pm 21, \pm 7, \pm 3, \pm 1$

$$\text{set } x^2 - 4x - 21 = 0 \leftarrow$$

Possible
 $21 \cdot 1$
 $7 \cdot 3$

$$(x+3)(x-7) = 0$$

$3(2)$
 $7(1)$

$$x+3=0 \quad \text{or} \quad x-7=0$$

$$x+3-3=0-3 \quad \text{OR} \quad x-7+7=0+7$$

$x = -3$

$x = 7$

Answer

$$\boxed{-1 \quad -3 \quad 7}$$

$$(17) \quad 3x^4 - 28x^3 + 81x^2 - 84x + 2020$$

possibly
LAST
First
 $\frac{+20}{x-3}$

Use Synthetic division

$$\begin{matrix} \pm 20, \pm 10, \pm 5, \pm 4, \pm 2, \pm 1 \\ \pm 3, \pm 1 \end{matrix}$$

$$\begin{matrix} \pm 20 & \pm 10 & \pm 5 & \pm 4 & \pm 2 & \pm 1 \\ \hline 1 & 1 & 1 & 1 & 1 & 1 \\ & 3 & 3 & 3 & 3 & 3 \\ \hline & \pm 20 & \pm 10 & \pm 5 & \pm 4 & \pm 1 \end{matrix}$$

use synthetic division try $x=2$

$$\begin{array}{r} (2) \quad 3 \quad -28 \quad 81 \quad -84 \quad 20 \\ \hline 6 \quad -44 \quad 74 \quad -20 \\ \hline 3 \quad -22 \quad 37 \quad -10 \quad 0 \end{array} \quad \text{rem}$$

$$\begin{array}{r} (2) \quad 3 \quad -22 \quad 37 \quad -10 \\ \hline 6 \quad -32 \quad 10 \\ \hline 3 \quad -16 \quad 5 \quad 0 \end{array} \quad \begin{matrix} \text{try } x=2 \text{ again} \\ \text{use synthetic division} \end{matrix}$$

$\downarrow \quad \downarrow \quad \downarrow$

$$3x^2 - 16x + 5 = 0$$

$$(3x-1)(x-5) = 0$$

$$3x-1=0 \quad \text{or} \quad x-5=0$$

$$3x-1+1=0+1 \quad \text{OR} \quad x-5+5=0+5$$

$$3x=1$$

$$\frac{3x}{3} = \frac{1}{3}$$

$$x = \frac{1}{3}$$

$$\text{OR } x=5$$

Answer

$$\boxed{2, 2, \frac{1}{3}, 5} \quad \checkmark$$

OR

$$\boxed{2, \frac{1}{3}, 5} \quad \checkmark$$

Repeat

18. Find the vertical and horizontal asymptotes

$$R(x) = \frac{8x^2}{x^2 - 2x - 15}$$

set $x^2 - 2x - 15 = 0$

$$(x+3)(x-5) = 0$$

$$x+3=0 \text{ OR } x-5=0$$

$$x+3-3=x-3 \text{ OR } x-5+5=x+5$$

$$x=-3$$

$$\text{OR } x=5$$

Vertical asymptotes

set $\frac{8x^2}{1x^2} = \frac{\text{highest power top}}{\text{highest power bottom}}$

$$\frac{8}{1} = 8 \text{ Simplify}$$

$$8 =$$

$$y = 8$$

horizontal asymptote

⑯ $f(x) = 4x + 9$ and $g(x) = 2x - 5$

a) $(f \circ g)(x) =$

$f(g(x)) =$

$f(2x - 5) =$

$4(2x - 5) + 9 =$

$8x - 20 + 9 =$

$8x - 11 =$

✓✓✓

b) $(g \circ f)(x) =$

$g(f(x)) =$

$g(4x + 9) =$

$2(4x + 9) - 5 =$

$8x + 18 - 5 =$

$8x + 13 =$

$f(x) = 4x + 9$ and $g(x) = 2x - 5$

$$(20) \quad f(x) = 3x + 3 \quad \text{and} \quad g(x) = x^2$$

$$\text{(a)} \quad (g \circ f)(x) =$$

$$g(f(x)) =$$

$$g(3x+3) =$$

$$(3x+3)^2 =$$

$$(3x+3)(3x+3) =$$

$$9x^2 + 9x + 9x + 9^2 \quad \checkmark$$

$$9x^2 + 18x + 9 =$$

$$\text{(b)} \quad (f \circ g)(-3) \quad \text{find} \quad f(x) = 3x + 3 \quad \text{at} \quad g(x) = x^2$$

