

Student: _____
Date: _____

Instructor: Alfredo Alvarez
Course: 2413 Cal I

Assignment:
calmath2413alvarez145nextp

1. The function $s(t)$ represents the position of an object at time t moving along a line. Suppose $s(1) = 114$ and $s(6) = 254$. Find the average velocity of the object over the interval of time $[1, 6]$.

The average velocity over the interval $[1, 6]$ is $v_{av} =$. (Simplify your answer.)

Answer: 28

2. The position of an object moving along a line is given by the function $s(t) = -8t^2 + 80t$. Find the average velocity of the object over the following intervals.

(a) $[1, 4]$

(b) $[1, 3]$

(c) $[1, 2]$

(d) $[1, 1 + h]$ where $h > 0$ is any real number.

(a) The average velocity of the object over the interval $[1, 4]$ is .

(b) The average velocity of the object over the interval $[1, 3]$ is .

(c) The average velocity of the object over the interval $[1, 2]$ is .

(d) The average velocity of the object over the interval $[1, 1 + h]$ is .

Answers 40

48

56

$-8h + 64$

3. For the position function $s(t) = -16t^2 + 102t$, complete the following table with the appropriate average velocities. Then make a conjecture about the value of the instantaneous velocity at $t = 1$.

Time Interval	[1, 2]	[1, 1.5]	[1, 1.1]	[1, 1.01]	[1, 1.001]
Average Velocity	_____	_____	_____	_____	_____

Complete the following table.

Time Interval	[1, 2]	[1, 1.5]	[1, 1.1]	[1, 1.01]	[1, 1.001]
Average Velocity					

(Type exact answers. Type integers or decimals.)

The value of the instantaneous velocity at $t = 1$ is .

(Round to the nearest integer as needed.)

Answers 54

62

68.4

69.84

69.984

70

4. For the function $f(x) = 8x^3 - x$, make a table of slopes of secant lines and make a conjecture about the slope of the tangent line at $x = 1$.

Complete the table.

(Round the final answer to three decimal places as needed. Round all intermediate values to four decimal places as needed.)

Interval	Slope of secant line
[1, 2]	
[1, 1.5]	
[1, 1.1]	
[1, 1.01]	
[1, 1.001]	

An accurate conjecture for the slope of the tangent line at $x = 1$ is .

(Round to the nearest integer as needed.)

Answers 55.000

37.000

25.480

23.240

23.000

23

5.

Let $f(x) = \frac{x^2 - 4}{x + 2}$. **(a)** Calculate $f(x)$ for each value of x in the following table. **(b)** Make a conjecture about the value of

$$\lim_{x \rightarrow -2} \frac{x^2 - 4}{x + 2}.$$

(a) Calculate $f(x)$ for each value of x in the following table.

x	- 1.9	- 1.99	- 1.999	- 1.9999
$f(x) = \frac{x^2 - 4}{x + 2}$				
x	- 2.1	- 2.01	- 2.001	- 2.0001
$f(x) = \frac{x^2 - 4}{x + 2}$				

(Type an integer or decimal rounded to four decimal places as needed.)

(b) Make a conjecture about the value of $\lim_{x \rightarrow -2} \frac{x^2 - 4}{x + 2}$.

$$\lim_{x \rightarrow -2} \frac{x^2 - 4}{x + 2} = \boxed{} \text{ (Type an integer or a decimal.)}$$

Answers - 3.9

- 3.99

- 3.999

- 3.9999

- 4.1

- 4.01

- 4.001

- 4.0001

- 4

6. Let $g(t) = \frac{t - 25}{\sqrt{t} - 5}$.

a. Make two tables, one showing the values of g for $t = 24.9, 24.99,$ and 24.999 and one showing values of g for $t = 25.1, 25.01,$ and 25.001 .

b. Make a conjecture about the value of $\lim_{t \rightarrow 25} \frac{t - 25}{\sqrt{t} - 5}$.

a. Make a table showing the values of g for $t = 24.9, 24.99,$ and 24.999 .

t	24.9	24.99	24.999
g(t)			

(Round to four decimal places.)

Make a table showing the values of g for $t = 25.1, 25.01,$ and 25.001 .

t	25.1	25.01	25.001
g(t)			

(Round to four decimal places.)

b. Make a conjecture about the value of $\lim_{t \rightarrow 25} \frac{t - 25}{\sqrt{t} - 5}$. Select the correct choice below and fill in any answer boxes in your choice.

☐ A. $\lim_{t \rightarrow 25} \frac{t - 25}{\sqrt{t} - 5} =$ _____ (Simplify your answer.)

☐ B. The limit does not exist.

Answers

9.9990

9.9999

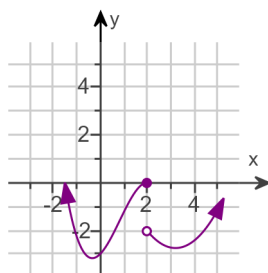
10.0100

10.0010

10.0001

A. $\lim_{t \rightarrow 25} \frac{t - 25}{\sqrt{t} - 5} =$ (Simplify your answer.)

7. Use the graph to find the following limits and function value.



- a. $\lim_{x \rightarrow 2^-} f(x)$
- b. $\lim_{x \rightarrow 2^+} f(x)$
- c. $\lim_{x \rightarrow 2} f(x)$
- d. $f(2)$

a. Find the limit. Select the correct choice below and fill in any answer boxes in your choice.

☐ A. $\lim_{x \rightarrow 2^-} f(x) =$ _____ (Type an integer.)

☐ B. The limit does not exist.

b. Find the limit. Select the correct choice below and fill in any answer boxes in your choice.

☐ A. $\lim_{x \rightarrow 2^+} f(x) =$ _____ (Type an integer.)

☐ B. The limit does not exist.

c. Find the limit. Select the correct choice below and fill in any answer boxes in your choice.

☐ A. $\lim_{x \rightarrow 2} f(x) =$ _____ (Type an integer.)

☐ B. The limit does not exist.

d. Find the function value. Select the correct choice below and fill in any answer boxes in your choice.

☐ A. $f(2) =$ _____ (Type an integer.)

☐ B. The answer is undefined.

Answers A. $\lim_{x \rightarrow 2^-} f(x) =$ (Type an integer.)

A. $\lim_{x \rightarrow 2^+} f(x) =$ (Type an integer.)

B. The limit does not exist.

A. $f(2) =$ (Type an integer.)

8. Explain why $\lim_{x \rightarrow 7} \frac{x^2 - 10x + 21}{x - 7} = \lim_{x \rightarrow 7} (x - 3)$, and then evaluate $\lim_{x \rightarrow 7} \frac{x^2 - 10x + 21}{x - 7}$.

Choose the correct answer below.

- ☐ A. Since each limit approaches 7, it follows that the limits are equal.
- ☐ B. The numerator of the expression $\frac{x^2 - 10x + 21}{x - 7}$ simplifies to $x - 3$ for all x , so the limits are equal.
- ☐ C. The limits $\lim_{x \rightarrow 7} \frac{x^2 - 10x + 21}{x - 7}$ and $\lim_{x \rightarrow 7} (x - 3)$ equal the same number when evaluated using direct substitution.
- ☐ D. Since $\frac{x^2 - 10x + 21}{x - 7} = x - 3$ whenever $x \neq 7$, it follows that the two expressions evaluate to the same number as x approaches 7.

Now evaluate the limit.

$$\lim_{x \rightarrow 7} \frac{x^2 - 10x + 21}{x - 7} = \boxed{} \text{ (Simplify your answer.)}$$

Answers D.

Since $\frac{x^2 - 10x + 21}{x - 7} = x - 3$ whenever $x \neq 7$, it follows that the two expressions evaluate to the same number as x approaches 7.

4

9. Assume $\lim_{x \rightarrow 2} f(x) = 20$ and $\lim_{x \rightarrow 2} h(x) = 2$. Compute the following limit and state the limit laws used to justify the computation.

$$\lim_{x \rightarrow 2} \frac{f(x)}{h(x)}$$

$$\lim_{x \rightarrow 2} \frac{f(x)}{h(x)} = \boxed{} \text{ (Simplify your answer.)}$$

Select each limit law used to justify the computation.

- ☐ A. Difference
☐ B. Root
☐ C. Quotient
☐ D. Product
☐ E. Power
☐ F. Sum
☐ G. Constant multiple

Answers 10

C. Quotient

10. Find the following limit or state that it does not exist.

$$\lim_{x \rightarrow 25} \frac{\sqrt{x} - 5}{x - 25}$$

Simplify the given limit.

$$\lim_{x \rightarrow 25} \frac{\sqrt{x} - 5}{x - 25} = \lim_{x \rightarrow 25} \left(\boxed{} \right) \text{ (Simplify your answer.)}$$

Evaluate the limit, if possible. Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

- ☐ A. $\lim_{x \rightarrow 25} \frac{\sqrt{x} - 5}{x - 25} = \underline{\hspace{2cm}}$ (Type an exact answer.)
☐ B. The limit does not exist.

Answers $\frac{1}{\sqrt{x} + 5}$

$$\text{A. } \lim_{x \rightarrow 25} \frac{\sqrt{x} - 5}{x - 25} = \boxed{\frac{1}{10}} \text{ (Type an exact answer.)}$$

11. Determine the following limit at infinity.

$$\lim_{x \rightarrow \infty} \frac{f(x)}{g(x)} \text{ if } f(x) \rightarrow 200,000 \text{ and } g(x) \rightarrow \infty \text{ as } x \rightarrow \infty$$

Find the limit. Choose the correct answer below.

- ☐ A. $\lim_{x \rightarrow \infty} \frac{f(x)}{g(x)} = \infty$
- ☐ B. $\lim_{x \rightarrow \infty} \frac{f(x)}{g(x)} = 200,000$
- ☐ C. $\lim_{x \rightarrow \infty} \frac{f(x)}{g(x)} = \frac{1}{200,000}$
- ☐ D. $\lim_{x \rightarrow \infty} \frac{f(x)}{g(x)} = 0$

Answer: D. $\lim_{x \rightarrow \infty} \frac{f(x)}{g(x)} = 0$

12. Determine the following limit at infinity.

$$\lim_{x \rightarrow \infty} \frac{8 + 2x + 6x^3}{x^3}$$

Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

- ☐ A. $\lim_{x \rightarrow \infty} \frac{8 + 2x + 6x^3}{x^3} = \underline{\hspace{2cm}}$
- ☐ B. The limit does not exist and is neither $-\infty$ nor ∞ .

Answer: A. $\lim_{x \rightarrow \infty} \frac{8 + 2x + 6x^3}{x^3} = \boxed{6}$

13. Determine the following limit.

$$\lim_{w \rightarrow \infty} \frac{6w^2 + 3w + 5}{\sqrt{4w^4 + 2w^3}}$$

Select the correct choice below, and, if necessary, fill in the answer box to complete your choice.

- ☐ A. $\lim_{w \rightarrow \infty} \frac{6w^2 + 3w + 5}{\sqrt{4w^4 + 2w^3}} = \underline{\hspace{2cm}}$ (Simplify your answer.)
- ☐ B. The limit does not exist and is neither ∞ nor $-\infty$.

Answer: A. $\lim_{w \rightarrow \infty} \frac{6w^2 + 3w + 5}{\sqrt{4w^4 + 2w^3}} = \boxed{3}$ (Simplify your answer.)

14. Determine the following limit.

$$\lim_{x \rightarrow -\infty} \frac{\sqrt{36x^2 + x}}{x}$$

Select the correct choice below, and, if necessary, fill in the answer box to complete your choice.

- ☐ A. $\lim_{x \rightarrow -\infty} \frac{\sqrt{36x^2 + x}}{x} = \underline{\hspace{2cm}}$ (Simplify your answer.)
- ☐ B. The limit does not exist and is neither ∞ nor $-\infty$.

Answer: A. $\lim_{x \rightarrow -\infty} \frac{\sqrt{36x^2 + x}}{x} = \boxed{-6}$ (Simplify your answer.)

