

01-07-20 01-09-20 01-13-20 01-25-20

Student: \_\_\_\_\_  
Date: \_\_\_\_\_

Instructor: Alfredo Alvarez  
Course: Math 1314 Sullivan Coreq

Assignment: finalm1314COC038sullljjRZZ18M

1. Solve the equation.

$$9x^3 + x^2 - 81x - 9 = 0$$

The solution set is

(Simplify your answer. Type an integer or a simplified fraction. Use a comma to separate answers as needed.)

Answer:  $-\frac{1}{9}, -3, 3$

ID: PF.4.39

*use synthetic division*

*use synthetic division*

*Possible List First*  
 $\pm 9$   
 $\pm 3$   
 $\pm 1$   
 $\pm 9, \pm 3, \pm 1$   
 $\pm 9, \pm 3, \pm 1, \pm \frac{1}{9}, \pm \frac{1}{3} =$

*Try  
x = -3*

$$\begin{array}{r|rrrr} -3 & 9 & 1 & -81 & -9 \\ & & & -27 & 78 & 9 \end{array}$$

$9x^2 - 26x - 3 = 0$  *rem possible*

$$9x^2 - 26x - 3 = 0$$

$$(9x + 1)(x - 3) = 0$$

$$9x + 1 = 0 \quad \text{OR} \quad x - 3 = 0$$

$$9x + 1 - 1 = 0 - 1 \quad \text{OR} \quad x - 3 + 3 = 0 + 3$$

$$9x = -1 \quad \text{OR} \quad x = 3$$

$$\frac{9x}{9} = \frac{-1}{9}$$

$$x = -\frac{1}{9}$$

*Answer*  
 $-3, -\frac{1}{9}, 3$



*Sharky*

2. Find the domain of the function.

$f(x) = \sqrt{4x - 28}$

The domain is . (Type your answer in interval notation.)

Answer:  $[7, \infty)$

ID: 1.1.59

$f(x) = \sqrt{4x - 28}$

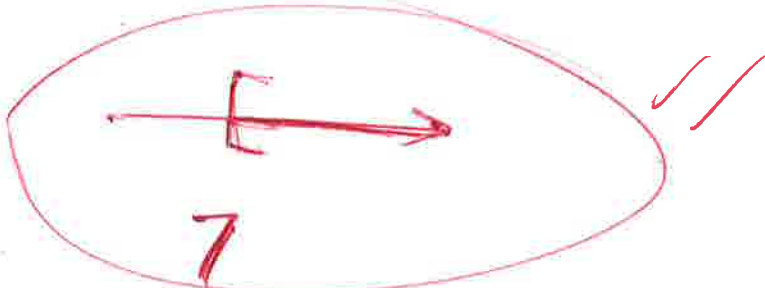
set  $4x - 28 \geq 0$

$4x - 28 + 28 \geq 0 + 28$

$4x \geq 28$

$\frac{4x}{4} \geq \frac{28}{4}$

$x \geq 7$  ✓



$[7, \infty)$  ✓

Formula  
Domain  
 $f(x) = \sqrt{Ax+B}$   
set  $Ax+B \geq 0$

3. For the given functions  $f$  and  $g$ , complete parts (a)-(h). For parts (a)-(d), also find the domain.

$f(x) = 2x + 3; g(x) = 9x - 5$

(a) Find  $(f + g)(x)$ .

$(f + g)(x) = \text{[ ]}$  (Simplify your answer.)

$(f+g)(x) =$   
 $f(x) + g(x) =$   
 $(2x+3) + (9x-5) =$   
 $2x+3 + 9x-5 =$   
 $11x-2 =$  ✓

Domain  
 $(-\infty, \infty)$

What is the domain of  $f + g$ ? Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

A. The domain is  $\{x | \text{[ ]}\}$ .  
 (Use integers or fractions for any numbers in the expression. Use a comma to separate answers as needed.)

B. The domain is  $\{x | x \text{ is any real number}\}$ .

(b) Find  $(f - g)(x)$ .

$(f - g)(x) = \text{[ ]}$  (Simplify your answer.)

$(f-g)(x) =$   
 $f(x) - g(x) =$   
 $(2x+3) - (9x-5) =$   
 $2x+3 - 9x+5 =$   
 $-7x+8 =$  ✓

Domain  
 $(-\infty, \infty)$

What is the domain of  $f - g$ ? Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

A. The domain is  $\{x | \text{[ ]}\}$ .  
 (Use integers or fractions for any numbers in the expression. Use a comma to separate answers as needed.)

B. The domain is  $\{x | x \text{ is any real number}\}$ .

(c) Find  $(f \cdot g)(x)$ .

$(f \cdot g)(x) = \text{[ ]}$  (Simplify your answer.)

$(f \cdot g)(x) =$   
 $f(x) \cdot g(x) =$   
 $(2x+3)(9x-5) =$   
 $18x^2 - 10x + 27x - 15 =$   
 $18x^2 + 17x - 15 =$  ✓

Domain  
 $(-\infty, \infty)$

What is the domain of  $f \cdot g$ ? Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

A. The domain is  $\{x | \text{[ ]}\}$ .  
 (Use integers or fractions for any numbers in the expression. Use a comma to separate answers as needed.)

B. The domain is  $\{x | x \text{ is any real number}\}$ .

(d) Find  $\left(\frac{f}{g}\right)(x)$ .

$\left(\frac{f}{g}\right)(x) = \text{[ ]}$  (Simplify your answer.)

$\left(\frac{f}{g}\right)(x) =$   
 $\frac{f(x)}{g(x)} =$   
 $\frac{2x+3}{9x-5} =$  ✓  
 $9x-5=0$   
 $9x-5+5=0+5$   
 $9x=5$   
 $x = \frac{5}{9}$   
 Domain  $x \neq \frac{5}{9}$

What is the domain of  $\frac{f}{g}$ ? Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

A. The domain is  $\{x | \text{[ ]}\}$ .  
 (Use integers or fractions for any numbers in the expression. Use a comma to separate answers as needed.)

B. The domain is  $\{x | x \text{ is any real number}\}$ .

(e) Find  $(f + g)(3)$ .

$(f+g)(x) = 11x - 2$   
 $(f+g)(3) = 11(3) - 2$   
 $(f+g)(3) = 33 - 2$   
 $(f+g)(3) = 31$  ✓



$(f + g)(3) =$   (Type an integer or a simplified fraction.)

(f) Find  $(f - g)(4)$ .

$(f - g)(4) =$   (Type an integer or a simplified fraction.)

(g) Find  $(f \cdot g)(2)$ .

$(f \cdot g)(2) =$   (Type an integer or a simplified fraction.)

(h) Find  $\left(\frac{f}{g}\right)(1)$ .

$\left(\frac{f}{g}\right)(1) =$   (Type an integer or a simplified fraction.)

$(f - g)(x) = -7x + 8$   
 $(f - g)(4) = -7(4) + 8$   
 $(f - g)(4) = -28 + 8$   
 $(f - g)(4) = -20$  ✓✓

$(f \cdot g)(x) = 18x^2 + 17x - 15$   
 $(f \cdot g)(2) = 18(2)^2 + 17(2) - 15$

$(f \cdot g)(2) = 18(2)(2) + 17(2) - 15$   
 $(f \cdot g)(2) = 18(4) + 17(2) - 15$   
 $(f \cdot g)(2) = 72 + 34 - 15$   
 $(f \cdot g)(2) = 106 - 15$   
 $(f \cdot g)(2) = 91$  ✓✓

$\left(\frac{f}{g}\right)(x) = \frac{2x + 3}{9x - 5}$

$\left(\frac{f}{g}\right)(1) = \frac{2(1) + 3}{9(1) - 5}$

$\left(\frac{f}{g}\right)(1) = \frac{2 + 3}{9 - 5}$

$\left(\frac{f}{g}\right)(1) = \frac{5}{4}$  ✓✓

Answers  $11x - 2$

B. The domain is  $\{x \mid x \text{ is any real number}\}$ .

$-7x + 8$

B. The domain is  $\{x \mid x \text{ is any real number}\}$ .

$18x^2 + 17x - 15$

B. The domain is  $\{x \mid x \text{ is any real number}\}$ .

$\frac{2x + 3}{9x - 5}$

A. The domain is  $\left\{x \mid \boxed{x \neq \frac{5}{9}}\right\}$ .

(Use integers or fractions for any numbers in the expression. Use a comma to separate answers as needed.)

31

-20

91

$\frac{5}{4}$

ID: 1.1.67

4. For the given functions  $f$  and  $g$ , complete parts (a)-(h). For parts (a)-(d), also find the domain.

$f(x) = x - 1; g(x) = 5x^2$

(a) Find  $(f + g)(x)$ .

$(f + g)(x) = \text{[ ]}$  (Simplify your answer.)  $x - 1 + 5x^2 =$

Handwritten work for (a):  
 $(f+g)(x) = f(x) + g(x) = (x-1) + (5x^2) = 5x^2 + x - 1 =$   
 Domain:  $(-\infty, \infty)$

What is the domain of  $f + g$ ? Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

A. The domain is  $\{x \mid \text{[ ]}\}$ .  
 (Use integers or fractions for any numbers in the expression. Use a comma to separate answers as needed.)

B. The domain is  $\{x \mid x \text{ is any real number}\}$ .

(b) Find  $(f - g)(x)$ .

$(f - g)(x) = \text{[ ]}$  (Simplify your answer.)  $x - 1 - 5x^2 =$

Handwritten work for (b):  
 $(f-g)(x) = f(x) - g(x) = (x-1) - (5x^2) = x - 1 - 5x^2 =$   
 Domain:  $(-\infty, \infty)$

What is the domain of  $f - g$ ? Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

A. The domain is  $\{x \mid \text{[ ]}\}$ .  
 (Use integers or fractions for any numbers in the expression. Use a comma to separate answers as needed.)

B. The domain is  $\{x \mid x \text{ is any real number}\}$ .

(c) Find  $(f \cdot g)(x)$ .

$(f \cdot g)(x) = \text{[ ]}$  (Simplify your answer.)  $(x-1)(5x^2) =$

Handwritten work for (c):  
 $(f \cdot g)(x) = f(x) \cdot g(x) = (x-1)(5x^2) = 5x^3 - 5x^2 =$   
 Domain:  $(-\infty, \infty)$

What is the domain of  $f \cdot g$ ? Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

A. The domain is  $\{x \mid \text{[ ]}\}$ .  
 (Use integers or fractions for any numbers in the expression. Use a comma to separate answers as needed.)

B. The domain is  $\{x \mid x \text{ is any real number}\}$ .

(d) Find  $\left(\frac{f}{g}\right)(x)$ .