$$(f \circ g)(x) = \text{1st}$$

$$f(g(x)) = \text{do this}$$

$$f(x^2) =$$

$$3(x^2) + 3 = x$$

$$3x^2 + 3 =$$

$$(f \circ g)(x) = 3x^2 + 3$$

$$(f \circ g)(-3) = 3(-3)^2 + 3$$

$$(f \circ g)(-3) = 3(-3)(-3) + 3$$

$$(f \circ g)(-3) = 3(9) + 3$$

$$(f \circ g)(-3) = 27 + 3$$

$$(f \circ g)(-3) = 30 \quad \checkmark$$

④ The function $f(x) = 6x - 3$ is ~~one-to-one~~
Find the following at graph f at f^{-1}

$$f(x) = 6x - 3$$

$$\text{let } y = 6x - 3$$

$$x = 6y - 3$$

$$x + 3 = 6y - 3 + 3$$

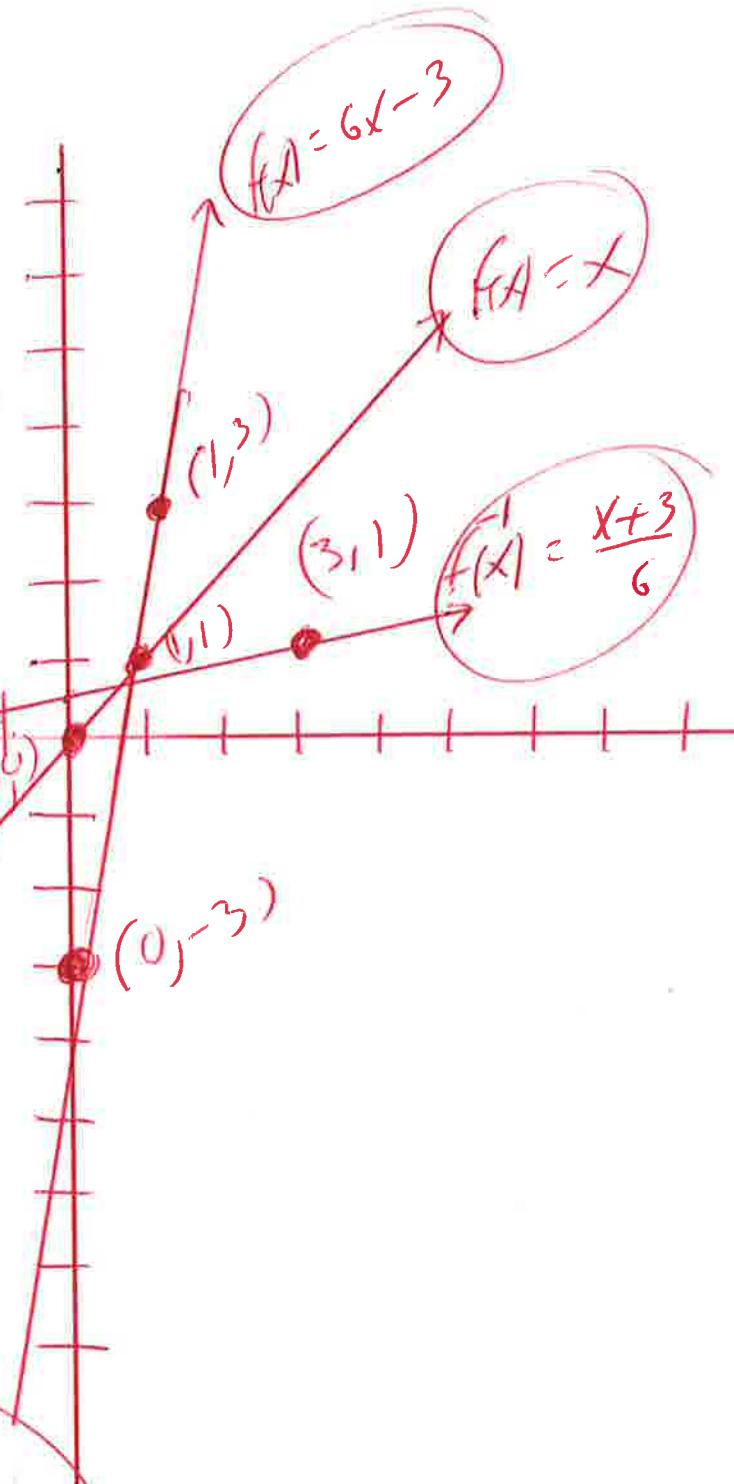
$$x + 3 = 6y$$

$$\frac{x+3}{6} = \cancel{\frac{6y}{6}} \quad (\cancel{6})$$

$$\frac{x+3}{6} = y$$

$$y = \frac{x+3}{6}$$

$$f^{-1}(x) = \frac{x+3}{6}$$



One-to-one

22

Solve

$$-x + 52$$

$$64 = 128^x$$

$$(2^6)^{-x+52} = (2^7)^x$$

rewr1k

$$\cancel{2}^{-6x+312} = \cancel{2}^{7x}$$

$$-6x + 312 = 7x$$

$$-6x + 312 - 312 = 7x - 312$$

$$-6x = 7x - 312$$

$$-6x - 7x = 7x - 312 - 7x$$

$$-13x = -312$$

$$\frac{-13x}{-13} = \frac{-312}{-13}$$

$$x = 24$$