15. Determine $\lim_{x \rightarrow \infty} f(x)$ and $\lim_{x \rightarrow -\infty} f(x)$ for the following function. Then give the horizontal asymptotes of f , if any.

$$f(x) = \frac{5x}{35x + 1}$$

Evaluate $\lim_{x \rightarrow \infty} f(x)$. Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

- ☐ A. $\lim_{x \rightarrow \infty} \frac{5x}{35x + 1} = \underline{\hspace{2cm}}$ (Simplify your answer.)
- ☐ B. The limit does not exist and is neither ∞ nor $-\infty$.

Evaluate $\lim_{x \rightarrow -\infty} f(x)$. Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

- ☐ A. $\lim_{x \rightarrow -\infty} \frac{5x}{35x + 1} = \underline{\hspace{2cm}}$ (Simplify your answer.)
- ☐ B. The limit does not exist and is neither ∞ nor $-\infty$.

Give the horizontal asymptotes of f , if any. Select the correct choice below and, if necessary, fill in the answer box(es) to complete your choice.

- ☐ A. The function has one horizontal asymptote, $\underline{\hspace{2cm}}$.
(Type an equation.)
- ☐ B. The function has two horizontal asymptotes. The top asymptote is $\underline{\hspace{2cm}}$ and the bottom asymptote is $\underline{\hspace{2cm}}$.
(Type equations.)
- ☐ C. The function has no horizontal asymptotes.

Answers A. $\lim_{x \rightarrow \infty} \frac{5x}{35x + 1} = \boxed{\frac{1}{7}}$ (Simplify your answer.)

A. $\lim_{x \rightarrow -\infty} \frac{5x}{35x + 1} = \boxed{\frac{1}{7}}$ (Simplify your answer.)

A. The function has one horizontal asymptote, $\boxed{y = \frac{1}{7}}$. (Type an equation.)

16. Evaluate $\lim_{x \rightarrow \infty} f(x)$ and $\lim_{x \rightarrow -\infty} f(x)$ for the following rational function. Use ∞ or $-\infty$ where appropriate. Then give the horizontal asymptote of f (if any).

$$f(x) = \frac{4x^2 - 9x + 8}{2x^2 + 1}$$

Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

- ☐ A. $\lim_{x \rightarrow \infty} f(x) =$ _____ (Simplify your answer.)
- ☐ B. The limit does not exist and is neither ∞ nor $-\infty$.

Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

- ☐ A. $\lim_{x \rightarrow -\infty} f(x) =$ _____ (Simplify your answer.)
- ☐ B. The limit does not exist and is neither ∞ nor $-\infty$.

Identify the horizontal asymptote. Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

- ☐ A. The horizontal asymptote is $y =$ _____.
- ☐ B. There are no horizontal asymptotes.

Answers A. $\lim_{x \rightarrow \infty} f(x) =$ (Simplify your answer.)

A. $\lim_{x \rightarrow -\infty} f(x) =$ (Simplify your answer.)

A. The horizontal asymptote is $y =$.

17. Evaluate $\lim_{x \rightarrow \infty} f(x)$ and $\lim_{x \rightarrow -\infty} f(x)$ for the rational function. Then give the horizontal asymptote of f (if any).

$$f(x) = \frac{28x^8 - 5}{4x^8 - 7x^7}$$

Select the correct choice below, and, if necessary, fill in the answer box to complete your choice.

☐ A. $\lim_{x \rightarrow -\infty} \frac{28x^8 - 5}{4x^8 - 7x^7} = \underline{\hspace{2cm}}$ (Simplify your answer.)

- ☐ B. The limit does not exist and is neither ∞ or $-\infty$.

Select the correct choice below, and, if necessary, fill in the answer box to complete your choice.

☐ A. $\lim_{x \rightarrow \infty} \frac{28x^8 - 5}{4x^8 - 7x^7} = \underline{\hspace{2cm}}$ (Simplify your answer.)

- ☐ B. The limit does not exist and is neither ∞ or $-\infty$.

Select the correct choice below, and, if necessary, fill in the answer box to complete your choice.

- ☐ A. The function has a horizontal asymptote at $y = \underline{\hspace{2cm}}$.
(Simplify your answer.)

- ☐ B. The function has no horizontal asymptote.

Answers A. $\lim_{x \rightarrow -\infty} \frac{28x^8 - 5}{4x^8 - 7x^7} = \boxed{7}$ (Simplify your answer.)

A. $\lim_{x \rightarrow \infty} \frac{28x^8 - 5}{4x^8 - 7x^7} = \boxed{7}$ (Simplify your answer.)

A. The function has a horizontal asymptote at $y = \boxed{7}$. (Simplify your answer.)

18. Determine $\lim_{x \rightarrow \infty} f(x)$ and $\lim_{x \rightarrow -\infty} f(x)$ for the following function. Then give the horizontal asymptotes of f , if any.

$$f(x) = \frac{2x^5 - 9}{x^6 + 4x^4}$$

Evaluate $\lim_{x \rightarrow \infty} f(x)$. Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

☐ A. $\lim_{x \rightarrow \infty} \frac{2x^5 - 9}{x^6 + 4x^4} = \underline{\hspace{2cm}}$ (Simplify your answer.)

☐ B. The limit does not exist and is neither ∞ nor $-\infty$.

Evaluate $\lim_{x \rightarrow -\infty} f(x)$. Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

☐ A. $\lim_{x \rightarrow -\infty} \frac{2x^5 - 9}{x^6 + 4x^4} = \underline{\hspace{2cm}}$ (Simplify your answer.)

☐ B. The limit does not exist and is neither ∞ nor $-\infty$.

Identify the horizontal asymptotes. Select the correct choice below and, if necessary, fill in the answer box(es) to complete your choice.

☐ A. The function has one horizontal asymptote, $\underline{\hspace{2cm}}$.
(Type an equation.)

☐ B. The function has two horizontal asymptotes. The top asymptote is $\underline{\hspace{2cm}}$ and the bottom asymptote is $\underline{\hspace{2cm}}$.
(Type equations.)

☐ C. The function has no horizontal asymptotes.

Answers A. $\lim_{x \rightarrow \infty} \frac{2x^5 - 9}{x^6 + 4x^4} = \boxed{0}$ (Simplify your answer.)

A. $\lim_{x \rightarrow -\infty} \frac{2x^5 - 9}{x^6 + 4x^4} = \boxed{0}$ (Simplify your answer.)

A. The function has one horizontal asymptote, $\boxed{y = 0}$. (Type an equation.)

19. Find all the asymptotes of the function.

$$f(x) = \frac{8x^2 + 16}{2x^2 + 9x - 5}$$

Find the horizontal asymptotes. Select the correct choice below and, if necessary, fill in the answer box(es) to complete your choice.

- ☐ A. The function has one horizontal asymptote, _____.
(Type an equation using y as the variable.)
- ☐ B. The function has two horizontal asymptotes. The top asymptote is _____ and the bottom asymptote is _____.
(Type equations using y as the variable.)
- ☐ C. The function has no horizontal asymptotes.

Find the vertical asymptotes. Select the correct choice below and, if necessary, fill in the answer box(es) to complete your choice.

- ☐ A. The function has one vertical asymptote, _____.
(Type an equation using x as the variable.)
- ☐ B. The function has two vertical asymptotes. The leftmost asymptote is _____ and the rightmost asymptote is _____.
(Type equations using x as the variable.)
- ☐ C. The function has no vertical asymptotes.

Find the slant asymptote(s). Select the correct choice below and, if necessary, fill in the answer box(es) to complete your choice.

- ☐ A. The function has one slant asymptote, _____.
(Type an equation using x and y as the variables.)
- ☐ B. The function has two slant asymptotes. The asymptote with the larger slope is _____ and the asymptote with the smaller slope is _____.
(Type equations using x and y as the variables.)
- ☐ C. The function has no slant asymptotes.

Answers A. The function has one horizontal asymptote, . (Type an equation using y as the variable.)

B.

The function has two vertical asymptotes. The leftmost asymptote is and the rightmost

asymptote is .

(Type equations using x as the variable.)

C. The function has no slant asymptotes.

20. Determine whether the following function is continuous at a . Use the continuity checklist to justify your answer.

$$f(x) = \frac{5x^2 + 16x + 3}{x^2 + 7x}, a = -7$$

Select all that apply.

- ☐ A. The function is continuous at $a = -7$.
- ☐ B. The function is not continuous at $a = -7$ because $f(-7)$ is undefined.
- ☐ C. The function is not continuous at $a = -7$ because $\lim_{x \rightarrow -7} f(x)$ does not exist.
- ☐ D. The function is not continuous at $a = -7$ because $\lim_{x \rightarrow -7} f(x) \neq f(-7)$.

Answer: B. The function is not continuous at $a = -7$ because $f(-7)$ is undefined. , C.

The function is not continuous at $a = -7$ because $\lim_{x \rightarrow -7} f(x)$ does not exist. , D.

The function is not continuous at $a = -7$ because $\lim_{x \rightarrow -7} f(x) \neq f(-7)$.

21. Determine whether the following function is continuous at a . Use the continuity checklist to justify your answer.

$$f(x) = \begin{cases} \frac{x^2 - 196}{x - 14} & \text{if } x \neq 14 \\ 1 & \text{if } x = 14 \end{cases}; a = 14$$

Select all that apply.

- ☐ A. The function is continuous at $a = 14$.
- ☐ B. The function is not continuous at $a = 14$ because $f(14)$ is undefined.
- ☐ C. The function is not continuous at $a = 14$ because $\lim_{x \rightarrow 14} f(x)$ does not exist.
- ☐ D. The function is not continuous at $a = 14$ because $\lim_{x \rightarrow 14} f(x) \neq f(14)$.

Answer: D. The function is not continuous at $a = 14$ because $\lim_{x \rightarrow 14} f(x) \neq f(14)$.

22. Determine the intervals on which the following function is continuous.

$$f(x) = \frac{x^2 - 6x + 8}{x^2 - 16}$$

On what interval(s) is f continuous?

(Simplify your answer. Type your answer in interval notation. Use a comma to separate answers as needed.)

Answer: $(-\infty, -4), (-4, 4), (4, \infty)$

23. Evaluate the following limit.

$$\lim_{x \rightarrow 4} \sqrt{x^2 + 9}$$

Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

- ☐ A. $\lim_{x \rightarrow 4} \sqrt{x^2 + 9} =$ _____, because $x^2 + 9$ is continuous for all x and the square root function is continuous for all $x \geq 0$.
(Type an integer or a fraction.)
- ☐ B. The limit does not exist and is neither ∞ nor $-\infty$.

Answer: A.

$$\lim_{x \rightarrow 4} \sqrt{x^2 + 9} = \boxed{5}, \text{ because } x^2 + 9 \text{ is continuous for all } x \text{ and the square root function is continuous for all } x \geq 0.$$

(Type an integer or a fraction.)

24. Suppose x lies in the interval $(3, 7)$ with $x \neq 5$. Find the smallest positive value of δ such that the inequality $0 < |x - 5| < \delta$ is true for all possible values of x .

The smallest positive value of δ is . (Type an integer or a fraction.)

Answer: 2

25. Suppose $|f(x) - 7| < 0.3$ whenever $0 < x < 7$. Find all values of $\delta > 0$ such that $|f(x) - 7| < 0.3$ whenever $0 < |x - 2| < \delta$.

The values of δ are $0 < \delta \leq$. (Type an integer or a fraction.)

Answer: 2

26.

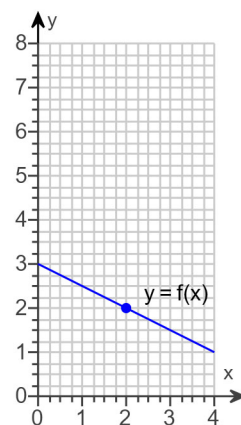
The function f in the figure satisfies $\lim_{x \rightarrow 2} f(x) = 2$. Determine the largest value of $\delta > 0$ satisfying each statement.

a. If $0 < |x - 2| < \delta$, then $|f(x) - 2| < \frac{1}{2}$.

b. If $0 < |x - 2| < \delta$, then $|f(x) - 2| < \frac{1}{4}$.

a. $\delta =$ (Simplify your answer.)

b. $\delta =$ (Simplify your answer.)