$\left(\frac{f}{g}\right)(x) = \text{[ ]}$  (Simplify your answer.)  $\frac{x-1}{5x^2} =$

Handwritten work for (d):  
 $\left(\frac{f}{g}\right)(x) = \frac{f(x)}{g(x)} = \frac{x-1}{5x^2} =$   
 Set bottom = 0:  $5x^2 = 0 \Rightarrow x^2 = 0 \Rightarrow x = 0$   
 Domain:  $x \neq 0$

What is the domain of  $\frac{f}{g}$ ? Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

A. The domain is  $\{x \mid \text{[ ]}\}$ .  
 (Use integers or fractions for any numbers in the expression. Use a comma to separate answers as needed.)

B. The domain is  $\{x \mid x \text{ is any real number}\}$ .

(e) Find  $(f + g)(3)$ .

Handwritten work for (e):  
 $(f+g)(x) = 5x^2 + x - 1$   
 $(f+g)(3) = 5(3)^2 + (3) - 1 = 45 + 3 - 1 = 47$

$(f + g)(3) = \boxed{\phantom{000}}$  (Type an integer or a simplified fraction.)

(f) Find  $(f - g)(2)$ .

$(f - g)(2) = \boxed{\phantom{000}}$  (Type an integer or a simplified fraction.)

(g) Find  $(f \cdot g)(4)$ .

$(f \cdot g)(4) = \boxed{\phantom{000}}$  (Type an integer or a simplified fraction.)

(h) Find  $\left(\frac{f}{g}\right)(4)$ .

$\left(\frac{f}{g}\right)(4) = \boxed{\phantom{000}}$  (Type an integer or a simplified fraction.)

Answers  $5x^2 + x - 1$

B. The domain is  $\{x \mid x \text{ is any real number}\}$ .

$-5x^2 + x - 1$

B. The domain is  $\{x \mid x \text{ is any real number}\}$ .

$5x^3 - 5x^2$

B. The domain is  $\{x \mid x \text{ is any real number}\}$ .

$\frac{x-1}{5x^2}$

A. The domain is  $\{x \mid \boxed{x \neq 0}\}$ .

(Use integers or fractions for any numbers in the expression. Use a comma to separate answers as needed.)

47

-19

240

$\frac{3}{80}$

ID: 1.1.69

5. Find the difference quotient of  $f$ ; that is, find  $\frac{f(x+h) - f(x)}{h}$ ,  $h \neq 0$ , for the following function. Be sure to simplify.

$f(x) = x^2 - 7x + 7$   $\frac{(x+h)^2 - 7(x+h) + 7 - (x^2 - 7x + 7)}{h} =$

$\frac{f(x+h) - f(x)}{h} = \frac{(x+h)(x+h) - 7x - 7h + 7 - x^2 + 7x - 7}{h} =$

Answer:  $2x + h - 7$   $\frac{x^2 + 1xh + 1xh + h^2 - 7x - 7h + 7 - x^2 + 7x - 7}{h} =$

ID: 1.1.83  $\frac{2xh + h^2 - 7h}{h} = \frac{2xh}{h} + \frac{h^2}{h} - \frac{7h}{h} = \boxed{2x + h - 7}$

$(f-g)(x) = -5x^2 + x - 1$   
 $(f-g)(2) = -5(2)^2 + (2) - 1$   
 $(f-g)(2) = -5(2)(2) + (2) - 1$   
 $(f-g)(2) = -5(4) + (2) - 1$   
 $(f-g)(2) = -20 + 2 - 1$   
 $(f-g)(2) = -19$

$(f \cdot g)(x) = 5x^3 - 5x^2$   
 $(f \cdot g)(4) = 5(4)^3 - 5(4)^2$   
 $(f \cdot g)(4) = 5(4)(4)(4) - 5(4)(4)$   
 $(f \cdot g)(4) = 5(64) - 5(16)$   
 $(f \cdot g)(4) = 320 - 80$   
 $(f \cdot g)(4) = 240$

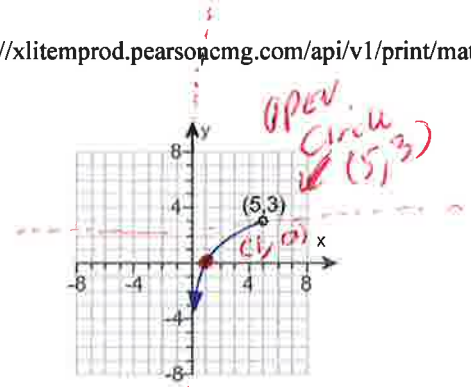
$\left(\frac{f}{g}\right)(x) = \frac{x-1}{5x^2}$

$\left(\frac{f}{g}\right)(4) = \frac{(4)-1}{5(4)^2}$   $\left(\frac{f}{g}\right)(4) = \frac{3}{80}$   
 $\left(\frac{f}{g}\right)(4) = \frac{4-1}{5(4)(4)}$   
 $\left(\frac{f}{g}\right)(4) = \frac{3}{5(16)}$



6. Determine whether the graph on the right is that of a function by using the vertical-line test. If it is, use the graph to find the following.

- (a) the domain and range
- (b) the intercepts, if any
- (c) any symmetry with respect to the x-axis, y-axis, or the origin



Does the graph represent a function? Choose the correct answer below.

- A. Yes, the graph is a function because every vertical line intersects the graph in at most one point.
- B. No, the graph is not a function because a vertical line  $x = 4$  intersects the graph at only one point.
- C. No, the graph is not a function because a vertical line  $x = 4$  intersects the graph at two points.
- D. Yes, the graph is a function because every vertical line intersects the graph in more than one point.

(a) What are the domain and range of the function? Select the correct choice below and, if necessary, fill in the answer box(es) to complete your choice.

- A. The domain is  $(0, 5)$ . The range is  $(-\infty, 3)$ .  
(Type your answers in interval notation. Use integers or fractions for any numbers in the expressions.)
- B. The graph is not that of a function.

(b) What is/are the intercept(s)? Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

- A. The intercept(s) is/are  $(1, 0)$ .  
(Type an ordered pair. Use a comma to separate answers as needed.)
- B. There are no intercepts.
- C. The graph is not that of a function.

(c) Determine if the graph is symmetric with respect to the x-axis, y-axis, or the origin. Select all that apply.

- A. The graph is symmetric with respect to the origin.
- B. The graph is symmetric with respect to the x-axis.
- C. The graph is symmetric with respect to the y-axis.
- D. The graph has no symmetry.
- E. The graph is not that of a function.

Answers A. Yes, the graph is a function because every vertical line intersects the graph in at most one point.

A. The domain is . The range is .

(Type your answers in interval notation. Use integers or fractions for any numbers in the expressions.)

A. The intercept(s) is/are . (Type an ordered pair. Use a comma to separate answers as needed.)

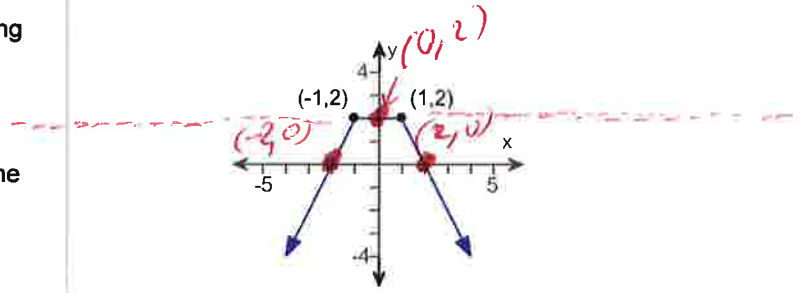
D. The graph has no symmetry.

ID: 1.2.19

---



7. Determine whether the graph is that of a function by using the vertical-line test. If it is, use the graph to find
- its domain and range.
  - the intercepts, if any.
  - any symmetry with respect to the x-axis, y-axis, or the origin.



Is the graph that of a function?

- Yes  
 No

If the graph is that of a function, what are the domain and range of the function? Select the correct choice below and fill in any answer boxes within your choice.

- A. The domain is  $(-\infty, \infty)$ . The range is  $(-\infty, 2]$ .  
 (Type your answers in interval notation.)
- B. The graph is not a function.

What are the intercepts? Select the correct choice below and fill in any answer boxes within your choice.

- A.  $(-2, 0), (2, 0), (0, 2)$   
 (Type an ordered pair. Use a comma to separate answers as needed.)
- B. There are no intercepts.
- C. The graph is not a function.

Determine if the graph is symmetrical.

- A. It is symmetrical with respect to the x-axis.
- B. It is symmetrical with respect to the origin.
- C. It is symmetrical with respect to the y-axis.
- D. The graph is not symmetrical.
- E. The graph is not a function.

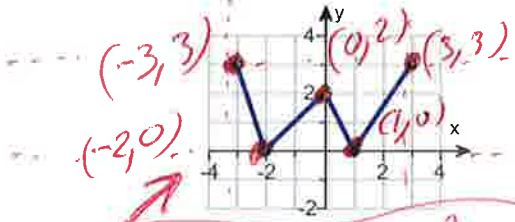
Answers Yes

- A. The domain is  $(-\infty, \infty)$ . The range is  $(-\infty, 2]$ . (Type your answers in interval notation.)
- A.  $(2, 0), (-2, 0), (0, 2)$  (Type an ordered pair. Use a comma to separate answers as needed.)
- C. It is symmetrical with respect to the y-axis.

ID: 1.2.21

8. Using the given graph of the function  $f$ , find the following.

- (a) the intercepts, if any
- (b) its domain and range
- (c) the intervals on which it is increasing, decreasing, or constant
- (d) whether it is even, odd, or neither



(a) What are the intercepts?

(Simplify your answer. Type an ordered pair. Use a comma to separate answers as needed.)

(b) The domain is    
 (Type your answer in interval notation.)

The range is    
 (Type your answer in interval notation.)

(c) On which interval(s) is the graph increasing? Select the correct choice below and fill in any answer boxes within your choice.

- A. The graph is increasing on     
 (Type your answer in interval notation. Use a comma to separate answers as needed.)
- B. The graph is not increasing on any interval.

On which interval(s) is the graph decreasing? Select the correct choice below and fill in any answer boxes within your choice.

- A. The graph is decreasing on     
 (Type your answer in interval notation. Use a comma to separate answers as needed.)
- B. The graph is not decreasing on any interval.

On which interval(s) is the graph constant? Select the correct choice below and fill in any answer boxes within your choice.

- A. The graph is constant on \_\_\_\_\_   
 (Type your answer in interval notation. Use a comma to separate answers as needed.)
- B. The graph is not constant on any interval.