(23)

Solve \leftarrow
 $\log_2(2x+1) = 3$



$$2^3 = 2x+1$$

rewr1k

$$2 \cdot 2 \cdot 2 = 2x+1$$

$$8 = 2x+1$$

$$8 - 1 = 2x+1 - 1$$

$$7 = 2x$$

$$\frac{7}{2} = \frac{2x}{2}$$

$$\frac{7}{2} = x$$

(24) Solve ~~\log~~

$$\log_4(5x) = 2$$



$$4^2 = 5x \quad \text{Rewrite}$$

$$4 \cdot 4 = 5x$$

$$16 = 5x$$

$$\frac{16}{5} = \cancel{5}x$$

$$\frac{16}{5} = x$$

(25) find the accumulated value of a \$400 investment after 4 years if interest is compounded quarterly at an annual rate of 5.2%

$$A = P(1 + \frac{r}{N})^{Nt}$$

$$A = \$400 \left(1 + \frac{0.052}{4}\right)^{4(4)}$$

$$A = \$400 \left(1 + \frac{0.052}{4}\right)^{16}$$

$$A = \$400 \left(1 + \frac{0.052}{4}\right)^{16}$$

$$A = \$491.8255849$$

$$P = \$400$$

$$r = 5.2\% = .052$$

$$N = 4 = \text{quarterly}$$

$$t = 4 = \text{years}$$

MS
graphing
calculator

OR

Round

$$A = \$491.83$$

⑥ how many years will it take for an investment of $\$10,000$ to grow to $\$135,000$? Assume an interest rate 9% compounded continuously.