Answers 1

$$\frac{1}{2}$$

27. Use the precise definition of a limit to prove the following limit. Specify a relationship between ε and δ that guarantees the limit exists.

$$\lim_{x \rightarrow 0} (4x + 2) = 2$$

Let $\varepsilon > 0$ be given. Choose the correct proof below.

- ☐ A. Choose $\delta = \varepsilon$. Then, $|(4x + 2) - 2| < \varepsilon$ whenever $0 < |x - 0| < \delta$.
- ☐ B. Choose $\delta = \frac{\varepsilon}{4}$. Then, $|(4x + 2) - 2| < \varepsilon$ whenever $0 < |x - 0| < \delta$.
- ☐ C. Choose $\delta = 4\varepsilon$. Then, $|(4x + 2) - 2| < \varepsilon$ whenever $0 < |x - 0| < \delta$.
- ☐ D. Choose $\delta = \frac{\varepsilon}{2}$. Then, $|(4x + 2) - 2| < \varepsilon$ whenever $0 < |x - 0| < \delta$.
- ☐ E. None of the above proofs is correct.

Answer:

B. Choose $\delta = \frac{\varepsilon}{4}$. Then, $|(4x + 2) - 2| < \varepsilon$ whenever $0 < |x - 0| < \delta$.

28. Find the average velocity of the function over the given interval.

$$y = \frac{3}{x-2}, [4, 7]$$

- ☐ A. $\frac{1}{3}$
- ☐ B. 2
- ☐ C. 7
- ☐ D. $-\frac{3}{10}$

Answer: D. $-\frac{3}{10}$

29. Find all vertical asymptotes of the given function.

$$g(x) = \frac{x+11}{x^2-49x}$$

- ☐ A. $x=0, x=-7, x=7$
- ☐ B. $x=-7, x=7$
- ☐ C. $x=49, x=-11$
- ☐ D. $x=0, x=49$

Answer: D. $x=0, x=49$

30. Divide numerator and denominator by the highest power of x in the denominator to find the limit at infinity.

$$\lim_{x \rightarrow \infty} \frac{\sqrt[3]{x} - 4x + 3}{-2x + x^{2/3} + 7}$$

- ☐ A. 2
- ☐ B. 0
- ☐ C. $\frac{1}{2}$
- ☐ D. $-\infty$

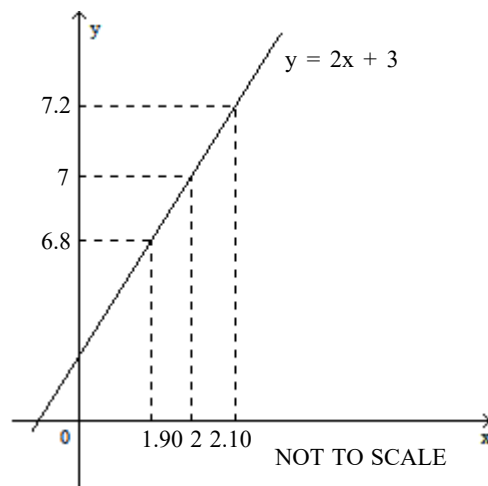
Answer: A. 2

31. Use the graph to find a $\delta > 0$ such that for all x , $0 < |x - x_0| < \delta$ and $|f(x) - L| < \varepsilon$. Use the following information:
 $f(x) = 2x + 3$, $\varepsilon = 0.2$, $x_0 = 2$, $L = 7$.

¹ Click the icon to view the graph.

- ☐ A. 0.2
☐ B. 5
☐ C. 0.4
☐ D. 0.1

1: Graph



Answer: D. 0.1

32. Find the value of the derivative of the function at the given point.

$$f(x) = 4x^2 - 2x; (-1, 6)$$

$f'(-1) =$ (Type an integer or a simplified fraction.)

Answer: -10

33. **a.** Use the definition $m_{\tan} = \lim_{h \rightarrow 0} \frac{f(a+h) - f(a)}{h}$ to find the slope of the line tangent to the graph of f at P .
b. Determine an equation of the tangent line at P .

$$f(x) = x^2 - 4, P(-5, 21)$$

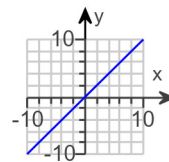
a. $m_{\tan} =$

b. $y =$

Answers -10

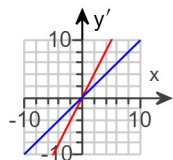
$$-10x - 29$$

34. Match the graph of the function on the right with the graph of its derivative.

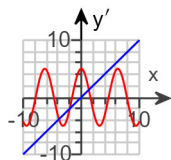


Choose the correct graph of the function (in blue) and its derivative (in red) below.

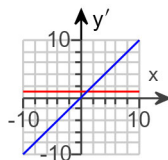
☐ A.



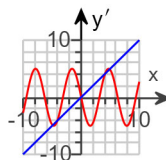
☐ B.



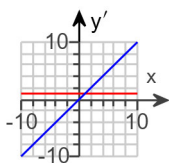
☐ C.



☐ D.



Answer:



C.

35. A line perpendicular to another line or to a tangent line is called a normal line. Find an equation of the line perpendicular to the line that is tangent to the following curve at the given point P.

$$y = 5x + 7; P(-1, 2)$$

The equation of the normal line at P(-1, 2) is .

Answer: $y = -\frac{1}{5}x + \frac{9}{5}$

36. Evaluate the derivative of the function given below using a limit definition of the derivative.

$$f(x) = x^2 + 3x - 8$$

$f'(x) =$

Answer: $2x + 3$

37. Use the Quotient Rule to evaluate and simplify $\frac{d}{dx} \left(\frac{x-1}{4x-5} \right)$.

$$\frac{d}{dx} \left(\frac{x-1}{4x-5} \right) = \boxed{}$$

Answer: $-\frac{1}{(4x-5)^2}$

38. Use the Quotient Rule to find $g'(1)$ given that $g(x) = \frac{2x^2}{3x+2}$.

$$g'(1) = \boxed{}$$

(Simplify your answer.)

Answer: $\frac{14}{25}$

39. **a.** Use the Product Rule to find the derivative of the given function.
b. Find the derivative by expanding the product first.

$$f(x) = (x-3)(5x+3)$$

a. Use the product rule to find the derivative of the function. Select the correct answer below and fill in the answer box(es) to complete your choice.

- ☐ **A.** The derivative is $(x-3)() + (5x+3)()$.
- ☐ **B.** The derivative is $(x-3)(5x+3) + ()$.
- ☐ **C.** The derivative is $()(x-3)$.
- ☐ **D.** The derivative is $(x-3)(5x+3)()$.
- ☐ **E.** The derivative is $()x(5x+3)$.

b. Expand the product.

$$(x-3)(5x+3) = \boxed{} \text{ (Simplify your answer.)}$$

Using either approach, $\frac{d}{dx}(x-3)(5x+3) = \boxed{}$.

Answers **A.** The derivative is $(x-3)(\boxed{5}) + (5x+3)(\boxed{1})$.

$$5x^2 - 12x - 9$$

$$10x - 12$$

40. Use the quotient rule to find the derivative of the given function. Then find the derivative by first simplifying the function. Are the results the same?

$$h(w) = \frac{3w^4 - w}{w}$$

What is the immediate result of applying the quotient rule? Select the correct answer below.

- ☐ A. $\frac{w(12w^3 - 1) - (3w^4 - w)(1)}{w^2}$
- ☐ B. $(12w^3 - 1)(w) + (3w^4 - w)(1)$
- ☐ C. $3w^3 - 1$
- ☐ D. $9w^2$

What is the fully simplified result of applying the quotient rule?

What is the result of first simplifying the function, then taking the derivative? Select the correct answer below.

- ☐ A. $\frac{w(12w^3 - 1) - (3w^4 - w)(1)}{w^2}$
- ☐ B. $(12w^3 - 1)(w) + (3w^4 - w)(1)$
- ☐ C. $3w^3 - 1$
- ☐ D. $9w^2$

Are the two results the same?

- ☐ No
- ☐ Yes

Answers

A. $\frac{w(12w^3 - 1) - (3w^4 - w)(1)}{w^2}$

$$9w^2$$

D. $9w^2$

Yes

41. If $f(x) = \sin x$, then what is the value of $f'\left(\frac{\pi}{2}\right)$?

$f'\left(\frac{\pi}{2}\right) =$ (Simplify your answer.)

Answer: 0

42. Evaluate the limit.

$$\lim_{x \rightarrow 0} \frac{\sin 6x}{\sin 5x}$$

Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

- ☐ A. $\lim_{x \rightarrow 0} \frac{\sin 6x}{\sin 5x} = \underline{\hspace{2cm}}$
- ☐ B. The limit is undefined.

Answer: A. $\lim_{x \rightarrow 0} \frac{\sin 6x}{\sin 5x} = \boxed{\frac{6}{5}}$

43. Find $\frac{dy}{dx}$ for the following function.

$$y = 2 \sin x + 8 \cos x$$

$$\frac{dy}{dx} = \boxed{\hspace{2cm}}$$

Answer: $2 \cos x - 8 \sin x$

44. Find the derivative of the following function.

$$y = e^{-x} \sin x$$

$$\frac{dy}{dx} = \boxed{\hspace{2cm}}$$

Answer: $e^{-x}(\cos x - \sin x)$

45. Find an equation of the line tangent to the following curve at the given point.

$$y = -15x^2 + 8 \sin x; P(0,0)$$

The equation for the tangent line is $\boxed{\hspace{2cm}}$.

Answer: $y = 8x$

46.

Let $h(x) = f(g(x))$ and $p(x) = g(f(x))$. Use the table below to compute the following derivatives.

a. $h'(2)$ b. $p'(4)$

x	1	2	3	4
$f(x)$	1	2	3	4
$f'(x)$	-5	-2	-3	-7
$g(x)$	2	1	4	3
$g'(x)$	$\frac{1}{7}$	$\frac{5}{7}$	$\frac{6}{7}$	$\frac{4}{7}$

Answers $-\frac{25}{7}$

-4

$h'(2) =$ (Simplify your answer.)

$p'(4) =$ (Simplify your answer.)

47. Calculate the derivative of the following function.

$$y = (4x + 9)^8$$

$$\frac{dy}{dx} =$$

Answer: $32(4x + 9)^7$

48. Calculate the derivative of the following function.

$$y = 8(8x^2 + 1)^{-2}$$

$$\frac{dy}{dx} =$$

Answer: $\frac{-256x}{(8x^2 + 1)^3}$

49. Calculate the derivative of the following function.

$$y = \sin(13t + 20)$$

$$\frac{dy}{dt} =$$

Answer: $13 \cos(13t + 20)$

50. Calculate the derivative of the following function.

$$y = \tan(e^x)$$

$$\frac{dy}{dx} = \boxed{}$$

Answer: $e^x \sec^2 e^x$

51. Calculate the derivative of the following function.

$$y = \sin(9 \cos x)$$

$$\frac{dy}{dx} = \boxed{}$$

Answer: $-9 \cos(9 \cos x) \cdot \sin x$

52. Calculate $\frac{dy}{dx}$ using implicit differentiation.

$$2x = y^2$$

$$\frac{dy}{dx} = \boxed{}$$

Answer: $\frac{1}{y}$

53. Calculate $\frac{dy}{dx}$ using implicit differentiation.

$$\cos(y) + 10 = x$$

$$\frac{dy}{dx} = \boxed{}$$

Answer: $-\csc y$

54.

Consider the curve $x = y^{19}$. Use implicit differentiation to verify that $\frac{dy}{dx} = \frac{1}{19y^{18}}$ and then find $\frac{d^2y}{dx^2}$.