(d) The function is (1)

- (1)  odd.
- even.
- neither odd nor even.

*Favorite hamburger place to eat a double meat, double cheese, double bacon with unsweet tea at 236 am on Saturday night.*

*then go home and work out.*

Answers  $(-2,0),(1,0),(0,2)$

$[-3,3]$

$[0,3]$

A. The graph is increasing on  $[-2,0],[1,3]$ .

(Type your answer in interval notation. Use a comma to separate answers as needed.)

A. The graph is decreasing on  $[-3,-2],[0,1]$ .

(Type your answer in interval notation. Use a comma to separate answers as needed.)

B. The graph is not constant on any interval.

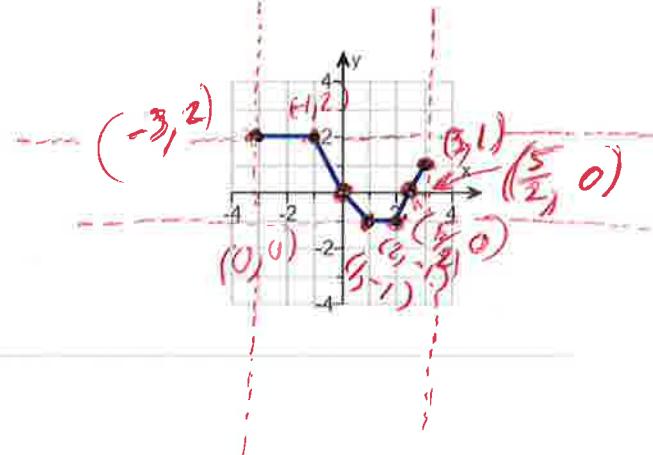
(1) neither odd nor even.

ID: 1.3.25

---

9. Using the given graph of the function  $f$ , find the following.

- (a) the intercepts, if any
- (b) its domain and range
- (c) the intervals on which it is increasing, decreasing, or constant
- (d) whether it is even, odd, or neither



Both y-intercept  
 (0, 0)  
 x-intercept  
 (5/2, 0)

(a) What are the intercepts?

(Simplify your answer. Type an ordered pair. Use a comma to separate answers as needed.)

(b) The domain is  $[-3, 3]$   
 (Type your answer in interval notation.)

The range is  $[-1, 2]$   
 (Type your answer in interval notation.)

(c) On which interval(s) is the graph increasing? Select the correct choice below and fill in any answer boxes within your choice.

- A. The graph is increasing on  $[2, 3]$   
 (Type your answer in interval notation. Use a comma to separate answers as needed.)
- B. The graph is not increasing on any interval.

On which interval(s) is the graph decreasing? Select the correct choice below and fill in any answer boxes within your choice.

- A. The graph is decreasing on  $[-1, 1]$   
 (Type your answer in interval notation. Use a comma to separate answers as needed.)
- B. The graph is not decreasing on any interval.

On which interval(s) is the graph constant? Select the correct choice below and fill in any answer boxes within your choice.

- A. The graph is constant on  $[-3, -1]$   $[1, 2]$   
 (Type your answer in interval notation. Use a comma to separate answers as needed.)
- B. The graph is not constant on any interval.

(d) The function is (1)

- (1)  even.
- odd.
- neither odd nor even.



Answers  $(0,0)$ ,  $\left(\frac{5}{2},0\right)$

$[-3,3]$

$[-1,2]$

A. The graph is increasing on .

(Type your answer in interval notation. Use a comma to separate answers as needed.)

A. The graph is decreasing on .

(Type your answer in interval notation. Use a comma to separate answers as needed.)

A. The graph is constant on .

(Type your answer in interval notation. Use a comma to separate answers as needed.)

(1) neither odd nor even.

ID: 1.3.31

---

10. The function  $f$  is defined as follows.

$$f(x) = \begin{cases} -3x + 4 & \text{if } x < 1 \\ 2x - 1 & \text{if } x \geq 1 \end{cases}$$

- (a) Find the domain of the function.
- (b) Locate any intercepts.
- (c) Graph the function.
- (d) Based on the graph, find the range.

(a) The domain of the function  $f$  is  $(-\infty, \infty)$  ← (left, right)  
 (Type your answer in interval notation.)

(b) Locate any intercepts. Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

- A. The intercept(s) is/are  $(0, 4)$ .  
 (Type an ordered pair. Use a comma to separate answers as needed.)
- B. There are no intercepts.

(c) Choose the correct graph below.

A.

B.

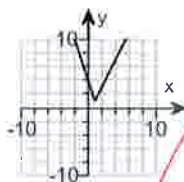
C.

D.

(d) The range of the function  $f$  is  $[1, \infty)$  ← (bottom, top)

Answers  $(-\infty, \infty)$

A. The intercept(s) is/are  $(0, 4)$ .  
 (Type an ordered pair. Use a comma to separate answers as needed.)



D.  
 $[1, \infty)$

ID: 1.4.33

Window  
 $x\text{-min} = -12$   
 $x\text{-max} = 12$   
 $y\text{-min} = -10$   
 $y\text{-max} = 10$

Use graphing calculator

$y_1 = -3x + 4 \div (x < 1)$  OPEN circle  
 $y_2 = 2x - 1 \div (x \geq 1)$  CLOSE circle  
 BIG

11. The function  $f$  is defined as follows.

✓ 
$$f(x) = \begin{cases} 1+x & \text{if } x < 0 \\ x^2 & \text{if } x \geq 0 \end{cases}$$

- (a) Find the domain of the function.
- (b) Locate any intercepts.
- (c) Graph the function.
- (d) Based on the graph, find the range.

(a) The domain of the function  $f$  is  $(-\infty, \infty)$  ← (left, right)  
 (Type your answer in interval notation.)

(b) Locate any intercepts. Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

- A. The intercept(s) is/are  $(-1, 0), (0, 0)$  ←  $x$ -intercept &  $y$ -intercept (Both)
- B. There are no intercepts.

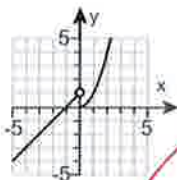
→ (c) Choose the correct graph of  $f(x)$  below.

A. OPEN circle at  $(0, 1)$   B.  C.  D.

(d) The range of the function  $f$  is  $(-\infty, \infty)$  ← (bottom, top)  
 (Type your answer in interval notation.)

Answers  $(-\infty, \infty)$

A. The intercept(s) is/are  $(-1, 0), (0, 0)$ .  
 (Type an ordered pair. Use a comma to separate answers as needed.)



A.  
 $(-\infty, \infty)$

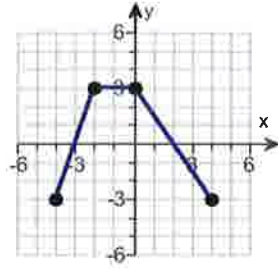
ID: 1.4.37

Window  
 $x$ -min = -12  
 $x$ -max = 12  
 $y$ -min = -10  
 $y$ -max = 10

Use graphing calculator

2nd Math  
 $y_1 = 1+x$  (x < 0) OPEN Circle  
 $y_2 = x^2$  (x ≥ 0) CLOSE Circle

12. The graph of a function  $f$  is illustrated to the right. Use the graph of  $f$  as the first step toward graphing each of the following functions.



- (a)  $F(x) = f(x) + 2$
- (b)  $G(x) = f(x + 3)$
- (c)  $P(x) = -f(x)$
- (d)  $H(x) = f(x + 2) - 3$
- (e)  $Q(x) = \frac{1}{3}f(x)$
- (f)  $g(x) = f(-x)$
- (g)  $h(x) = f(2x)$

(a) Choose the correct graph of  $F(x) = f(x) + 2$  below.

A.  B.  C.  D.

(b) Choose the correct graph of  $G(x) = f(x + 3)$  below.

A.  B.  C.  D.

(c) Choose the correct graph of  $P(x) = -f(x)$  below.

A.  B.  C.  D.

(d) Choose the correct graph of  $H(x) = f(x + 2) - 3$  below.

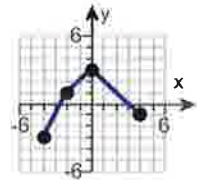
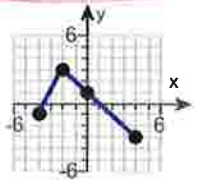
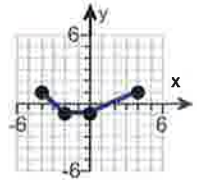
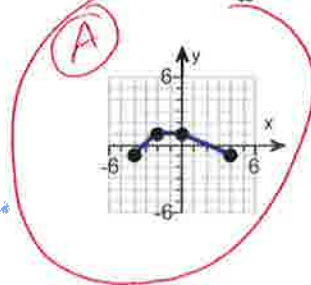
A.  B.  C.  D.

*Handwritten notes: "Shift left -2", "Shift down -3", "Opposite".*

(e) Choose the correct graph of  $Q(x) = \frac{1}{3}f(x)$  below.

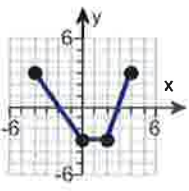


$Q(x) = \frac{1}{3} f(x)$

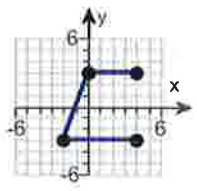


(f) Choose the correct graph of  $g(x) = f(-x)$  below.

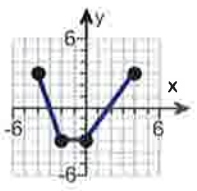
A.



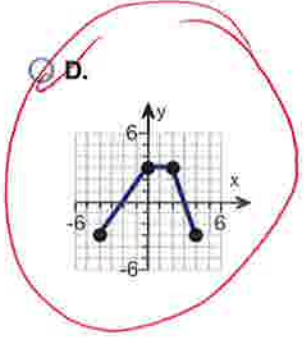
B.



C.

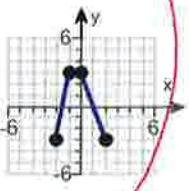


D.

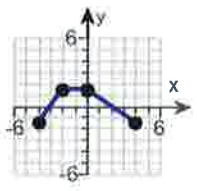


(g) Choose the correct graph of  $h(x) = f(2x)$  below.

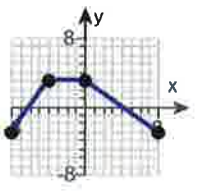
A.



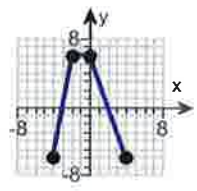
B.



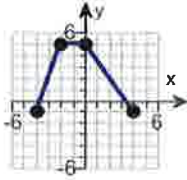
C.