$$A = Pe^{rt} \quad \text{formula}$$

$$35000 = 10000e^{.09t}$$

$$\frac{35000}{10000} = \frac{10000e^{.09t}}{10000}$$

$$3.5 = e^{.09t}$$

$$\ln(3.5) = \ln(e^{.09t})$$

$$\ln(3.5) = .09t \ln(e)$$

$$\ln(3.5) = .09t(1)$$

$$\ln(3.5) = .09t$$

$$\frac{\ln(3.5)}{.09} = \frac{.09t}{.09}$$

$$13.91958854 = t$$

years

Or

$$13.92 \text{ years} = t$$

Round

$$A = \$35,000$$

$$P = \$10,000$$

$$r = 9\% = .09$$

$$t = ?? = \text{years}$$

formula

$$\ln(A^n) = n \ln A$$

$$\ln(e) = 1$$

(27)

$$4x - 3y = -1$$

$$5x + y = 13$$

$$\begin{array}{r} \\ \hline \end{array} \left(\begin{array}{l} 4x - 3y = -1 \\ 5x + y = 13 \end{array} \right) \left(\begin{array}{l} 1 \\ 3 \end{array} \right) \text{ mult}$$

$$\begin{array}{r} \\ \hline \end{array} \left(\begin{array}{l} 4x - 3y = -1 \\ 15x + 3y = 39 \end{array} \right) \left(\begin{array}{l} \\ 3 \end{array} \right)$$

$$19x = 38$$

$$\frac{19x}{19} = \frac{38}{19}$$

$$x = 2$$

Subs

$$4x - 3y = -1$$

$$4(2) - 3y = -1$$

$$8 - 3y = -1$$

$$8 - 3y - 8 = -1 - 8$$

$$-3y = -9$$

$$\frac{-3y}{-3} = \frac{-9}{-3}$$

$$y = 3$$

$$\checkmark \quad \checkmark$$

$$(x, y) = (2, 3)$$

(28)
$$\begin{array}{rcl} x - 3y + 4z & = & 24 \\ 2x + y + z & = & 6 \\ -2x + 3y - 3z & = & -22 \end{array}$$

Use
graphing
C.a(calculation)

2nd Matrix, edit, [A], 3x3, enter

$$[A] = \begin{bmatrix} 1 & -3 & 4 & 24 \\ 2 & 1 & 1 & 6 \\ -2 & 3 & -3 & -22 \end{bmatrix}$$

2nd Matrix, Math, ↓, rref(), enter

$$\text{rref}([A]) =$$

$$\begin{bmatrix} 1 & 0 & 0 & 2 \\ 0 & 1 & 0 & -2 \\ 0 & 0 & 1 & 4 \end{bmatrix} \quad \begin{pmatrix} x \\ y \\ z \end{pmatrix}$$

$(x, y, z) = (2, -2, 4)$

$$29) \sqrt{5x-1} = x-3$$

$$(\sqrt{5x-1})^2 = (x-3)^2$$

$$5x-1 = (x-3)(x-3)$$

$$5x-1 = x^2 - 3x - 3x + 9$$

$$5x-1 = x^2 - 6x + 9$$

$$0 = x^2 - 6x + 9 - 5x + 1$$

$$0 = x^2 - 11x + 10$$

$$0 = (x-1)(x-10)$$

$$\text{so } x-1=0 \text{ OR } x-10=0$$

$$x-1+1=0+1 \text{ OR } x-10+10=0+10$$

~~$x=1$~~ OR $x=10$

Check

$$\sqrt{5x-1} = x-3$$

$$\sqrt{5(1)-1} = 1-3$$

$$\sqrt{5-1} = 1-3$$

$$\sqrt{4} = -2$$

$$2 \neq -2$$

BAD

$$\sqrt{5(10)-1} = 10-3$$

$$\sqrt{50-1} = 10-3$$

$$\sqrt{49} = 7$$

$$7 = 7$$

Good

answer

$$\boxed{x=10 \text{ only}}$$

(Solve)