Use implicit differentiation to find the derivative of each side of the equation.

$$\frac{d}{dx}x = \boxed{} \text{ and } \frac{d}{dx}y^{19} = \boxed{} \frac{dy}{dx}$$

Solve for $\frac{dy}{dx}$.

$$\frac{dy}{dx} = \boxed{}$$

Find $\frac{d^2y}{dx^2}$.

$$\frac{d^2y}{dx^2} = \boxed{}$$

Answers 1

$$\begin{aligned} &19y^{18} \\ &\frac{1}{19y^{18}} \\ &-\frac{18}{361y^{37}} \end{aligned}$$

55. Carry out the following steps for the given curve.

a. Use implicit differentiation to find $\frac{dy}{dx}$.

b. Find the slope of the curve at the given point.

$$x^3 + y^3 = 19; (-2, 3)$$

a. Use implicit differentiation to find $\frac{dy}{dx}$.

$$\frac{dy}{dx} = \boxed{}$$

b. Find the slope of the curve at the given point.

The slope of $x^3 + y^3 = 19$ at $(-2, 3)$ is $\boxed{}$.
(Simplify your answer.)

Answers $-\frac{x^2}{y^2}$
 $-\frac{4}{9}$

56. Use implicit differentiation to find $\frac{dy}{dx}$.

$$\sin(y) + \cos(x) = 5y$$

$$\frac{dy}{dx} = \boxed{}$$

Answer: $-\frac{\sin x}{5 - \cos y}$

57. Use implicit differentiation to find $\frac{dy}{dx}$.

$$4 \sin(xy) = 7x + 9y$$

$$\frac{dy}{dx} = \boxed{}$$

Answer: $\frac{7 - 4y \cos(xy)}{4x \cos(xy) - 9}$

58. Use implicit differentiation to find $\frac{dy}{dx}$.

$$e^{3xy} = 4y$$

$$\frac{dy}{dx} = \boxed{}$$

Answer: $\frac{3y e^{3xy}}{4 - 3x e^{3xy}}$

59. Use implicit differentiation to find $\frac{dy}{dx}$ for the following equation.

$$5x^4 + 8y^4 = 13xy$$

$$\frac{dy}{dx} = \boxed{}$$

Answer: $\frac{20x^3 - 13y}{13x - 32y^3}$

60. Find $\frac{d}{dx} (\ln \sqrt{x^2 + 1})$.

$$\frac{d}{dx} (\ln \sqrt{x^2 + 1}) = \boxed{}$$

Answer: $\frac{x}{x^2 + 1}$

61. Express the function $f(x) = g(x)^{h(x)}$ in terms of the natural logarithmic and natural exponential functions (base e).

$$f(x) = \boxed{}$$

Answer: $e^{h(x) \ln g(x)}$

62. Find the derivative.

$$\frac{d}{dx} (\ln (5x^2 + 2))$$

$$\frac{d}{dx} (\ln (5x^2 + 2)) = \boxed{}$$

Answer: $\frac{10x}{5x^2 + 2}$

63. Evaluate the derivative.

$$y = 4x^{2\pi}$$

$$y' = \boxed{} \text{ (Type an exact answer.)}$$

Answer: $8\pi x^{(2\pi - 1)}$

64. Find $\frac{dy}{dx}$ for the function $y = 2^x$.

$$\frac{dy}{dx} = \boxed{}$$

Answer: $2^x \ln 2$

65. Calculate the derivative of the following function.

$$y = 3 \log_2 (x^3 - 8)$$

$$\frac{d}{dx} 3 \log_2 (x^3 - 8) = \boxed{}$$

Answer: $\frac{9x^2}{(x^3 - 8) \ln 2}$

66. Use logarithmic differentiation to evaluate $f'(x)$.

$$f(x) = \frac{(x+3)^{12}}{(3x-6)^{10}}$$

$$f'(x) = \boxed{}$$

Answer: $\frac{(x+3)^{12}}{(3x-6)^{10}} \left[\frac{12}{x+3} - \frac{10}{x-2} \right]$

67. State the derivative formulas for $\sin^{-1}x$, $\tan^{-1}x$, and $\sec^{-1}x$.

What is the derivative of $\sin^{-1}x$?

- ☐ A. $-\frac{1}{|x|\sqrt{x^2-1}}$ for $|x| > 1$
- ☐ B. $\frac{1}{\sqrt{1-x^2}}$ for $-1 < x < 1$
- ☐ C. $\frac{1}{|x|\sqrt{x^2-1}}$ for $|x| > 1$
- ☐ D. $-\frac{1}{\sqrt{1-x^2}}$ for $-1 < x < 1$

What is the derivative of $\tan^{-1}x$?

- ☐ A. $-\frac{1}{1+x^2}$ for $-\infty < x < \infty$
- ☐ B. $\frac{1}{1+x^2}$ for $-\infty < x < \infty$
- ☐ C. $-\frac{1}{|x|\sqrt{x^2-1}}$ for $|x| > 1$
- ☐ D. $-\frac{1}{\sqrt{1-x^2}}$ for $-1 < x < 1$

What is the derivative of $\sec^{-1}x$?

- ☐ A. $-\frac{1}{|x|\sqrt{x^2-1}}$ for $|x| > 1$
- ☐ B. $\frac{1}{\sqrt{1-x^2}}$ for $-1 < x < 1$
- ☐ C. $\frac{1}{|x|\sqrt{x^2-1}}$ for $|x| > 1$
- ☐ D. $-\frac{1}{\sqrt{1-x^2}}$ for $-1 < x < 1$

Answers B. $\frac{1}{\sqrt{1-x^2}}$ for $-1 < x < 1$

B. $\frac{1}{1+x^2}$ for $-\infty < x < \infty$

C. $\frac{1}{|x|\sqrt{x^2-1}}$ for $|x| > 1$

68. Evaluate the derivative of the function.

$$f(x) = \sin^{-1}(4x^4)$$

$$f'(x) = \boxed{}$$

Answer: $\frac{16x^3}{\sqrt{1-16x^8}}$

69. Find the derivative of the function $y = 6 \tan^{-1}(3x)$.

$$\frac{dy}{dx} = \boxed{}$$

Answer: $\frac{18}{1+(3x)^2}$

70. Evaluate the derivative of the following function.

$$f(s) = \cot^{-1}(e^s)$$

$$\frac{d}{ds} \cot^{-1}(e^s) = \boxed{}$$

Answer: $-\frac{e^s}{1+e^{2s}}$

71. The sides of a square increase in length at a rate of 4 m/sec.

- a. At what rate is the area of the square changing when the sides are 11 m long?
 b. At what rate is the area of the square changing when the sides are 25 m long?

a. Write an equation relating the area of a square, A , and the side length of the square, s .

Differentiate both sides of the equation with respect to t .

$$\frac{dA}{dt} = \left(\frac{\quad}{\quad} \right) \frac{ds}{dt}$$

The area of the square is changing at a rate of (1) when the sides are 11 m long.

b. The area of the square is changing at a rate of (2) when the sides are 25 m long.

- (1) ☐ m^3/s (2) ☐ m^2/s
☐ m/s ☐ m^3/s
☐ m ☐ m
☐ m^2/s ☐ m/s

Answers $A = s^2$

$2s$

88

(1) m^2/s

200

(2) m^2/s

72. The area of a circle increases at a rate of $2 \text{ cm}^2 / \text{s}$.

- a. How fast is the radius changing when the radius is 3 cm?
 b. How fast is the radius changing when the circumference is 1 cm?

a. Write an equation relating the area of a circle, A , and the radius of the circle, r .

(Type an exact answer, using π as needed.)

Differentiate both sides of the equation with respect to t .

$$\frac{dA}{dt} = \left(\frac{\quad}{\quad} \right) \frac{dr}{dt}$$

(Type an exact answer, using π as needed.)

When the radius is 3 cm, the radius is changing at a rate of (1)
 (Type an exact answer, using π as needed.)

b. When the circumference is 1 cm, the radius is changing at a rate of (2)
 (Type an exact answer, using π as needed.)

- | | |
|--|--|
| (1) ☐ cm^2 / s . | (2) ☐ cm / s . |
| ☐ cm . | ☐ cm^2 / s . |
| ☐ cm / s . | ☐ cm . |
| ☐ cm^3 / s . | ☐ cm^3 / s . |

Answers $A = \pi r^2$

$$2\pi r$$

$$\frac{1}{3\pi}$$

(1) cm / s .

$$2$$

(2) cm / s .

73. The edges of a cube increase at a rate of 3 cm / s. How fast is the volume changing when the length of each edge is 50 cm?

Write an equation relating the volume of a cube, V , and an edge of the cube, a .

Differentiate both sides of the equation with respect to t .

$$\frac{dV}{dt} = \left(\text{ } \right) \frac{da}{dt} \text{ (Type an expression using } a \text{ as the variable.)}$$

The rate of change of the volume is (1)
(Simplify your answer.)

- (1) ☐ cm. ☐ cm^3 .
☐ $\text{cm}^2 / \text{sec.}$ ☐ cm / sec.
☐ cm^2 .
☐ $\text{cm}^3 / \text{sec.}$

Answers $V = a^3$

$$3a^2$$

$$22,500$$

$$(1) \text{ cm}^3 / \text{sec.}$$

74. Find an equation for the tangent to the curve at the given point.

$$y = x^2 - 2, (2, 2)$$

- ☐ A. $y = 4x - 12$
☐ B. $y = 4x - 10$
☐ C. $y = 2x - 6$
☐ D. $y = 4x - 6$

Answer: D. $y = 4x - 6$

75. At time t , the position of a body moving along the s -axis is $s = t^3 - 18t^2 + 60t$ m. Find the displacement of the body from $t = 0$ to $t = 3$.

- ☐ A. 105 m
☐ B. 56 m
☐ C. 67 m
☐ D. 45 m

Answer: D. 45 m

76. Use implicit differentiation to find dy/dx .

$$xy + x = 2$$

- ☐ A. $\frac{1+y}{x}$
- ☐ B. $\frac{1+x}{y}$
- ☐ C. $-\frac{1+x}{y}$
- ☐ D. $-\frac{1+y}{x}$

Answer: D. $-\frac{1+y}{x}$

77. Find the derivative of the function.

$$y = \log_7 \sqrt{3x+6}$$

- ☐ A. $\frac{3}{\ln 7}$
- ☐ B. $\frac{3}{2(\ln 7)(3x+6)}$
- ☐ C. $\frac{3}{\ln 7 (3x+6)}$
- ☐ D. $\frac{3 \ln 7}{3x+6}$

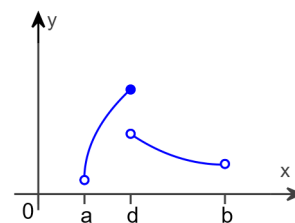
Answer: B. $\frac{3}{2(\ln 7)(3x+6)}$

78. Boyle's law states that if the temperature of a gas remains constant, then $PV = c$, where P = pressure, V = volume, and c is a constant. Given a quantity of gas at constant temperature, if V is decreasing at a rate of $9 \text{ in}^3/\text{sec}$, at what rate is P increasing when $P = 70 \text{ lb/in}^2$ and $V = 90 \text{ in}^3$? (Do not round your answer.)

- ☐ A. $7 \text{ lb / in}^2 \text{ per sec}$
- ☐ B. $\frac{81}{7} \text{ lb / in}^2 \text{ per sec}$
- ☐ C. $700 \text{ lb / in}^2 \text{ per sec}$
- ☐ D. $\frac{49}{81} \text{ lb / in}^2 \text{ per sec}$

Answer: A. $7 \text{ lb / in}^2 \text{ per sec}$

79. Determine from the graph whether the function has any absolute extreme values on $[a, b]$.



Where do the absolute extreme values of the function occur on $[a, b]$?

- ☐ A. There is no absolute maximum and there is no absolute minimum on $[a, b]$.
- ☐ B. The absolute maximum occurs at $x = d$ and the absolute minimum occurs at $x = a$ on $[a, b]$.
- ☐ C. There is no absolute maximum and the absolute minimum occurs at $x = a$ on $[a, b]$.
- ☐ D. The absolute maximum occurs at $x = d$ and there is no absolute minimum on $[a, b]$.