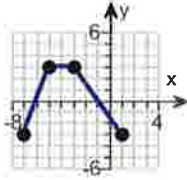
D.



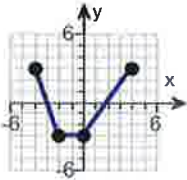
Answers



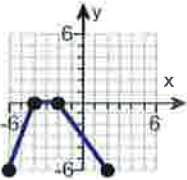
A.



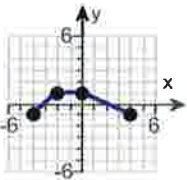
D.



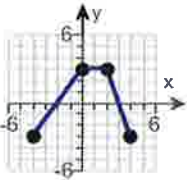
B.



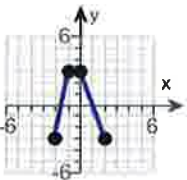
B.



A.



D.



A.

ID: 1.5.63

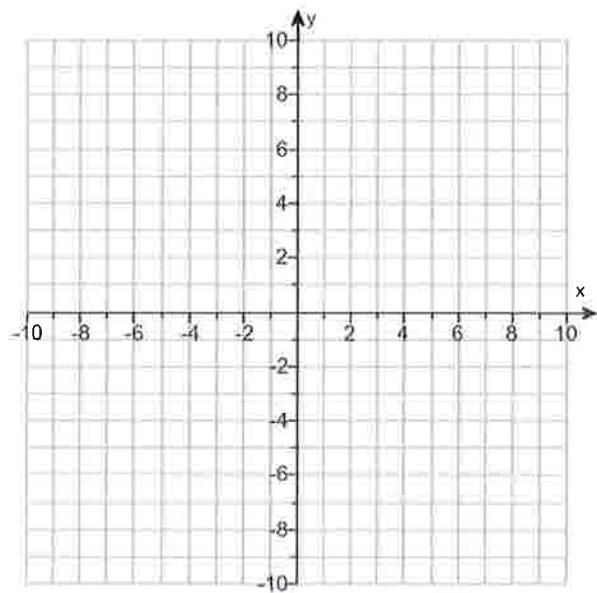
13.

- (a) Graph  $f(x) = |x + 5| - 2$  using transformations.
- (b) Find the area of the region bounded by  $f$  and the  $x$ -axis that lies below the  $x$ -axis.

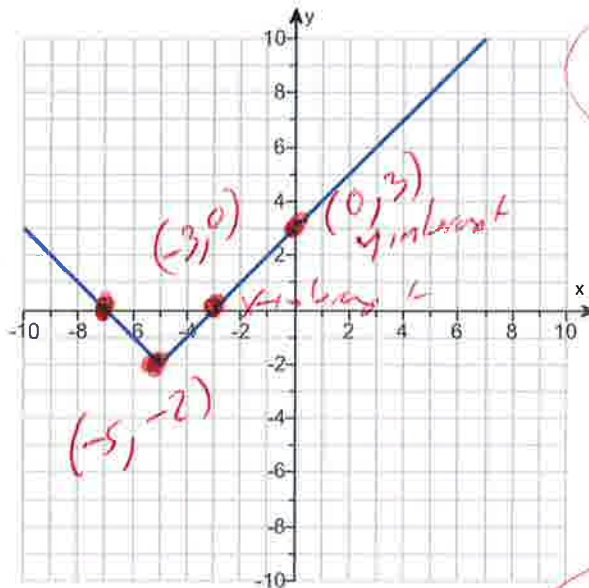
(a) Graph  $f(x)$ .

(Use the graphing tool provided to graph the function.)

(b) The area of the region bounded by  $f$  and the  $x$ -axis is  square units.  
(Simplify your answer.)



Answers



$$f(x) = |x + 5| - 2$$

x	f(x)
-7	0
-5	-2
-3	0
0	3

4

ID: 1.5.81

Window  
 $x$ -min = -12  
 $x$ -max = 12  
 $y$ -min = -10  
 $y$ -max = 10

Use graphing calculator

$y_1 = \text{Math, num, abs}$

$$y_1 = \text{abs}(x + 5) - 2$$

BIG

14. Solve the following equation using the quadratic formula.

$$3x^2 - x - 2 = 0$$

$a=3, b=-1, c=-2$

The solution set is

(Type an exact answer, using radicals and  $i$  as needed. Use integers or fractions for any numbers in the expression. Use a comma to separate answers as needed.)

Answer:  $1, -\frac{2}{3}$

ID: Quick Check P2.2.2

Handwritten work for problem 14:

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} = \frac{-(-1) \pm \sqrt{(-1)^2 - 4(3)(-2)}}{2(3)} = \frac{1 \pm \sqrt{1 + 24}}{6} = \frac{1 \pm \sqrt{25}}{6} = \frac{1 \pm 5}{6}$$

$x = \frac{1+5}{6} = \frac{6}{6} = 1$  OR  $x = \frac{1-5}{6} = \frac{-4}{6} = -\frac{2}{3}$   
 $x = -1$  OR  $x = -\frac{2}{3}$

15. Find the zeros, if any, of the quadratic function using the quadratic formula. What are the x-intercepts, if any, of the graph of the function?

$$f(x) = 2x^2 + 3 + 6x$$

$f(x) = 2x^2 + 6x + 3$   
 $a=2, b=6, c=3$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} = \frac{-(6) \pm \sqrt{(6)^2 - 4(2)(3)}}{2(2)} = \frac{-6 \pm \sqrt{36 - 24}}{4} = \frac{-6 \pm \sqrt{12}}{4}$$

Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

(Simplify your answer, including any radicals. Use integers or fractions for any numbers in the expression. Use a comma to separate answers as needed.)

- A. The zeros and the x-intercepts are the same. They are
- B. The zeros and the x-intercepts are different. The zeros are , the x-intercepts are
- C. There is no real zero solution and no x-intercept.

Answer: A. The zeros and the x-intercepts are the same. They are

$$\frac{-3 + \sqrt{3}}{2}, \frac{-3 - \sqrt{3}}{2}$$

ID: 2.3.47

Handwritten work for problem 15:

$$x = \frac{-3 + \sqrt{3}}{2} \text{ OR } x = \frac{-3 - \sqrt{3}}{2}$$

$$= \frac{-6 \pm \sqrt{12}}{4} = \frac{-6 \pm \sqrt{4 \cdot 3}}{4} = \frac{-6 \pm 2\sqrt{3}}{4} = \frac{-3 \pm \sqrt{3}}{2} = \frac{2(-3 \pm \sqrt{3})}{2(2)}$$

16. Find the real zeros of the function. What are the x-intercepts of the graph of the function?

$$g(x) = x + 2\sqrt{x} - 15$$

Select the correct choice below and fill in the answer box to complete your choice.

- A. The zeros and the x-intercepts are the same. They are
- B. The zeros and the x-intercepts are different. The zeros are , the x-intercepts are

(Simplify your answer, including any radicals. Use integers or fractions for any numbers in the expression. Use a comma to separate answers as needed.)

Answer: A. The zeros and the x-intercepts are the same. They are

ID: 2.3.75



16

part 1

$$x + 2\sqrt{x} - 15 = 0$$

$$x - 15 = -2\sqrt{x} \quad \text{rewrite}$$

$$(x - 15)^2 = (-2\sqrt{x})^2 \quad \text{Square Both Sides}$$

$$(x - 15)(x - 15) = (-2)^2(\sqrt{x})^2$$

$$x^2 - 15x - 15x + 225 = (-2)(-2)(\sqrt{x})^2$$

$$x^2 - 30x + 225 = (4)(x)$$

$$x^2 - 30x + 225 = 4x$$

$$x^2 - 30x + 225 - 4x = 0$$

$$x^2 - 34x + 225 = 0$$

$$(x - 9)(x - 25) = 0$$

$$x - 9 = 0 \quad \text{OR} \quad x - 25 = 0$$

$$x - 9 + 9 = 0 + 9 \quad \text{OR} \quad x - 25 + 25 = 0 + 25$$

$$x = 9$$

$$x = 25$$

$$\text{try } x = 9$$

check

$$x + 2\sqrt{x} - 15 = 0$$

$$(9) + 2\sqrt{9} - 15 = 0$$

$$9 + 2(3) - 15 = 0$$

$$9 + 6 - 15 = 0$$

$$15 - 15 = 0$$

$$0 = 0$$



(10) part 2

Good

try  $x = 25$

$$x + 2\sqrt{x} - 15 = 0$$

$$(25) + 2\sqrt{25} - 15 = 0$$

$$25 + 2(5) - 15 = 0$$

$$25 + 10 - 15 = 0$$

$$35 - 15 = 0$$

$$20 \neq 0$$

**BAD**



Answer

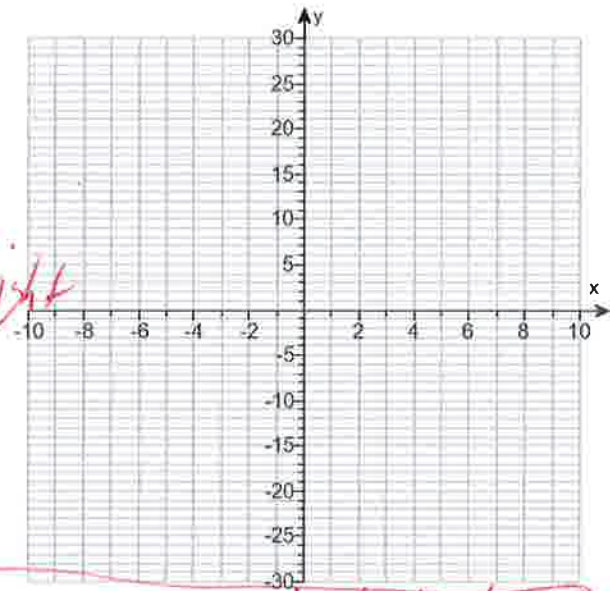
$$x = 9$$

only

17.

Graph the function  $f(x) = -x^2 - 6x$  by starting with the graph of  $y = x^2$  and using transformations (shifting, stretching/compressing, and/or reflecting).