from

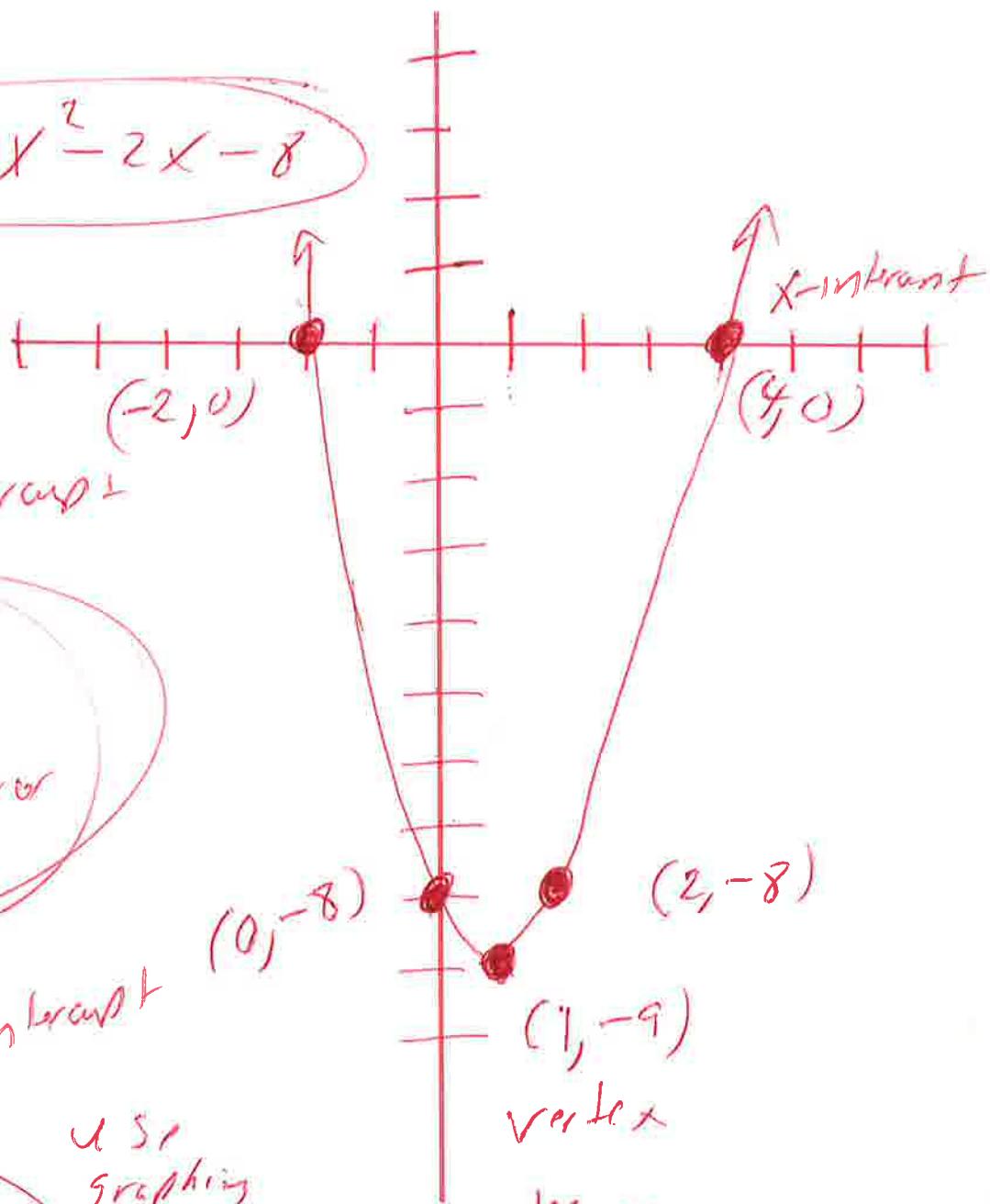
check

Possible

10, 1
2, 5

30. graph

$$f(x) = x^2 - 2x - 8$$



using
graphing
calculator

window

$$x_{\min} = -12$$

$$x_{\max} = 12$$

$$y_{\min} = -10$$

$$y_{\max} = 10$$

using
graphing
calculator

$$y_1 = x^2 - 2x - 8 \quad \text{BIG}$$

$$\text{vertex} = (1, -9)$$

$$y\text{-intercept} = (0, -8)$$

$$x\text{-intercepts} = (-2, 0) \text{ and } (4, 0)$$

$$\text{other point} = (2, -8)$$

(exponential growth)