Answer: D. The absolute maximum occurs at $x = d$ and there is no absolute minimum on $[a, b]$.

80. Find the critical points of the following function.

$$f(x) = 3x^2 - 5x + 2$$

What is the derivative of $f(x) = 3x^2 - 5x + 2$?

$$f'(x) = \boxed{}$$

Find the critical points, if any, of f on the domain. Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

- ☐ A. The critical point(s) occur(s) at $x = $.
(Use a comma to separate answers as needed.)
- ☐ B. There are no critical points for $f(x) = 3x^2 - 5x + 2$ on the domain.

Answers $6x - 5$

A. The critical point(s) occur(s) at $x = \boxed{\frac{5}{6}}$. (Use a comma to separate answers as needed.)

81. Find the critical points of the following function.

$$f(x) = -\frac{x^3}{3} + 36x$$

Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

- ☐ A. The critical point(s) occur(s) at $x = $.
(Use a comma to separate answers as needed.)
- ☐ B. There are no critical points.

Answer: A. The critical point(s) occur(s) at $x = \boxed{6, -6}$. (Use a comma to separate answers as needed.)

82. Determine the location and value of the absolute extreme values of f on the given interval, if they exist.

$$f(x) = -x^2 + 8 \text{ on } [-3, 4]$$

What is/are the absolute maximum/maxima of f on the given interval? Select the correct choice below and, if necessary, fill in the answer boxes to complete your choice.

- ☐ A. The absolute maximum/maxima is/are _____ at $x =$ _____.
(Use a comma to separate answers as needed.)
- ☐ B. There is no absolute maximum of f on the given interval.

What is/are the absolute minimum/minima of f on the given interval? Select the correct choice below and, if necessary, fill in the answer boxes to complete your choice.

- ☐ A. The absolute minimum/minima is/are _____ at $x =$ _____.
(Use a comma to separate answers as needed.)
- ☐ B. There is no absolute minimum of f on the given interval.

Answers A. The absolute maximum/maxima is/are at $x =$.

(Use a comma to separate answers as needed.)

A. The absolute minimum/minima is/are at $x =$.

(Use a comma to separate answers as needed.)

83. A stone is launched vertically upward from a cliff 336 ft above the ground at a speed of 64 ft/s. Its height above the ground t seconds after the launch is given by $s = -16t^2 + 64t + 336$ for $0 \leq t \leq 7$. When does the stone reach its maximum height?

Find the derivative of s .

$$s' = \text{$$

The stone reaches its maximum height at s.
(Simplify your answer.)

Answers $-32t + 64$

2

84. Suppose a tour guide has a bus that holds a maximum of 90 people. Assume his profit (in dollars) for taking n people on a city tour is $P(n) = n(45 - 0.5n) - 90$. (Although P is defined only for positive integers, treat it as a continuous function.)

- a. How many people should the guide take on a tour to maximize the profit?
 b. Suppose the bus holds a maximum of 38 people. How many people should be taken on a tour to maximize the profit?

- a. Find the derivative of the given function $P(n)$.

$$P'(n) = \boxed{}$$

If the bus holds a maximum of 90 people, the guide should take $\boxed{}$ people on a tour to maximize the profit.

- b. If the bus holds a maximum of 38 people, the guide should take $\boxed{}$ people on a tour to maximize the profit.

Answers $-n + 45$

45

38

85. At what points c does the conclusion of the Mean Value Theorem hold for $f(x) = x^3$ on the interval $[-8, 8]$?

The conclusion of the Mean Value Theorem holds for $c = \boxed{}$.

(Use a comma to separate answers as needed. Type an exact answer, using radicals as needed.)

$$\text{Answer: } \frac{8\sqrt{3}}{3}, -\frac{8\sqrt{3}}{3}$$

86. a. Determine whether the Mean Value Theorem applies to the function $f(x) = -7 + x^2$ on the interval $[-1, 2]$.
 b. If so, find the point(s) that are guaranteed to exist by the Mean Value Theorem.

- a. Choose the correct answer below.

- ☐ A. No, because the function is not continuous on the interval $[-1, 2]$, and is not differentiable on the interval $(-1, 2)$.
☐ B. No, because the function is differentiable on the interval $(-1, 2)$, but is not continuous on the interval $[-1, 2]$.
☐ C. Yes, because the function is continuous on the interval $[-1, 2]$ and differentiable on the interval $(-1, 2)$.
☐ D. No, because the function is continuous on the interval $[-1, 2]$, but is not differentiable on the interval $(-1, 2)$.

- b. Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

- ☐ A. The point(s) is/are $x = \boxed{}$.
 (Simplify your answer. Use a comma to separate answers as needed.)
☐ B. The Mean Value Theorem does not apply in this case.

Answers C. Yes, because the function is continuous on the interval $[-1, 2]$ and differentiable on the interval $(-1, 2)$.

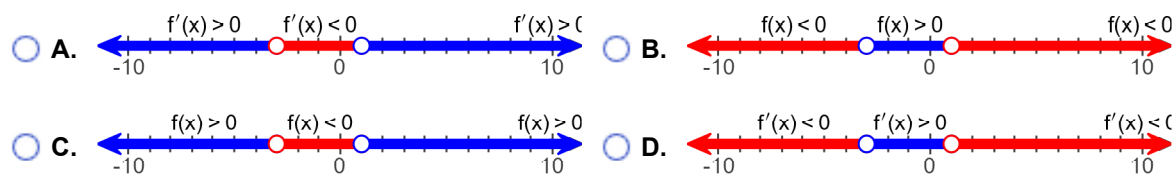
$$\text{A. The point(s) is/are } x = \boxed{\frac{1}{2}}.$$

(Simplify your answer. Use a comma to separate answers as needed.)

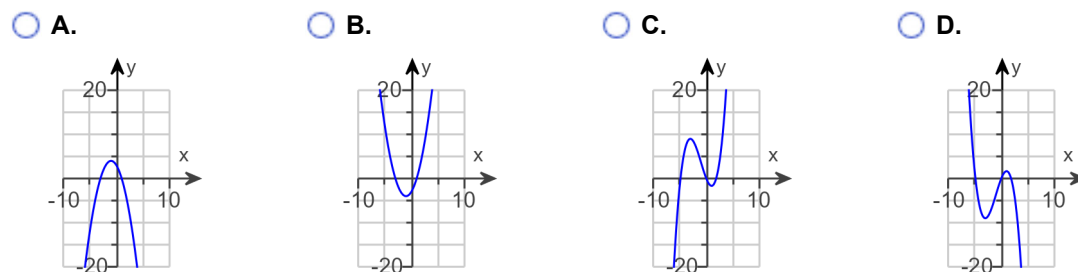
87. Sketch a function that is continuous on $(-\infty, \infty)$ and has the following properties. Use a number line to summarize information about the function.

$$f'(x) < 0 \text{ on } (-\infty, -3); f'(x) > 0 \text{ on } (-3, 1); f'(x) < 0 \text{ on } (1, \infty).$$

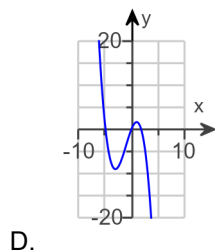
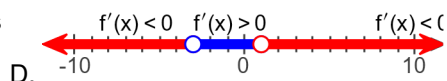
Which number line summarizes the information about the function?



Which of the following graphs matches the description of the given properties?



Answers



88. Find the intervals on which f is increasing and the intervals on which it is decreasing.

$$f(x) = -5 + x^2$$

Select the correct choice below and, if necessary, fill in the answer box(es) to complete your choice.

- ☐ A. The function is increasing on _____ and decreasing on _____.
(Simplify your answers. Type your answers in interval notation. Use a comma to separate answers as needed.)
- ☐ B. The function is decreasing on _____. The function is never increasing.
(Simplify your answer. Type your answer in interval notation. Use a comma to separate answers as needed.)
- ☐ C. The function is increasing on _____. The function is never decreasing.
(Simplify your answer. Type your answer in interval notation. Use a comma to separate answers as needed.)
- ☐ D. The function is never increasing nor decreasing.

Answer: A. The function is increasing on $(0, \infty)$ and decreasing on $(-\infty, 0)$.

(Simplify your answers. Type your answers in interval notation. Use a comma to separate answers as needed.)

89. Find the intervals on which f is increasing and the intervals on which it is decreasing.

$$f(x) = -4 + x - 2x^2$$

Select the correct choice below and, if necessary, fill in the answer box(es) to complete your choice.

- ☐ A. The function is increasing on _____ and decreasing on _____.
(Simplify your answers. Type your answers in interval notation. Use a comma to separate answers as needed.)
- ☐ B. The function is decreasing on _____. The function is never increasing.
(Simplify your answer. Type your answer in interval notation. Use a comma to separate answers as needed.)
- ☐ C. The function is increasing on _____. The function is never decreasing.
(Simplify your answer. Type your answer in interval notation. Use a comma to separate answers as needed.)
- ☐ D. The function is never increasing nor decreasing.

Answer: A. The function is increasing on $\left(-\infty, \frac{1}{4}\right)$ and decreasing on $\left(\frac{1}{4}, \infty\right)$.

(Simplify your answers. Type your answers in interval notation. Use a comma to separate answers as needed.)

90. Locate the critical points of the following function. Then use the Second Derivative Test to determine whether they correspond to local maxima, local minima, or neither.

$$f(x) = x^3 - 6x^2$$

What is(are) the critical point(s) of f ? Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

- ☐ A. The critical point(s) is(are) $x =$ _____.
(Use a comma to separate answers as needed. Type an integer or a simplified fraction.)
- ☐ B. There are no critical points for f .

Find $f''(x)$.

$$f''(x) = \boxed{}$$

What is/are the local maximum/maxima of f ? Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

- ☐ A. The local maximum/maxima of f is/are at $x =$ _____.
(Use a comma to separate answers as needed. Type an integer or a simplified fraction.)
- ☐ B. There is no local maximum of f .

What is/are the local minimum/minima of f ? Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

- ☐ A. The local minimum/minima of f is/are at $x =$ _____.
(Use a comma to separate answers as needed. Type an integer or a simplified fraction.)
- ☐ B. There is no local minimum of f .

Answers A. The critical point(s) is(are) $x =$.

(Use a comma to separate answers as needed. Type an integer or a simplified fraction.)

$$6x - 12$$

A. The local maximum/maxima of f is/are at $x =$.

(Use a comma to separate answers as needed. Type an integer or a simplified fraction.)

A. The local minimum/minima of f is/are at $x =$.

(Use a comma to separate answers as needed. Type an integer or a simplified fraction.)

91. Locate the critical points of the following function. Then use the Second Derivative Test to determine whether they correspond to local maxima, local minima, or neither.

$$f(x) = 3 - 4x^2$$

What is(are) the critical point(s) of f ? Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

- ☐ A. The critical point(s) is(are) $x =$ _____.
(Use a comma to separate answers as needed. Type an integer or a simplified fraction.)
- ☐ B. There are no critical points for f .

What is/are the local maximum/maxima of f ? Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

- ☐ A. The local maximum/maxima of f is/are at $x =$ _____.
(Use a comma to separate answers as needed. Type an integer or a simplified fraction.)
- ☐ B. There is no local maximum of f .

What is/are the local minimum/minima of f ? Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

- ☐ A. The local minimum/minima of f is/are at $x =$ _____.
(Use a comma to separate answers as needed. Type an integer or a simplified fraction.)
- ☐ B. There is no local minimum of f .

Answers A. The critical point(s) is(are) $x =$.
(Use a comma to separate answers as needed. Type an integer or a simplified fraction.)

A. The local maximum/maxima of f is/are at $x =$.
(Use a comma to separate answers as needed. Type an integer or a simplified fraction.)