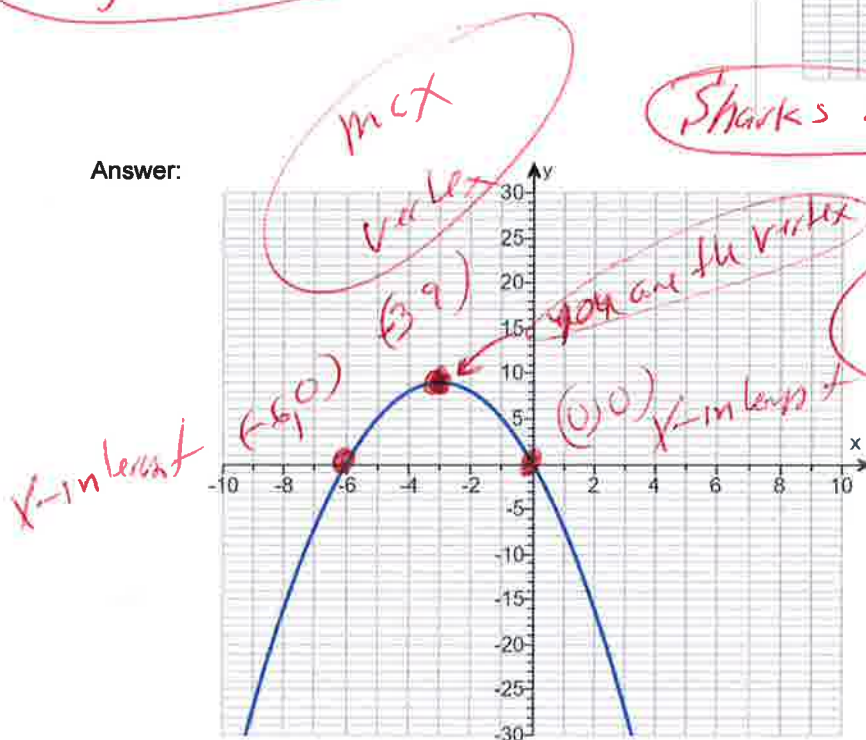
Use the graphing tool to graph the function.



Example like swimming in the ocean at 2:34 am on Saturday night by yourself

Sharks never eat at night

Answer:



$f(x) = -x^2 - 6x$

x	f(x)
-6	0
-3	9
0	0

ID: 2.4.29

Window  
 $x_{\min} = -12$   
 $x_{\max} = 12$   
 $y_{\min} = -10$   
 $y_{\max} = 10$

Use graphing calculator with  $y = -x^2 - 6x$



SMART Bird 5-7-17  
MARI

$$\frac{1}{3} \times \frac{4}{4} = \frac{4}{12}, \quad \frac{2}{4} \times \frac{3}{3} = \frac{6}{12}$$



$$\frac{4}{12} + \frac{6}{12} = \frac{10}{12} = \frac{5}{6}$$

$$\frac{12}{12} - \frac{10}{12} = \frac{2}{12} \text{ or } \frac{1}{6}$$

MATH IS FUN



18. For the quadratic function  $f(x) = x^2 - 4x - 5$ , answer parts (a) through (c).

(a) Graph the quadratic function by determining whether its graph opens up or down and by finding its vertex, axis of symmetry, y-intercept, and x-intercepts, if any.

Does the graph of  $f$  open up or down?

- down  
 up

What are the coordinates of the vertex?

The vertex of the parabola is .

(Type an ordered pair. Use integers or fractions for any numbers in the expression.)

What is the equation of the axis of symmetry?

The axis of symmetry is .

(Type an equation.)

What is/are the x-intercept(s)? Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

- A. The x-intercept(s) is/are

(Type an integer or a decimal. Use a comma to separate answers as needed.)

- B. There are no x-intercepts.

What is the y-intercept? Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

- A. The y-intercept is .

(Type an integer or a decimal.)

- B. There is no y-intercept.

Use the graphing tool to graph the function.

(b) Determine the domain and the range of the function.

The domain of  $f$  is .

(Type your answer in interval notation.)

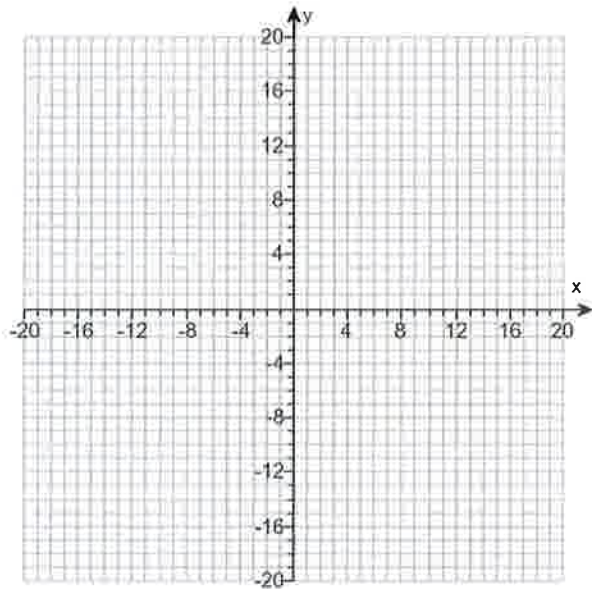
The range of  $f$  is .

(Type your answer in interval notation.)

(c) Determine where the function is increasing and where it is decreasing.

The function is increasing on the interval .

(Type your answer in interval notation.)



Answers up

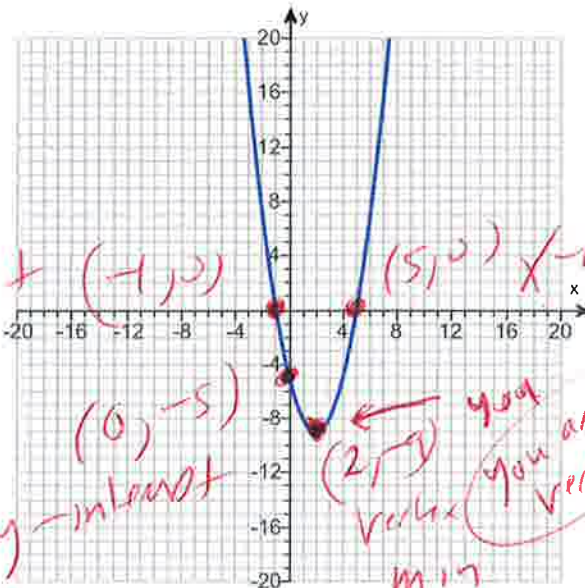
(2, -9)

x = 2

A. The x-intercept(s) is/are .

(Type an integer or a decimal. Use a comma to separate answers as needed.)

A. The y-intercept is . (Type an integer or a decimal.)



sharks always sleep at night.

Example Like swimming in the sea at 239 am on Saturday night by yourself after eating a double meat, double cheese, double bacon Hamburger with a diet soda.

$f(x) = x^2 - 4x - 5$

use graphing calculator

x	f(x)
-1	0
0	-5
2	-9
5	0

$(-\infty, \infty)$

$[-9, \infty)$

$[2, \infty)$

$(-\infty, 2]$

Window  
~~x~~-min = -12  
 x-max = 12  
~~y~~-min = -10  
 y-max = 10

Vertex

$y_1 = x^2 - 4x - 5$

ID: 2.4.37

19.

For the quadratic function  $f(x) = -2x^2 - 2x - 3$ , answer parts (a) through (c). Verify the results using a graphing utility.

(a) Graph the quadratic function by determining whether its graph opens up or down and by finding its vertex, axis of symmetry, y-intercept, and x-intercepts, if any.

The graph of  $f$  opens (1)

The vertex of  $f$  is .  
(Type an ordered pair.)

The axis of symmetry is .  
(Type an equation. Simplify your answer.)

Determine the y-intercept. Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

A. The y-intercept is .  
(Type an integer or a decimal.)

B. There is no y-intercept.

Determine the x-intercept(s). Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

A. The x-intercept(s) is/are .  
(Type an integer or a decimal rounded to two decimal places as needed. Use a comma to separate answers as needed.)

B. There is no x-intercept.

Use the graphing tool to graph the function.

(b) Determine the domain and the range of the function.

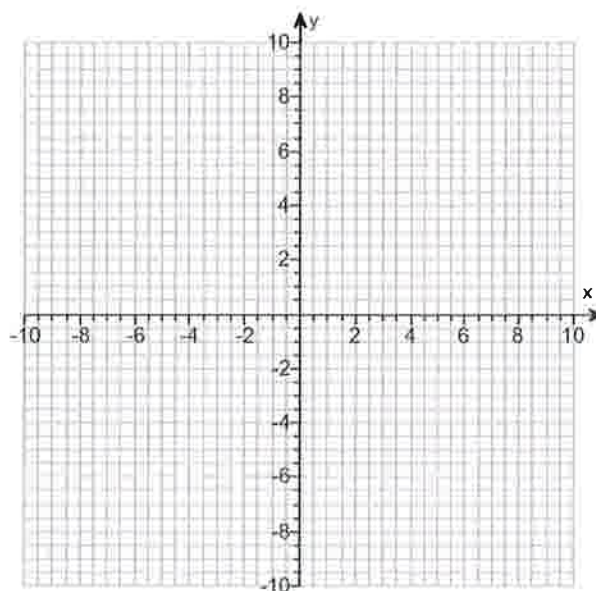
The domain of  $f$  is .  
(Type your answer in interval notation.)

The range of  $f$  is .  
(Type your answer in interval notation.)

(c) Determine where the function is increasing and where it is decreasing.

The function is increasing on the interval .  
(Type your answer in interval notation.)

The function is decreasing on the interval .  
(Type your answer in interval notation.)





- (1)  up.  
 down.

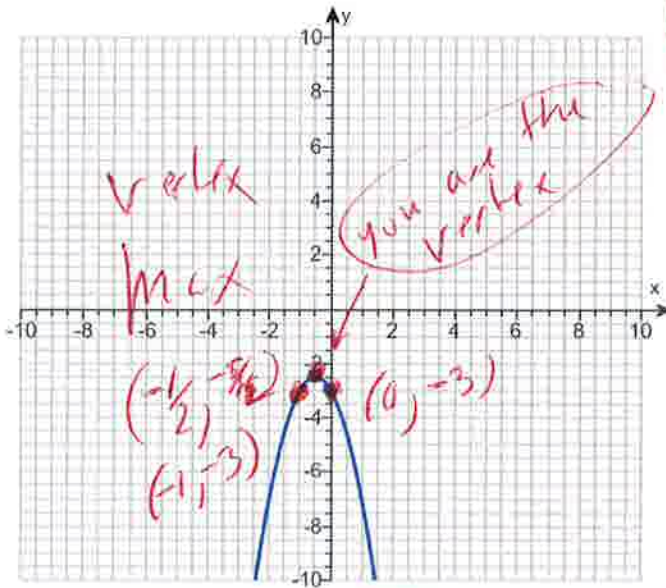
Answers (1) down.

$$\left(-\frac{1}{2}, -\frac{5}{2}\right)$$

$$x = -\frac{1}{2}$$

A. The y-intercept is . (Type an integer or a decimal.)

B. There is no x-intercept.



Example. Only swim in the ocean at 236 am by yourself for 2 hours max OR you could get leg and arm cramps.

Sharks eat in the day and sleep at night.  
 Shark Law

$$f(x) = -2x^2 - 2x - 3$$

use graphing calculator

x	f(x)
-1	-3
-1/2	-5/2
0	-3

- $(-\infty, \infty)$
- $\left[-\infty, -\frac{5}{2}\right]$
- $\left[-\infty, -\frac{1}{2}\right]$
- $\left[-\frac{1}{2}, \infty\right)$

Window  
 $x\text{-min} = -12$   
 $x\text{-max} = 12$   
 $y\text{-min} = -10$   
 $y\text{-max} = 10$

ID: 2.4.43

$$y_1 = -2x^2 - 2x - 3$$

BIG      2x      BIG



20. Determine without graphing, whether the given quadratic function has a maximum value or a minimum value and then find the value.

$f(x) = -2x^2 + 16x - 4$

Does the quadratic function  $f$  have a minimum value or a maximum value?

- The function  $f$  has a maximum value.
- The function  $f$  has a minimum value.

What is this minimum or maximum value?

(Simplify your answer.)

Answers The function  $f$  has a maximum value.

28

ID: 2.4.59

*Since you have a negative then graph opens down (MAX)*

$a = -2, b = 16$

$MAX = Vertex = (-\frac{b}{2a}, f(-\frac{b}{2a}))$

$Vertex = (-\frac{16}{2(-2)}, f(-\frac{16}{2(-2)}))$

$Vertex = (-\frac{16}{-4}, f(-\frac{16}{-4}))$

$Vertex = (4, f(4))$

$Vertex = (4, -2(4)^2 + 16(4) - 4)$

$Vertex = (4, -2(16) + 64 - 4)$

$Vertex = (4, -32 + 64 - 4)$

$Vertex = (4, 32 - 4)$

$Vertex = (4, 28)$

**Max ✓✓**

21. Find the vertical, horizontal, and oblique asymptotes, if any, for the following rational function.

$R(x) = \frac{12x}{x+2}$

Select the correct choice below and fill in any answer boxes within your choice.

- A. The vertical asymptote(s) is/are  $x =$  \_\_\_\_\_ (Use a comma to separate answers as needed.)
- B. There is no vertical asymptote.

Select the correct choice below and fill in any answer boxes within your choice.

- A. The horizontal asymptote(s) is/are  $y =$  \_\_\_\_\_ (Use a comma to separate answers as needed.)
- B. There is no horizontal asymptote.

Select the correct choice below and fill in any answer boxes within your choice.

- A. The oblique asymptote(s) is/are  $y =$  \_\_\_\_\_ (Use a comma to separate answers as needed.)
- B. There is no oblique asymptote.

Answers A. The vertical asymptote(s) is/are  $x =$   (Use a comma to separate answers as needed.)

A. The horizontal asymptote(s) is/are  $y =$   (Use a comma to separate answers as needed.)

B. There is no oblique asymptote.

ID: 3.4.45

*sub  $x+2=0$*

*$x+2-2=0-2$*

*$x=-2$*

**Vertical asymptote  $x = -2$  ✓✓**

$\frac{12x}{x} = \frac{\text{highest power top}}{\text{highest power bottom}}$

$\frac{12}{1} = \text{Simplify}$

$12 =$

**$y = 12$  horizontal asymptote ✓✓**

*Since highest power top is same as highest power bottom then there is no oblique ✓✓*

22. For  $f(x) = 9x + 6$  and  $g(x) = 4x$ , find the following composite functions and state the domain of each.

- (a)  $f \circ g$       (b)  $g \circ f$       (c)  $f \circ f$       (d)  $g \circ g$

 (a)  $(f \circ g)(x) =$   (Simplify your answer.)

Select the correct choice below and fill in any answer boxes within your choice.

- A. The domain of  $f \circ g$  is  $\{x \mid \underline{\hspace{2cm}}\}$ .  
(Type an inequality. Use integers or fractions for any numbers in the expression. Use a comma to separate answers as needed.)
- B. The domain of  $f \circ g$  is all real numbers.

 (b)  $(g \circ f)(x) =$   (Simplify your answer.)

Select the correct choice below and fill in any answer boxes within your choice.

- A. The domain of  $g \circ f$  is  $\{x \mid \underline{\hspace{2cm}}\}$ .  
(Type an inequality. Use integers or fractions for any numbers in the expression. Use a comma to separate answers as needed.)
- B. The domain of  $g \circ f$  is all real numbers.

(c)  $(f \circ f)(x) =$   (Simplify your answer.)

Select the correct choice below and fill in any answer boxes within your choice.

- A. The domain of  $f \circ f$  is  $\{x \mid \underline{\hspace{2cm}}\}$ .  
(Type an inequality. Use integers or fractions for any numbers in the expression. Use a comma to separate answers as needed.)
- B. The domain of  $f \circ f$  is all real numbers.

(d)  $(g \circ g)(x) =$   (Simplify your answer.)

Select the correct choice below and fill in any answer boxes within your choice.

- A. The domain of  $g \circ g$  is  $\{x \mid \underline{\hspace{2cm}}\}$ .  
(Type an inequality. Use integers or fractions for any numbers in the expression. Use a comma to separate answers as needed.)
- B. The domain of  $g \circ g$  is all real numbers.

Answers  $36x + 6$

B. The domain of  $f \circ g$  is all real numbers.

$36x + 24$

B. The domain of  $g \circ f$  is all real numbers.

$81x + 60$

B. The domain of  $f \circ f$  is all real numbers.

$16x$

B. The domain of  $g \circ g$  is all real numbers.

ID: 4.1.23

(22) a  $f(x) = 9x + 6$  and  $g(x) = 4x$

$$(f \circ g)(x) =$$

$$f(g(x)) =$$

$$f(4x) =$$

$$9(4x) + 6 =$$

$$36x + 6 =$$

domain

$$(-\infty, \infty)$$

(22) b  $f(x) = 9x + 6$  and  $g(x) = 4x$

$$(g \circ f)(x) =$$

$$g(f(x)) =$$

$$g(9x + 6) =$$

$$4(9x + 6) =$$

$$36x + 24 =$$

domain

$$(-\infty, \infty)$$

23

inside itself

$$\textcircled{22} \subset f(x) = (9x+6) \text{ and } g(x) = 4x$$

$$(f \circ f)(x) =$$

$$f(f(x)) =$$

$$f(9x+6) =$$

$$9(9x+6) + 6 =$$

$$81x + 54 + 6 =$$

$$81x + 60 =$$

domain

$$(-\infty, \infty)$$

inside itself

$$\textcircled{22} \downarrow f(x) = 9x+6 \text{ and } g(x) = 4x$$

$$(g \circ g)(x) =$$

$$g(g(x)) =$$

$$g(4x) =$$

$$4(4x) =$$

$$16x =$$

domain

$$(-\infty, \infty)$$



23.

The function  $f(x) = 12x + 4$  is one-to-one.

- (a) Find the inverse of  $f$  and check the answer.
- (b) Find the domain and the range of  $f$  and  $f^{-1}$ .
- (c) Graph  $f$ ,  $f^{-1}$ , and  $y = x$  on the same coordinate axes.

(a)  $f^{-1}(x) =$

(Simplify your answer. Use integers or fractions for any numbers in the expression.)

(b) Find the domain of  $f$ . Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

- A. The domain is  $\{x|x \neq \underline{\hspace{2cm}}\}$ .
- B. The domain is  $\{x|x \leq \underline{\hspace{2cm}}\}$ .
- C. The domain is  $\{x|x \geq \underline{\hspace{2cm}}\}$ .
- D. The domain is the set of all real numbers.

Find the range of  $f$ . Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

- A. The range is  $\{y|y \neq \underline{\hspace{2cm}}\}$ .
- B. The range is  $\{y|y \geq \underline{\hspace{2cm}}\}$ .
- C. The range is  $\{y|y \leq \underline{\hspace{2cm}}\}$ .
- D. The range is the set of all real numbers.

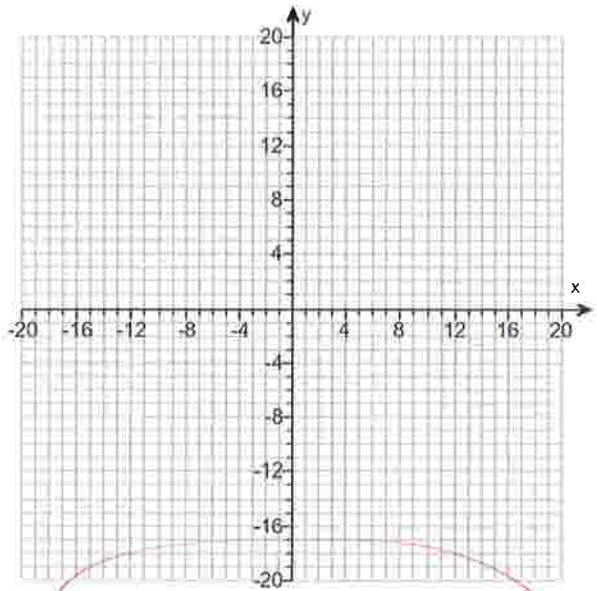
Find the domain of  $f^{-1}$ . Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

- A. The domain is  $\{x|x \neq \underline{\hspace{2cm}}\}$ .
- B. The domain is  $\{x|x \geq \underline{\hspace{2cm}}\}$ .
- C. The domain is  $\{x|x \leq \underline{\hspace{2cm}}\}$ .
- D. The domain is the set of all real numbers.

Find the range of  $f^{-1}$ . Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

- A. The range is  $\{y|y \neq \underline{\hspace{2cm}}\}$ .
- B. The range is  $\{y|y \leq \underline{\hspace{2cm}}\}$ .
- C. The range is  $\{y|y \geq \underline{\hspace{2cm}}\}$ .
- D. The range is the set of all real numbers.

(c) Graph  $f$ ,  $f^{-1}$ , and  $y = x$  on the same coordinate axes. Use the graphing tool to graph the functions.