B. There is no local minimum of f .

92. Locate the critical points of the following function. Then use the Second Derivative Test to determine whether they correspond to local maxima, local minima, or neither.

$$f(x) = 3x^3 + 9x^2 + 16$$

What is(are) the critical point(s) of f ? Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

- ☐ A. The critical point(s) is(are) $x =$ _____.
(Use a comma to separate answers as needed. Type an integer or a simplified fraction.)
- ☐ B. There are no critical points for f .

What is/are the local minimum/minima of f ? Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

- ☐ A. The local minimum/minima of f is/are at $x =$ _____.
(Use a comma to separate answers as needed. Type an integer or a simplified fraction.)
- ☐ B. There is no local minimum of f .

What is/are the local maximum/maxima of f ? Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

- ☐ A. The local maximum/maxima of f is/are at $x =$ _____.
(Use a comma to separate answers as needed. Type an integer or a simplified fraction.)
- ☐ B. There is no local maximum of f .

Answers A. The critical point(s) is(are) $x =$.
(Use a comma to separate answers as needed. Type an integer or a simplified fraction.)

A. The local minimum/minima of f is/are at $x =$.
(Use a comma to separate answers as needed. Type an integer or a simplified fraction.)

A. The local maximum/maxima of f is/are at $x =$.
(Use a comma to separate answers as needed. Type an integer or a simplified fraction.)

93. **a.** Squares with sides of length x are cut out of each corner of a rectangular piece of cardboard measuring 4 ft by 3 ft. The resulting piece of cardboard is then folded into a box without a lid. Find the volume of the largest box that can be formed in this way.
- b.** Suppose that in part (a) the original piece of cardboard is a square with sides of length s . Find the volume of the largest box that can be formed in this way.

a. To find the objective function, express the volume V of the box in terms of x .

$$V = \boxed{}$$

(Type an expression.)

The interval of interest of the objective function is $\boxed{}$.

(Simplify your answer. Type your answer in interval notation. Use integers or decimals for any numbers in the expression.)

The maximum volume of the box is approximately $\boxed{}$ ft^3 .

(Round to the nearest hundredth as needed.)

b. To find the objective function, express the volume V of the box in terms of s and x .

$$V = \boxed{}$$

(Type an expression.)

The maximum volume of the box is $\boxed{}$.

(Type an expression using s as the variable.)

Answers $x(4 - 2x)(3 - 2x)$

$[0, 1.5]$

3.03

$x(s - 2x)(s - 2x)$

$\frac{2s^3}{27}$

94. Use a linear approximation to estimate the following quantity. Choose a value of a to produce a small error.

$\ln(0.97)$

What is the value found using the linear approximation?

$\ln(0.97) \approx \boxed{}$ (Round to two decimal places as needed.)

Answer: -0.03

95. Consider the following function and express the relationship between a small change in x and the corresponding change in y in the form $dy = f'(x)dx$.

$$f(x) = 2x^3 - 6x$$

$$dy = \left(\boxed{} \right) dx$$

Answer: $6x^2 - 6$

96. Consider the following function and express the relationship between a small change in x and the corresponding change in y in the form $dy = f'(x) dx$.

$$f(x) = \cot 10x$$

$$dy = \boxed{} dx$$

Answer: $-10 \csc^2(10x)$

97. Evaluate the following limit. Use l'Hôpital's Rule when it is convenient and applicable.

$$\lim_{x \rightarrow 0} \frac{2 \sin 9x}{7x}$$

Use l'Hôpital's Rule to rewrite the given limit so that it is not an indeterminate form.

$$\lim_{x \rightarrow 0} \frac{2 \sin 9x}{7x} = \lim_{x \rightarrow 0} \left(\boxed{} \right)$$

Evaluate the limit.

$$\lim_{x \rightarrow 0} \frac{2 \sin 9x}{7x} = \boxed{} \text{ (Type an exact answer.)}$$

Answers $\frac{18 \cos(9x)}{7}$

$$\frac{18}{7}$$

98. Use a calculator or program to compute the first 10 iterations of Newton's method when they are applied to the following function with the given initial approximation.

$$f(x) = x^2 - 8; x_0 = 3$$

k	x_k	k	x_k
0		6	
1		7	
2		8	
3		9	
4		10	
5			

(Round to six decimal places as needed.)

Answers 3.000000

2.828427

2.833333

2.828427

2.828431

2.828427

2.828427

2.828427

2.828427

2.828427

2.828427

99. Use a calculator or program to compute the first 10 iterations of Newton's method for the given function and initial approximation.

$$f(x) = 3 \sin x + 4x - 1, x_0 = 1.6$$

Complete the table.

(Do not round until the final answer. Then round to six decimal places as needed.)

k	x_k	k	x_k
1		6	
2		7	
3		8	
4		9	
5		10	

Answers - 0.546692

0.143066

0.176536

0.143066

0.143026

0.143066

0.143066

0.143066

0.143066

0.143066

100. Determine the following indefinite integral. Check your work by differentiation.

$$\int (11x^{21} - 5x^9) dx$$

$$\int (11x^{21} - 5x^9) dx = \boxed{} \text{ (Use C as the arbitrary constant.)}$$

$$\text{Answer: } \frac{x^{22}}{2} - \frac{x^{10}}{2} + C$$

101. Evaluate the following indefinite integral.

$$\int \left(\frac{3}{\sqrt{x}} + 3\sqrt{x} \right) dx$$

$$\int \left(\frac{3}{\sqrt{x}} + 3\sqrt{x} \right) dx = \boxed{}$$

(Use C as the arbitrary constant.)

Answer: $6\sqrt{x} + 2x^{\frac{3}{2}} + C$

102. Find $\int (3x + 2)^2 dx$.

$$\int (3x + 2)^2 dx = \boxed{}$$

(Use C as the arbitrary constant.)

Answer: $3x^3 + 6x^2 + 4x + C$

103. Determine the following indefinite integral. Check your work by differentiation.

$$\int 4m(7m^2 - 10m) dm$$

$$\int 4m(7m^2 - 10m) dm = \boxed{} \text{ (Use C as the arbitrary constant.)}$$

Answer: $7m^4 - \frac{40m^3}{3} + C$

104. Determine the following indefinite integral. Check your work by differentiation.

$$\int \left(4x^{\frac{1}{3}} + 2x^{-\frac{2}{3}} + 12 \right) dx$$

$$\int \left(4x^{\frac{1}{3}} + 2x^{-\frac{2}{3}} + 12 \right) dx = \boxed{} \text{ (Use C as the arbitrary constant.)}$$

Answer: $3x^{\frac{4}{3}} + 6x^{\frac{1}{3}} + 12x + C$

105. Determine the following indefinite integral. Check your work by differentiation.

$$\int 3\sqrt[8]{x} \, dx$$

$$\int 3\sqrt[8]{x} \, dx = \boxed{} \text{ (Use } C \text{ as the arbitrary constant.)}$$

Answer: $\frac{8}{3}x^{\frac{9}{8}} + C$

106. Determine the following indefinite integral. Check your work by differentiation.

$$\int (6x + 5)(7 - x) \, dx$$

$$\int (6x + 5)(7 - x) \, dx = \boxed{} \text{ (Use } C \text{ as the arbitrary constant.)}$$

Answer: $-2x^3 + \frac{37}{2}x^2 + 35x + C$

107. Determine the following indefinite integral.

$$\int \frac{4x^4 + 6x^3}{x} \, dx$$

$$\int \frac{4x^4 + 6x^3}{x} \, dx = \boxed{} \text{ (Use } C \text{ as the arbitrary constant.)}$$

Answer: $x^4 + 2x^3 + C$

108. For the following function f , find the antiderivative F that satisfies the given condition.

$$f(x) = 6x^3 + 9 \sin x, F(0) = 4$$

The antiderivative that satisfies the given condition is $F(x) = \boxed{}$.

Answer: $\frac{3}{2}x^4 - 9 \cos x + 13$

109. For the following function f , find the antiderivative F that satisfies the given condition.

$$f(u) = 9e^u - 19; F(0) = 4$$

The antiderivative that satisfies the given condition is $F(u) =$.

Answer: $9e^u - 19u - 5$

110. Given the following velocity function of an object moving along a line, find the position function with the given initial position.

$$v(t) = 9t^2 + 2t - 5; s(0) = 0$$

The position function is $s(t) =$.

Answer: $3t^3 + t^2 - 5t$

111. Find the absolute extreme values of the function on the interval.

$$F(x) = \sqrt[3]{x}, -8 \leq x \leq 27$$

- ☐ A. absolute maximum is 3 at $x = -27$; absolute minimum is -2 at $x = 27$
☐ B. absolute maximum is 3 at $x = 27$; absolute minimum is 0 at $x = 0$
☐ C. absolute maximum is 0 at $x = 0$; absolute minimum is -2 at $x = -8$
☐ D. absolute maximum is 3 at $x = 27$; absolute minimum is -2 at $x = -8$

Answer: D. absolute maximum is 3 at $x = 27$; absolute minimum is -2 at $x = -8$

112. Find the value or values of c that satisfy the equation $\frac{f(b) - f(a)}{b - a} = f'(c)$ in the conclusion of the Mean Value Theorem for the function and interval.

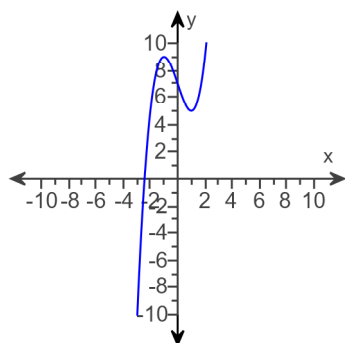
$$f(x) = x^2 + 4x + 2, [-3, 2]$$

- ☐ A. $-\frac{1}{2}, \frac{1}{2}$
☐ B. $0, -\frac{1}{2}$
☐ C. $-\frac{1}{2}$
☐ D. $-3, 2$

Answer: C. $-\frac{1}{2}$

113.

Use the graph of the function $f(x)$ to locate the local extrema and identify the intervals where the function is concave up and concave down.



- ☐ A. Local minimum at $x = 1$; local maximum at $x = -1$; concave down on $(-\infty, \infty)$
- ☐ B. Local minimum at $x = 1$; local maximum at $x = -1$; concave up on $(0, \infty)$; concave down on $(-\infty, 0)$
- ☐ C. Local minimum at $x = 1$; local maximum at $x = -1$; concave down on $(0, \infty)$; concave up on $(-\infty, 0)$
- ☐ D. Local minimum at $x = 1$; local maximum at $x = -1$; concave up on $(-\infty, \infty)$

Answer: B. Local minimum at $x = 1$; local maximum at $x = -1$; concave up on $(0, \infty)$; concave down on $(-\infty, 0)$

114. From a thin piece of cardboard 20 in by 20 in, square corners are cut out so that the sides can be folded up to make a box. What dimensions will yield a box of maximum volume? What is the maximum volume? Round to the nearest tenth, if necessary.

- ☐ A. 6.7 in $\times$ 6.7 in $\times$ 6.7 in; 296.3 in³
- ☐ B. 10.0 in $\times$ 10.0 in $\times$ 5.0 in; 500.0 in³
- ☐ C. 13.3 in $\times$ 13.3 in $\times$ 3.3 in; 592.6 in³
- ☐ D. 13.3 in $\times$ 13.3 in $\times$ 6.7 in; 1,185.2 in³

Answer: C. 13.3 in $\times$ 13.3 in $\times$ 3.3 in; 592.6 in³

115. Solve the initial value problem.

$$\frac{ds}{dt} = \cos t - \sin t, \quad s\left(\frac{\pi}{2}\right) = 7$$

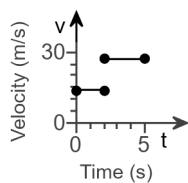
- ☐ A. $s = 2 \sin t + 5$
- ☐ B. $s = \sin t + \cos t + 8$
- ☐ C. $s = \sin t - \cos t + 6$
- ☐ D. $s = \sin t + \cos t + 6$

Answer: D. $s = \sin t + \cos t + 6$

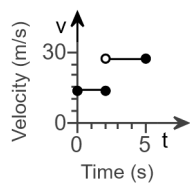
116. Suppose an object moves along a line at 14 m/s for $0 \leq t \leq 2$ s and at 27 m/s for $2 < t \leq 5$ s. Sketch the graph of the velocity function and find the displacement of the object for $0 \leq t \leq 5$.

Sketch the graph of the velocity function. Choose the correct graph below.

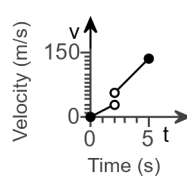
☐ A.



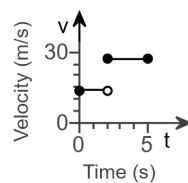
☐ B.



☐ C.

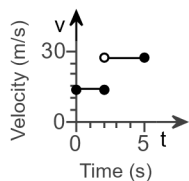


☐ D.



The displacement of the object for $0 \leq t \leq 5$ is m. (Simplify your answer.)

Answers

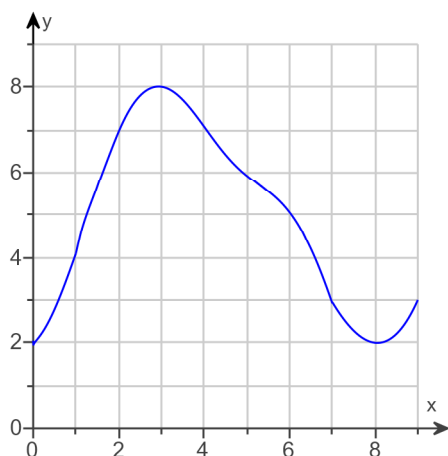


B.

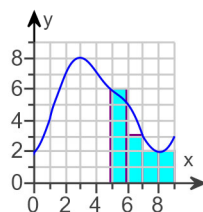
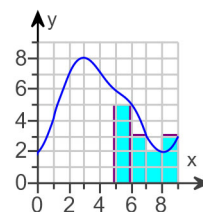
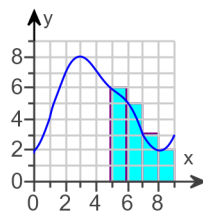
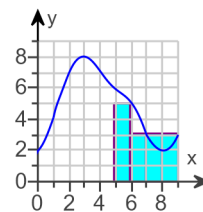
109

117.

Approximate the area of the region bounded by the graph of $f(x)$ (shown below) and the x -axis by dividing the interval $[5, 9]$ into $n = 4$ subintervals. Use a left and right Riemann sum to obtain two different approximations. Draw the approximating rectangles.

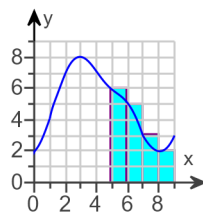
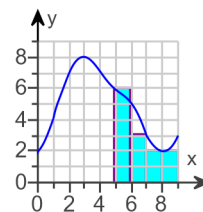
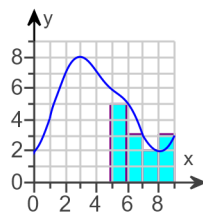
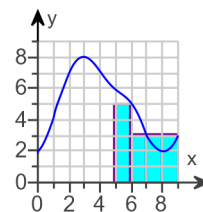


In which graph below are the selected points the left endpoints of the 4 approximating rectangles?

☐ A.☐ B.☐ C.☐ D.

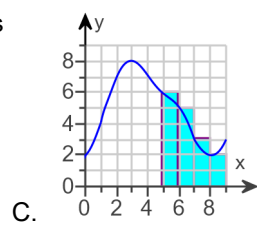
Using the specified rectangles, approximate the area.

In which graph below are the selected points the right endpoints of the 4 approximating rectangles?

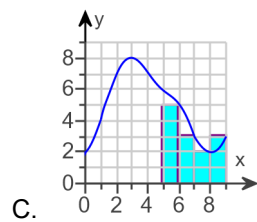
☐ A.☐ B.☐ C.☐ D.

Using the specified rectangles, approximate the area.

Answers



16



13

118. Evaluate the following expressions.

$$\begin{array}{llll} \text{a. } \sum_{k=1}^{16} k & \text{b. } \sum_{k=1}^9 (4k+1) & \text{c. } \sum_{k=1}^7 k^2 & \text{d. } \sum_{n=1}^8 (1+n^2) \\ \text{e. } \sum_{m=1}^3 \frac{3m+3}{8} & \text{f. } \sum_{j=1}^3 (5j-7) & \text{g. } \sum_{k=1}^9 k(5k+8) & \text{h. } \sum_{n=0}^7 \sin \frac{n\pi}{2} \end{array}$$

$$\begin{array}{ll} \text{a. } \sum_{k=1}^{16} k = \boxed{} & \text{(Type an integer or a simplified fraction.)} \\ \text{b. } \sum_{k=1}^9 (4k+1) = \boxed{} & \text{(Type an integer or a simplified fraction.)} \\ \text{c. } \sum_{k=1}^7 k^2 = \boxed{} & \text{(Type an integer or a simplified fraction.)} \\ \text{d. } \sum_{n=1}^8 (1+n^2) = \boxed{} & \text{(Type an integer or a simplified fraction.)} \\ \text{e. } \sum_{m=1}^3 \frac{3m+3}{8} = \boxed{} & \text{(Type an integer or a simplified fraction.)} \\ \text{f. } \sum_{j=1}^3 (5j-7) = \boxed{} & \text{(Type an integer or a simplified fraction.)} \\ \text{g. } \sum_{k=1}^9 k(5k+8) = \boxed{} & \text{(Type an integer or a simplified fraction.)} \\ \text{h. } \sum_{n=0}^7 \sin \frac{n\pi}{2} = \boxed{} & \text{(Type an integer or a simplified fraction.)} \end{array}$$

Answers 136

189

140

212

$\frac{27}{8}$

9

1785

0

119.

The functions f and g are integrable and $\int_1^7 f(x)dx = 8$, $\int_1^7 g(x)dx = 5$, and $\int_5^7 f(x)dx = 2$. Evaluate the integral below or state that there is not enough information.

$$-\int_7^1 4f(x)dx$$

Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

☐ A. $-\int_7^1 4f(x)dx =$ _____ (Simplify your answer.)

☐ B. There is not enough information to evaluate $-\int_7^1 4f(x)dx$.

Answer: A. $-\int_7^1 4f(x)dx =$ (Simplify your answer.)

120.

Evaluate $\frac{d}{dx} \int_a^x f(t) dt$ and $\frac{d}{dx} \int_a^b f(t) dt$, where a and b are constants.

$\frac{d}{dx} \int_a^x f(t) dt =$ (Simplify your answer.)

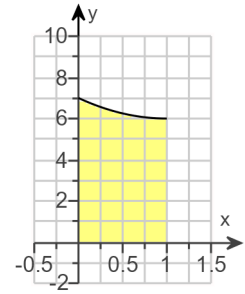
$\frac{d}{dx} \int_a^b f(t) dt =$ (Simplify your answer.)

Answers $f(x)$

0

121. Evaluate the following integral using the Fundamental Theorem of Calculus. Discuss whether your result is consistent with the figure.

$$\int_0^1 (x^2 - 2x + 7) dx$$



$$\int_0^1 (x^2 - 2x + 7) dx = \boxed{}$$

Is your result consistent with the figure?

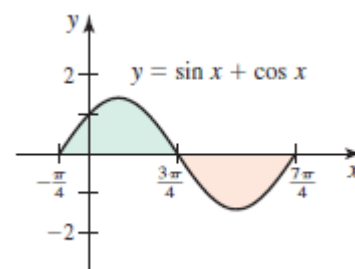
- ☐ A. Yes, because the definite integral is positive and the graph of f lies above the x -axis.
- ☐ B. Yes, because the definite integral is negative and the graph of f lies below the x -axis.
- ☐ C. No, because the definite integral is positive and the graph of f lies below the x -axis.
- ☐ D. No, because the definite integral is negative and the graph of f lies above the x -axis.

Answers $\frac{19}{3}$

A. Yes, because the definite integral is positive and the graph of f lies above the x -axis.

122.

Evaluate the integral $\int_{-\pi/4}^{7\pi/4} (\sin x + \cos x) dx$ using the fundamental theorem of calculus. Discuss whether your result is consistent with the figure shown to the right.



$$\int_{-\pi/4}^{7\pi/4} (\sin x + \cos x) dx = \boxed{}$$

Is this value consistent with the given figure?

- ☐ A. The value is not consistent with the figure because the figure is a graph of the base function, $f(x)$, instead of a graph of the area function, $A(x)$.
- ☐ B. The value is not consistent with the figure because the total area could be approximated using a rectangle of base π and height $\sin(\pi/4) + \cos(\pi/4) = \sqrt{2}$.
- ☐ C. The value is consistent with the figure because the total area can be approximated using a rectangle of base π and height $\sin(\pi/4) + \cos(\pi/4) = \sqrt{2}$.
- ☐ D. The value is consistent with the figure because the area below the x-axis appears to be equal to the area above the x-axis.

Answers 0

D.

The value is consistent with the figure because the area below the x-axis appears to be equal to the area above the x-axis.

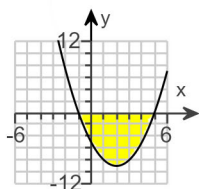
123. Evaluate the following integral using the fundamental theorem of calculus. Sketch the graph of the integrand and shade the region whose net area you have found.

$$\int_{-1}^5 (x^2 - 4x - 5) \, dx$$

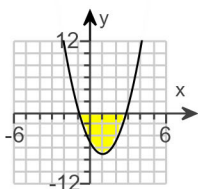
$$\int_{-1}^5 (x^2 - 4x - 5) \, dx = \boxed{}$$

Choose the correct sketch below.

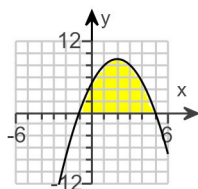
☐ A.



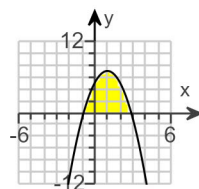
☐ B.



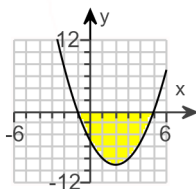
☐ C.



☐ D.



Answers - 36



A.

124. Use the fundamental theorem of calculus to evaluate the following definite integral.

$$\int_1^3 (4x^3 + 2) \, dx$$

$$\int_1^3 (4x^3 + 2) \, dx = \boxed{}$$

Answer: 84

125. Evaluate the following integral using the Fundamental Theorem of Calculus.

$$\int_1^5 (1-x)(x-5) \, dx$$

$$\int_1^5 (1-x)(x-5) \, dx = \boxed{}$$

Answer: $\frac{32}{3}$

126. Find the area of the region bounded by the graph of f and the x -axis on the given interval.

$$f(x) = x^2 - 20; [-1, 1]$$

The area is $\boxed{}$. (Type an integer or a simplified fraction.)

Answer: $\frac{118}{3}$

127. Simplify the following expression.

$$\frac{d}{dx} \int_x^6 \sqrt{t^3 + 2} \, dt$$

$$\frac{d}{dx} \int_x^6 \sqrt{t^3 + 2} \, dt = \boxed{}$$

Answer: $-\sqrt{x^3 + 2}$

128. Simplify the following expression.

$$\frac{d}{dx} \int_8^{x^3} \frac{dp}{p^2}$$

$$\frac{d}{dx} \int_8^{x^3} \frac{dp}{p^2} = \boxed{}$$

Answer: $\frac{3}{x^4}$

129. Evaluate the following integral.

$$\int_0^2 (x-3)^2 dx$$

$$\int_0^2 (x-3)^2 dx = \boxed{}$$

(Type an exact answer. Use C as the arbitrary constant as needed.)