Handwritten work in red ink:

$f(x) = 12x + 4$

$y = 12x + 4$

Set  $y =$

$x = 12y + 4$  (Note: "no var" written next to this line)

$-4 = 12y + 4 - 4$

$x - 4 = 12y$

$x - 4 = \frac{12y}{12}$

$\frac{x-4}{12} = y$

$y = \frac{x-4}{12}$

$f^{-1}(x) = \frac{x-4}{12}$

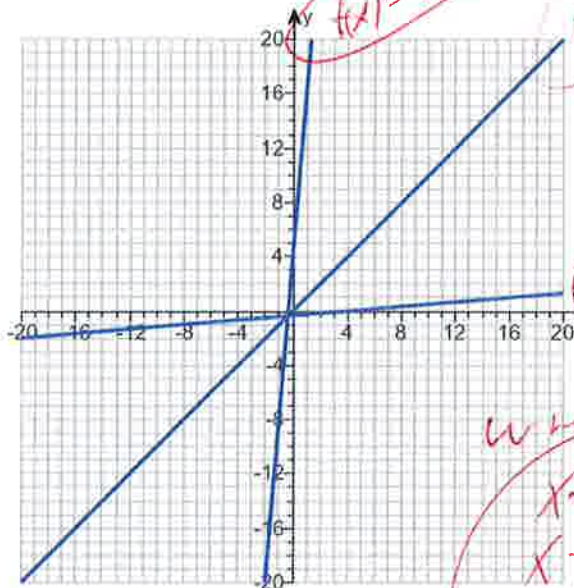
Set  $x =$

Solve for  $y$

INVERSE

Answers  $\frac{x-4}{12}$

- D. The domain is the set of all real numbers.
- D. The range is the set of all real numbers.
- D. The domain is the set of all real numbers.
- D. The range is the set of all real numbers.



Handwritten notes in red ink:

- $y_1 = 12x + 4$
- $y_2 = x$
- $f(x) = 12x + 4$
- $f^{-1}(x) = \frac{x-4}{12}$
- $y_3 = (x-4) \div 12$
- Use graphing calculator
- Window:
  - $x\text{-min} = -12$
  - $x\text{-max} = 12$
  - $y\text{-min} = -12$
  - $y\text{-max} = 10$

ID: 4.2.53

24. Solve the equation.

$8^{-x+33} = 256^x$

The solution set is  (Type an integer or a simplified fraction. Use a comma to separate answers as needed.)

Answer: 9

ID: 4.3.73

Handwritten work for problem 24:

- $(2)^{-x+33} = (2^8)^x$  (rewrite)
- $2^{-3x+99} = 2^{8x}$
- $-11x = -99$
- $\frac{-11x}{-11} = \frac{-99}{-11}$
- $x = 9$

25. Find the domain of the function.

$h(x) = \ln(x-1)$

The domain of h is  (Type your answer in interval notation.)

Answer: (1,∞)

ID: 4.4.39

Handwritten work for problem 25:

- Let  $x-1 > 0$  only
- $x-1+1 > 0+1$
- $x > 1$
- formal domain:  $f(x) = \ln(A+B)$  let  $A+B > 0$  only
- $(1, \infty)$



26. Solve the equation.

$\log_2(2x + 3) = 3$

Change the given logarithmic equation to exponential form.

(Type an equation. Do not simplify.)

The solution set is .

(Simplify your answer. Use a comma to separate answers as needed.)

Answers  $2x + 3 = 2^3$

$\frac{5}{2}$

$\log_2(2x+3) = 3$   
 $2^3 = 2x+3$  Rewrite

$2 \cdot 2 \cdot 2 = 2x+3$   
 $8 = 2x+3$   
 $8-3 = 2x+3-3$   
 $5 = 2x$   
 $\frac{5}{2} = \frac{2x}{2}$

$\frac{5}{2} = x$  ✓

ID: 4.4.91-Setup & Solve

27. Solve the equation. Write the answer in terms of the natural logarithm.

$5e^{0.5x} = 7 \rightarrow \frac{5e^{0.5x}}{5} = \frac{7}{5}$

The solution set is .

(Type an exact answer. Simplify your answer. Use a comma to separate answers as needed.)

Answer:  $\frac{\ln 1.4}{0.5}$

$e^{0.5x} = 1.4$   
 $\ln(e^{0.5x}) = \ln(1.4)$   
 $0.5x \ln(e) = \ln(1.4)$   
 $0.5x(1) = \ln(1.4)$

$0.5x = \ln(1.4)$   
 $\frac{0.5x}{0.5} = \frac{\ln(1.4)}{0.5}$   
 $x = \frac{\ln(1.4)}{0.5}$   
 $x = .67294497342$   
 $x = .6729$  ✓

ID: 4.4.109

28. The formula

$D = 50e^{-0.5h} \rightarrow 4 = 50e^{-0.5h}$

formula  $\ln(A^N) = N \ln A$   
 $\ln(e) = 1$

can be used to find the number of milligrams D of a certain drug that is in a patient's bloodstream h hours after the drug was administered. When the number of milligrams reaches 4, the drug is to be administered again. What is the time between injections?

The time between injections is  hour(s).

(Type an integer or a decimal rounded to two decimal places as needed.)

Answer: 5.05

$\frac{4}{50} = \frac{50e^{-0.5h}}{50}$   
 $0.08 = e^{-0.5h}$

$\frac{\ln(0.08)}{-0.5} = \frac{-0.5h}{-0.5}$   
 $5.05145728762 = h$   
 $5.05 = h$  ✓

$\ln(0.08) = \ln(e^{-0.5h})$   
 $\ln(0.08) = -0.5h \ln(e)$   
 $\ln(0.08) = -0.5h(1)$   
 $\ln(0.08) = -0.5h$

29. Write the expression as a sum and/or difference of logarithms. Express powers as factors.

$\log \left[ \frac{x(x+7)}{(x+4)^3} \right], x > 0$

$\rightarrow \log(x(x+7)) - \log(x+4)^3 =$   
 $\log(x) + \log(x+7) - \log(x+4)^3 =$

$\log \left[ \frac{x(x+7)}{(x+4)^3} \right] = \text{[ ]}$  (Simplify your answer.)

$\log(x) + \log(x+7) - 3\log(x+4) =$

Answer:  $\log x + \log(x+7) - 3\log(x+4)$

formule  $\log\left(\frac{A}{B}\right) = \log A - \log B$  ✓  $\log(A^N) = N \log A$  ✓  
 $\log(AB) = \log A + \log B$  ✓

ID: 4.5.51

30. Solve the logarithmic equation.

$\log_5(x+9) = \log_5 11$

Determine the equation to be solved after removing the logarithm.

[ ]

(Type an equation. Do not simplify.)

Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

- A. The solution set is { [ ] }.  
(Simplify your answer. Type an exact answer. Use a comma to separate answers as needed.)
- B. There is no solution.

Answers  $x + 9 = 11$

- A. The solution set is {  }.  
(Simplify your answer. Type an exact answer. Use a comma to separate answers as needed.)

ID: 4.6.9-Setup & Solve

$\log_5(x+9) = \log_5(11)$

$x+9 = 11$

$x+9-9 = 11-9$

$x = 2$



31. Solve the logarithmic equation.

$\log x + \log(x + 15) = 2$

Determine the equation to be solved after removing the logarithm.

(Type an equation. Do not simplify.)

Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

A. The solution set is { } (Simplify your answer. Type an exact answer. Use a comma to separate answers as needed.)

B. There is no solution.

Answers  $x(x + 15) = 10^2$

A. The solution set is { 5 } (Simplify your answer. Type an exact answer. Use a comma to separate answers as needed.)

ID: 4.6.17-Setup & Solve

$\log(x)(x+15) = 2$   
 $10^2 = x(x+15)$

$100 = x^2 + 15x$   
 $0 = x^2 + 15x - 100$   
 $0 = (x-5)(x+20)$

Answer  
 $x = 5$   
 only

$x-5=0$  OR  $x+20=0$   
 $x-5+5=0+5$  OR  $x+20-20=0-20$   
 $x=5$  OR  $x=-20$  Check

formula  
 $\log(A) + \log(B) = \log(AB)$

$\log(5) + \log(5+15) = 2$   
 $\log(5) + \log(20) = 2$   
 $\log(-20) + \log(-20+15) = 2$   
 $\log(-20) + \log(-5) = 2$

32. Solve the following logarithmic equation.

$\log(4x + 3) = 1 + \log(x - 8)$

Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

A. The solution set is { } (Simplify your answer. Type an exact answer. Use a comma to separate answers as needed.)

B. There is no solution.

Answer: A. The solution set is {  $\frac{83}{6}$  } (Simplify your answer. Type an exact answer. Use a comma to separate answers as needed.)

ID: 4.6.19

$\log(4x+3) - \log(x-8) = 1$   
 $10x = 4x + 83$   
 $10x - 4x = 4x + 83 - 4x$   
 $6x = 83$   
 $\frac{6x}{6} = \frac{83}{6}$   
 $x = \frac{83}{6}$  Check

formula  $\log(A) - \log(B) = \log(\frac{A}{B})$   
 $10^1 = \frac{4x+3}{x-8}$

$10 = \frac{4x+3}{x-8}$   
 $1(x-8) = 4x+3$   
 $x-8 = 4x+3$   
 $x-8-4x = 4x+3-4x$   
 $-3x-8 = 3$   
 $-3x = 11$   
 $x = -\frac{11}{3}$  (BAD)

Gross mult  $\rightarrow 10(x-8) = 1(4x+3)$   
 $10x - 80 = 4x + 3$   
 $10x - 80 + 80 = 4x + 3 + 80$   
 $10x = 83 + 4x$   
 $10x - 4x = 83 + 4x - 4x$   
 $6x = 83$   
 $x = \frac{83}{6}$  ✓

33. Find the amount that results from the given investment.

\$300 invested at 8% compounded quarterly after a period of 2 years

After 2 years, the investment results in \$  (Round to the nearest cent as needed.)

Answer: 351.50

ID: 4.7.7

$A = P(1 + \frac{r}{n})^{nt}$

$P = 300$   
 $r = 8\% = 0.08$   
 $n = 4 = \text{Quarter}$   
 $t = 2 = \text{years}$



$A = 300(1 + \frac{0.08}{4})^{4(2)}$   
 $A = 300(1 + 0.02)^8$   
 $A = 300(1.02)^8$   
 $A = 351.497814301$  OR  
 $A = 351.50$  Round

Let  
100  
↓  
200  
double

34. How long does it take for an investment to double in value if it is invested at 5% compounded monthly? Compounded continuously?

At 5% compounded monthly, the investment doubles in about  years.  
(Round to two decimal places as needed.)

At 5% compounded continuously, the investment doubles in about  years.  
(Round to two decimal places as needed.)

Answers 13.89

13.86

ID: 4.7.35

$A = P(1 + \frac{r}{n})^{nt}$   $A = Pe^{rt}$

$200 = 100(1 + \frac{0.05}{12})^{12t}$   $2 = e^{0.05t}$

$\frac{200}{100} = \frac{100(1 + \frac{0.05}{12})^{12t}}{100}$   $\ln(2) = \ln e^{0.05t}$

$2 = (1 + \frac{0.05}{12})^{12t}$   $\ln(2) = 0.05t \ln e$

$\ln(2) = \ln(1 + \frac{0.05}{12})^{12t}$   $\ln(2) = 0.05t(1)$

$\ln(2) = 12t \ln(1 + \frac{0.05}{12})$   $\ln(2) = 0.05t$

$13.89180473 = t$   $13.86 = t$

$13.86294361 = t$   $13.86 = t$

35. How many years will it take for an initial investment of \$50,000 to grow to \$75,000? Assume a rate of interest of 20% compounded continuously.

It will take about  years for the investment to grow to \$75,000.  
(Round to two decimal places as needed.)

Answer: 2.03

ID: 4.7.41

$A = Pe^{rt}$   $\ln(1.5) = \ln(e^{0.20t})$

$75000 = 50000 e^{0.20t}$   $\ln(1.5) = 0.20t \ln e$

$\frac{75000}{50000} = \frac{50000 e^{0.20t}}{50000}$   $\ln(1.5) = 0.20t(1)$

$1.5 = e^{0.20t}$   $\ln(1.5) = 0.20t$

$2.02732554259 = t$   $2.03 = t$

36. The population of a colony of mosquitoes obeys the law of uninhibited growth. Use this information to answer parts (a) through (c).

(a) If  $N$  is the population of the colony and  $t$  is the time in days, express  $N$  as a function of  $t$ . Consider  $N_0$  is the original amount at  $t = 0$  and  $k \neq 0$  is a constant that represents the growth rate.

$N(t) =$   (Type an expression using  $t$  as the variable and in terms of  $e$ .)

(b) The population of a colony of mosquitoes obeys the law of uninhibited growth. If there are 1000 mosquitoes initially and there are 1300 after 1 day, what is the size of the colony after 4 days?

Approximately  mosquitoes.  
(Do not round until the final answer. Then round to the nearest whole number as needed.)

(c) How long is it until there are 90,000 mosquitoes?

About  days.  
(Do not round until the final answer. Then round to the nearest tenth as needed.)

Answers  $N_0 e^{kt}$

2856

17.2

ID: 4.8.5

$N(t) = N_0 e^{kt}$   $N(t) = N_0 e^{kt}$

$1300 = 1000 e^{k(1)}$   $1300 = 1000 e^k$

$\frac{1300}{1000} = \frac{1000 e^k}{1000}$   $1.3 = e^k$

$\ln(1.3) = \ln(e^k)$



36) p. 12  $\ln(1.3) = k \ln(e)$

$$\ln(1.3) = k(1)$$

$$\ln(1.3) = k$$

$$.2623642695 = k$$

$$.262364 = k \text{ Round}$$

$$N(t) = 1000 e^{.262364t}$$

$$N(4) = 1000 e^{(.262364)(4)}$$

$$N(4) = 2856.096979 \text{ OR}$$

$$N(4) = 2856 \text{ Round}$$

Q  $N(t) = N_0 e^{kt}$

$$90,000 = 1000 e^{.262364t}$$

$$\frac{90,000}{1000} = \frac{1000 e^{.262364t}}{1000}$$

$$90 = e^{.262364t}$$

$$\ln(90) = \ln(e^{.262364t})$$

$$\ln(90) = .262364t \ln(e)$$

$$\ln(90) = .262364t (1)$$

36 part 3

$$h(90) = 0.262364 \text{ €}$$

$$\frac{h(90)}{0.262364} = \frac{0.262364 \text{ €}}{0.262364}$$

$$17.15101774 = \text{€}$$

$$17.2 = \text{€} \quad \text{or Round}$$





37. Solve the system of equations. If the system has no solution, say that it is inconsistent.

*mult*

$$\begin{cases} 2x - 5y = -18 \\ 10x + y = 14 \end{cases} \begin{pmatrix} 1 \\ 5 \end{pmatrix} = \begin{array}{r} 2x - 5y = -18 \\ 50x + 5y = 70 \\ \hline 52x + 0 = 52 \end{array}$$

*52x = 52*  
*52x = 52*  
*52*  
*52*  
*x = 1*

Select the correct choice below and, if necessary, fill in any answer boxes within your choice.

- A. The solution of the system is  $x =$  \_\_\_\_\_ and  $y =$  \_\_\_\_\_.  
(Type an integers or simplified fractions.)
- B. There are infinitely many solutions. Using ordered pairs, the solution can be written as  $\{(x,y) | x =$  \_\_\_\_\_,  $y$  any real number $\}$ .  
(Simplify your answer. Type an expression using  $y$  as the variable as needed.)
- C. The system is inconsistent.

*Subst*

$$\begin{array}{r} 2x - 5y = -18 \\ 2(1) - 5y = -18 \\ 2 - 5y = -18 \\ 2 - 5y - 2 = -18 - 2 \\ -5y = -20 \\ -5y = -20 \\ \hline y = \frac{-20}{-5} \\ y = 4 \end{array}$$

Answer: A. The solution of the system is  $x =$   and  $y =$  .

ID: 6.1.33

*(x, y) = (1, 4)*

38. Solve the given system of equations. If the system has no solution, say that it is inconsistent.

*2nd matrix edit (A), 3x4, full*

$$\begin{cases} x - 3y + 4z = 10 \\ 2x + y + z = 6 \\ -2x + 3y - 3z = -12 \end{cases}$$

*[A] =*

$$\begin{bmatrix} 1 & -3 & 4 & 10 \\ 2 & 1 & 1 & 6 \\ -2 & 3 & -3 & -12 \end{bmatrix}$$

Select the correct choice below and fill in any answer boxes within your choice.

- A. The solution is  $x =$  \_\_\_\_\_,  $y =$  \_\_\_\_\_, and  $z =$  \_\_\_\_\_. (Type integers or simplified fractions.)
- B. There are infinitely many solutions. Using ordered triplets, they can be expressed as  $\{(x,y,z) | x =$  \_\_\_\_\_,  $y =$  \_\_\_\_\_,  $z$  any real number $\}$ .  
(Simplify your answers. Type expressions using  $z$  as the variable as needed.)
- C. There are infinitely many solutions. Using ordered triplets, they can be expressed as  $\{(x,y,z) | x =$  \_\_\_\_\_,  $y$  any real number,  $z$  any real number $\}$ .  
(Simplify your answer. Type an expression using  $y$  and  $z$  as the variables as needed.)
- D. The system is inconsistent.

Answer: A.

The solution is  $x =$  ,  $y =$  , and  $z =$  .

ID: 6.1.45

*2nd, matrix, math, rref()*

$$\text{rref}([A]) = \begin{bmatrix} 1 & 0 & 0 & 3 \\ 0 & 1 & 0 & -1 \\ 0 & 0 & 1 & 1 \end{bmatrix}$$

*(x, y, z) = (3, -1, 1)*



MATH

MATH

MATH is Fun



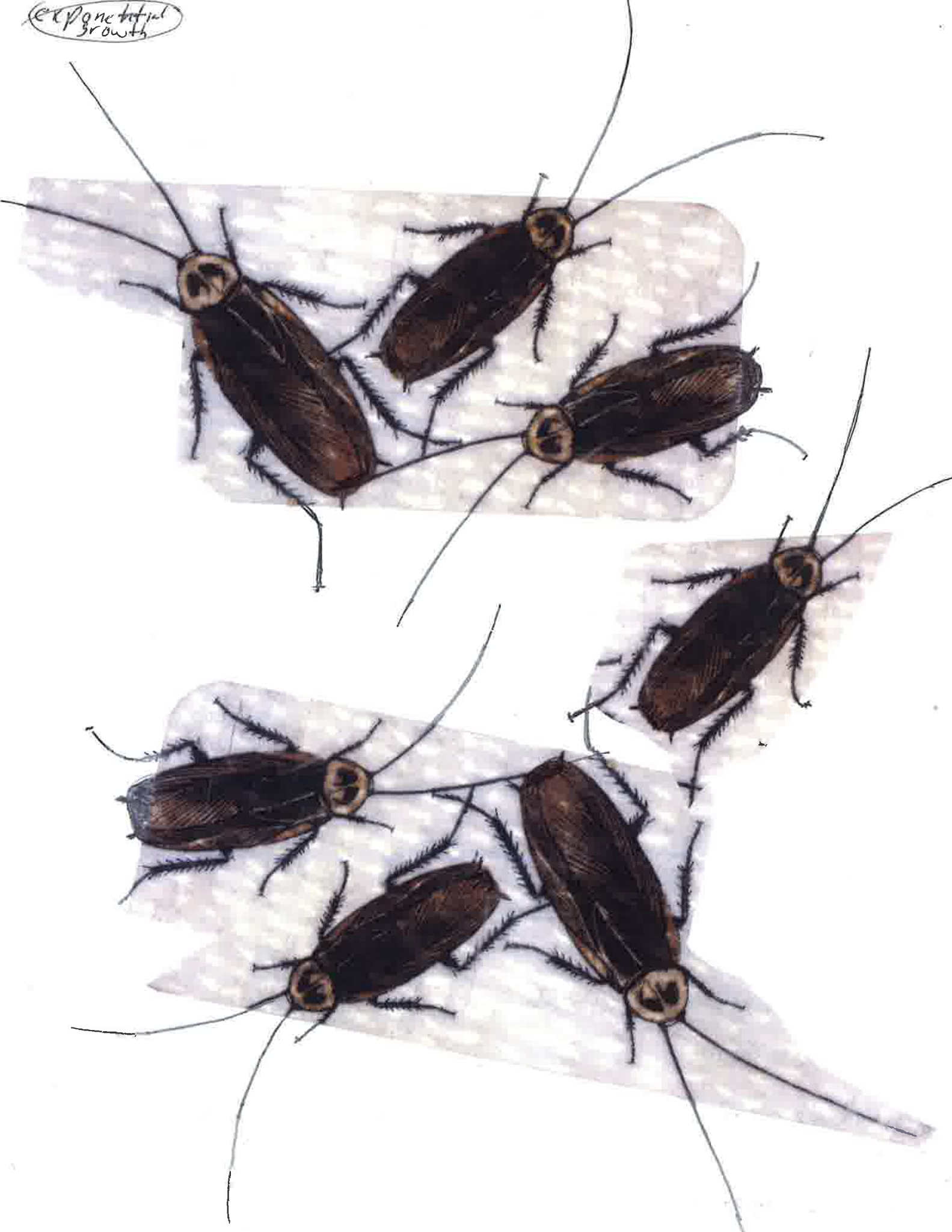
ARIA

AMPRÍ

MATHA  
is  
Fun



exponential  
growth



090316w