Answer: $\frac{26}{3}$

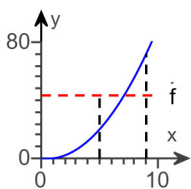
130. Find the average value of the following function over the given interval. Draw a graph of the function and indicate the average value.

$$f(x) = x(x-1); [5, 9]$$

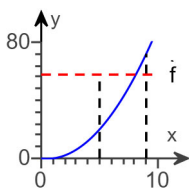
The average value of the function is $\bar{f} = \boxed{}$.

Choose the correct graph of $f(x)$ and $\bar{f}$ below.

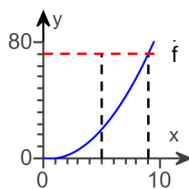
☐ A.



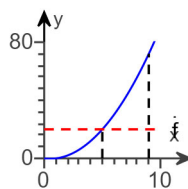
☐ B.



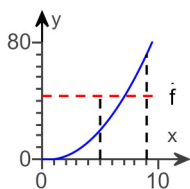
☐ C.



☐ D.



Answers $\frac{130}{3}$

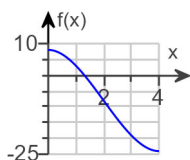


A.

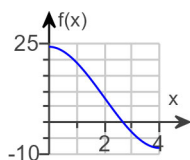
131. The elevation of a path is given by $f(x) = x^3 - 6x^2 + 8$, where x measures horizontal distances. Draw a graph of the elevation function and find its average value for $0 \leq x \leq 4$.

Choose the correct graph below.

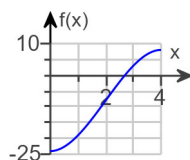
☐ A.



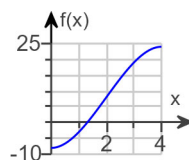
☐ B.



☐ C.

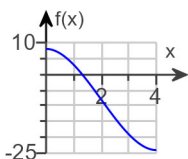


☐ D.



The average value is . (Type an integer or a simplified fraction.)

Answers



A.

- 8

132. Find the point(s) at which the function $f(x) = 8 - 6x$ equals its average value on the interval $[0, 6]$.

The function equals its average value at $x =$.
(Use a comma to separate answers as needed.)

Answer: 3

133. Use the substitution $u = x^2 + 8$ to find the following indefinite integral. Check your answer by differentiation.

$$\int 2x(x^2 + 8)^7 dx$$

$$\int 2x(x^2 + 8)^7 dx = \text{}$$

(Use C as the arbitrary constant.)

Answer: $\frac{1}{8}(x^2 + 8)^8 + C$

134. Use the substitution $u = 5x^2 + 2$ to find the following indefinite integral. Check your answer by differentiation.

$$\int -10x \sin(5x^2 + 2) \, dx$$

$$\int -10x \sin(5x^2 + 2) \, dx = \boxed{}$$

(Use C as the arbitrary constant.)

Answer: $\cos(5x^2 + 2) + C$

135. Use the substitution $u = 5x^2 + 4x$ to evaluate the indefinite integral below.

$$\int (10x + 4)\sqrt{5x^2 + 4x} \, dx$$

Write the integrand in terms of u .

$$\int (10x + 4)\sqrt{5x^2 + 4x} \, dx = \int (\boxed{}) \, du$$

Evaluate the integral.

$$\int (10x + 4)\sqrt{5x^2 + 4x} \, dx = \boxed{}$$

(Use C as the arbitrary constant.)

Answers $\sqrt{u}$

$$\frac{2}{3} (5x^2 + 4x)^{\frac{3}{2}} + C$$

136. Use a change of variables or the accompanying table to evaluate the following indefinite integral.

$$\int \frac{e^{6x}}{e^{6x} + 2} dx$$

² Click the icon to view the table of general integration formulas.

Determine a change of variables from x to u . Choose the correct answer below.

☐ A. $u = e^{6x} + 2$

☐ B. $u = \frac{1}{e^{6x} + 2}$

☐ C. $u = 6x$

☐ D. $u = e^{6x}$

Write the integral in terms of u .

$$\int \frac{e^{6x}}{e^{6x} + 2} dx = \int (\text{ }) du$$

Evaluate the integral.

$$\int \frac{e^{6x}}{e^{6x} + 2} dx = \text{ }$$

(Use C as the arbitrary constant.)

2: General Integration Formulas

$$\int \cos ax \, dx = \frac{1}{a} \sin ax + C$$

$$\int \sin ax \, dx = -\frac{1}{a} \cos ax + C$$

$$\int \sec^2 ax \, dx = \frac{1}{a} \tan ax + C$$

$$\int \csc^2 ax \, dx = -\frac{1}{a} \cot ax + C$$

$$\int \sec ax \tan ax \, dx = \frac{1}{a} \sec ax + C$$

$$\int \csc ax \cot ax \, dx = -\frac{1}{a} \csc ax + C$$

$$\int e^{ax} dx = \frac{1}{a} e^{ax} + C$$

$$\int b^x dx = \frac{1}{\ln b} b^x + C, b > 0, b \neq 1$$

$$\int \frac{dx}{a^2 + x^2} = \frac{1}{a} \tan^{-1} \frac{x}{a} + C$$

$$\int \frac{dx}{\sqrt{a^2 - x^2}} = \sin^{-1} \frac{x}{a} + C, a > 0$$

$$\int \frac{dx}{x\sqrt{x^2 - a^2}} = \frac{1}{a} \sec^{-1} \left| \frac{x}{a} \right| + C, a > 0$$

Answers A. $u = e^{6x} + 2$

$$\frac{1}{6u}$$

$$\frac{1}{6} \ln |e^{6x} + 2| + C$$

137. Use a change of variables or the table to evaluate the following definite integral.

$$\int_0^{\pi/4} \cos 6x \, dx$$

³ Click to view the table of general integration formulas.

$$\int_0^{\pi/4} \cos 6x \, dx = \boxed{} \text{ (Type an exact answer.)}$$

3: General Integration Formulas

$$\int \cos ax \, dx = \frac{1}{a} \sin ax + C$$

$$\int \sin ax \, dx = -\frac{1}{a} \cos ax + C$$

$$\int \sec^2 ax \, dx = \frac{1}{a} \tan ax + C$$

$$\int \csc^2 ax \, dx = -\frac{1}{a} \cot ax + C$$

$$\int \sec ax \tan ax \, dx = \frac{1}{a} \sec ax + C$$

$$\int \csc ax \cot ax \, dx = -\frac{1}{a} \csc ax + C$$

$$\int e^{ax} \, dx = \frac{1}{a} e^{ax} + C$$

$$\int b^x \, dx = \frac{1}{\ln b} b^x + C, b > 0, b \neq 1$$

$$\int \frac{dx}{a^2 + x^2} = \frac{1}{a} \tan^{-1} \frac{x}{a} + C$$

$$\int \frac{dx}{\sqrt{a^2 - x^2}} = \sin^{-1} \frac{x}{a} + C, a > 0$$

$$\int \frac{dx}{x\sqrt{x^2 - a^2}} = \frac{1}{a} \sec^{-1} \left| \frac{x}{a} \right| + C, a > 0$$

Answer: $-\frac{1}{6}$

138. Use a change of variables or the table to evaluate the following definite integral.

$$\int_0^5 8e^{2x} dx$$

⁴ Click to view the table of general integration formulas.

$$\int_0^5 8e^{2x} dx = \boxed{} \text{ (Type an exact answer.)}$$

4: General Integration Formulas

$$\int \cos ax \, dx = \frac{1}{a} \sin ax + C$$

$$\int \sin ax \, dx = -\frac{1}{a} \cos ax + C$$

$$\int \sec^2 ax \, dx = \frac{1}{a} \tan ax + C$$

$$\int \csc^2 ax \, dx = -\frac{1}{a} \cot ax + C$$

$$\int \sec ax \tan ax \, dx = \frac{1}{a} \sec ax + C$$

$$\int \csc ax \cot ax \, dx = -\frac{1}{a} \csc ax + C$$

$$\int e^{ax} dx = \frac{1}{a} e^{ax} + C$$

$$\int b^x dx = \frac{1}{\ln b} b^x + C, b > 0, b \neq 1$$

$$\int \frac{dx}{a^2 + x^2} = \frac{1}{a} \tan^{-1} \frac{x}{a} + C$$

$$\int \frac{dx}{\sqrt{a^2 - x^2}} = \sin^{-1} \frac{x}{a} + C, a > 0$$

$$\int \frac{dx}{x\sqrt{x^2 - a^2}} = \frac{1}{a} \sec^{-1} \left| \frac{x}{a} \right| + C, a > 0$$

Answer: $4e^{10} - 4$

139. Use a change of variables or the table to evaluate the following definite integral.

$$\int_0^1 5x^4 (1 - x^5) dx$$

⁵ Click to view the table of general integration formulas.

$$\int_0^1 5x^4 (1 - x^5) dx = \boxed{} \text{ (Type an exact answer.)}$$

5: General Integration Formulas

$$\int \cos ax \, dx = \frac{1}{a} \sin ax + C$$

$$\int \sin ax \, dx = -\frac{1}{a} \cos ax + C$$

$$\int \sec^2 ax \, dx = \frac{1}{a} \tan ax + C$$

$$\int \csc^2 ax \, dx = -\frac{1}{a} \cot ax + C$$

$$\int \sec ax \tan ax \, dx = \frac{1}{a} \sec ax + C$$

$$\int \csc ax \cot ax \, dx = -\frac{1}{a} \csc ax + C$$

$$\int e^{ax} \, dx = \frac{1}{a} e^{ax} + C$$

$$\int b^x \, dx = \frac{1}{\ln b} b^x + C, b > 0, b \neq 1$$

$$\int \frac{dx}{a^2 + x^2} = \frac{1}{a} \tan^{-1} \frac{x}{a} + C$$

$$\int \frac{dx}{\sqrt{a^2 - x^2}} = \sin^{-1} \frac{x}{a} + C, a > 0$$

$$\int \frac{dx}{x\sqrt{x^2 - a^2}} = \frac{1}{a} \sec^{-1} \left| \frac{x}{a} \right| + C, a > 0$$

Answer: $\frac{1}{2}$

140. Use a finite approximation to estimate the area under the graph of the given function on the stated interval as instructed.

$f(x) = x^2$ between $x = 0$ and $x = 4$, using a right sum with two rectangles of equal width

- ☐ A. 38.75
☐ B. 20
☐ C. 8
☐ D. 40

Answer: D. 40

141. Suppose that $\int_5^6 f(x)dx = -7$. Find $\int_5^6 4f(u)du$ and $\int_5^6 -f(u)du$.

- ☐ A. $-28; 7$
☐ B. $-28; -\frac{1}{7}$
☐ C. $4; 7$
☐ D. $-3; -7$

Answer: A. $-28; 7$

142. Find the derivative.

$$\frac{d}{dx} \int_1^{\sqrt{x}} 12t^5 dt$$

- ☐ A. $4x^{2.5} - 4$
☐ B. $6x^{0.5}4$
☐ C. $8x^{2.5}$
☐ D. $12x^{5/2}$

Answer: B. $6x^{0.5}4$

143. Evaluate the integral using the given substitution.

$$\int x \cos(4x^2) dx, \quad u = 4x^2$$

- ☐ A. $\frac{1}{8} \sin(4x^2) + C$
☐ B. $\sin(4x^2) + C$
☐ C. $\frac{x^2}{2} \sin(4x^2) + C$
☐ D. $\frac{1}{u} \sin(u) + C$

Answer: A. $\frac{1}{8} \sin(4x^2) + C$

144. Evaluate the following integral.

$$\int \frac{dx}{x^2 - 2x + 101}$$

$$\int \frac{dx}{x^2 - 2x + 101} = \boxed{}$$

(Use C as the arbitrary constant as needed.)

Answer: $\frac{1}{10} \tan^{-1} \frac{x-1}{10} + C$

145. If the general solution of a differential equation is $y(t) = C e^{-4t} + 7$, what is the solution that satisfies the initial condition $y(0) = 3$?

$$y(t) = \boxed{}$$

Answer: $-4 e^{-4t} + 7$